ANALYSIS OF SHIP FLOW IN AN IDEAL FLUID USING GUILLOTON'S METHOD AND SPLINE FUNCTIONS

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JIUNN-MING CHUANG







ANALYSIS OF SHIP FLOW IN AN IDEAL FLUID USING GUILLOTON'S METHOD AND SPLINE FUNCTIONS

Jiunn-Ming Chuang, M.Sc. (Eng.)

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C

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ABSTRACT

In this thesis, the numerical evaluation is formulated for computing the linearised disturbance velocity of a steady, invised free surface gravity flow past a ship hull. The hull is represented by a system of source panels with uniformly distributed strengths on the centerplane. The imporvement of the results on the boundaries, i.e. free surface and hull surface, by Guilloton's method is investigated. Based on Guilloton's method, thin-shippanel approximation and cubic spline curve fitting, a scheme has been developed for setting up a computer program to compute theship wave-making resistance, flow around the ship hull and wave elevation along the ship side. The results of sample calculations for standard hull forms of Wigley model 3012 and Series 60 block 60 have shown good agreement with the experimental results for proude numbers between 0.25 and 0.35 which are just in the speed

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NOMENCLATURE Linearized space(LS) = The domain (x_0, y_0, z_0) of the linearized solution. Real space (RS) The domain (x, y, z) of the Guilloton's solution f(x,z), f⁰(x,z) Ship hull functions in RS and LS, respectively. 5(x,y), 5°(x,y) Wave elevations in RS and LS respectively. Wave-making resistances in RS and LS, Ro respectively. Gravitational acceleration. (u,v,w), Disturbance velocity vector. q(x,y,z) Perturbation parameter. G(x,y,z;x',0, z') = Green's function of linearized problem. Re Real part of complex function. Im Imaginary part of complex function. C1, C2 Integrating paths in complex plane. m(x';z') Strength of source distribution on the centerplane. "ij' Vij' Wij Element velocity components induced by a. source panel (i,j) on the centerplane. = . Element wave-making resistance induced by a source panel (i,j) on the centerplane. Element wave-elevation induced by a . source panel (i,j) on the centerplane.

vii = 🔓 Complex integrals I1, I2, 5, IR (N Residue of complex function, f(k), at Res(a) pole k Jsig w . -1 for $\omega < 0$, 1 for $\omega > 0$ = Heaviside "unit step function", H(x - x')0 for x < x', 1 for x > x' $(f(x^{*},z^{*})) \begin{vmatrix} x_{1}^{i} \\ x_{1}^{i} \end{vmatrix} \begin{pmatrix} z_{1}^{i} \\ z_{1}^{i} \end{vmatrix} = (f(x^{*},z^{*})) \begin{vmatrix} x^{*} \\ x^{*} \\ z^{*} \end{vmatrix} = x^{*}_{1} \downarrow_{1} \downarrow_{1} = (f(x^{*},x^{*})) \begin{vmatrix} x^{*} \\ x^{*} \\ z^{*} \end{vmatrix} = x^{*}_{1} \downarrow_{1} \downarrow_{1} = (f(x^{*},x^{*})) \begin{vmatrix} x^{*} \\ x^{*} \\ z^{*} \\ z^{*} \end{vmatrix} = x^{*}_{1} \downarrow_{1} \downarrow_{1} = (f(x^{*},x^{*})) \begin{vmatrix} x^{*} \\ x^{*} \\ z^{*} \\ z^{*} \\ z^{*} \end{vmatrix} = x^{*}_{1} \downarrow_{1} \downarrow_{1} = (f(x^{*},x^{*})) \begin{vmatrix} x^{*} \\ x^{*} \\ z^{*} \\ z^{*} \\ z^{*} \\ z^{*} \end{vmatrix} = x^{*}_{1} \downarrow_{1} \downarrow_{1} = (f(x^{*},x^{*})) \begin{vmatrix} x^{*} \\ x^{*} \\ z^{*} \\ z^{*} \\ z^{*} \\ z^{*} \\ z^{*} \end{vmatrix} = x^{*}_{1} \downarrow_{1} \downarrow_{1} = (f(x^{*},x^{*})) \begin{vmatrix} x^{*} \\ x^{*} \\ z^{*} \\ z^{$ $\{f(x^{\prime},z^{\prime})\}_{z^{\prime}=z^{\prime}i+1}^{z^{\prime}=x^{\prime}i} + \{f(x^{\prime},z^{\prime})\}_{z^{\prime}=z^{\prime}i+1}^{z^{\prime}=z^{\prime}i+1}$ $\int_{0}^{\infty} \frac{e^{-K}}{dK} dK, \ (\lambda \text{ is a complex number}), \text{ or }$ E_1 (λ) called gomplex exponential integral. n or ETA Nondimensional wave elevation. A(x,z,),B(x,z), Displacements of Guilloton's transformation in x_0^- , \dot{y}_0^- and z_0^- directions, respectively. C(x,z) F.P. Forward perpendicular of a ship (-1) After perpendicular of a ship (1) A.P. Rw/(1/20SU²), Wave resistance coefficient 1/2 LBP

CHAPTER 1

INTRODUCTION

Since Michell [1] developed the thin ship theory to solve the linearized problem of the waves produced by a ship of given form moving with uniform velocity in the free surface of unbounded water which is considered to be inviscid, many researchers have tried to modify the thin ship theory to obtain more reasonable results by including the nonlinear effects. From a practical point of view, one of the notable methods was developed by Guilloton [2] based on geometrical and intuitive physical reasoning and was formulated in mathematical form by Gadd [10]. As a matter of fact, Guilloton's basic idea is the same as that of the well-known "strained coordinates method" which was developed by Poincaré and successfully used in some singular perturbation problems [3]. The main idea of this kind of method is that the linearized solution of the nonlinear problem may have the right form, but not guite at the right place, so that the remedy is to slightly strain the coordinates or set up a transformation between the "linearized space" and the "real space". "Following the method of strained coordinates, a perturbation analysis can be carried out to rationalize Guilloton's method, such as in [4] and [5]. They have shown that Guilloton's solution is essentially equivalent to an inconsistent second order approximation, in which the field equation is satisfied to first order and the boundary conditions are satisfied to second order.

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From the computational point of view, Guilloton's method includes the following three sub-procedures: 1. Find the "linearized hull" corresponding to a given "real

hull" for a given Froude number by an "inverse Guilloton's transformation". This is an iterative process.

 Calculate the flow quantities around the "linearized hull" by the thin ship theory.

 Transform the calculated flow quantities to that around the "real hull" by Guilloton's transformation.

Based on these sub-procedures, abcomputer program has been developed to analyse the flow and isobar around the ship hull, the wave elevation along the ship side and the ship wave-making resistance. In mathematical principle, Guilloton's solution is still only of first-order accuracy. But from the results of numerical experiments, the prediction of the ship flow with Guilloton's method is much better than that with the thin shiptheory for Froude numbers of about 0.25 to 0.35. The use of Guilloton's method' for preliminary design of conventional ships/has a good potential.

CHAPTER 2 THEORETICAL BACKGROUND AND NUMERICAL FORMULATION

2.1 Exact and linearized steady ship-flow problem

It is assumed that the fluid is incompressible and inviscid and that the flow is irrotational. Let 0xyz be a moving coordinate system fixed on the ship, with velocity $\vec{U} = (-\vec{y}, 0, 0)$ with respect to the obvious infertial frame and the origin 0 is at midship. The 0xy plane is taken to coincide with the undisturbed free-surface and the x-axis is positive upwards as in Figure 1. The effects of ginkage and trim are not considered. The hull equation is $y = \pm f(x, z)$ for $-1 \le x \le 1$, $-b(x) \le z \le (-1x, y)$, where 2L is the length of the ship, z = z (x, y) denotes the elevation of the disturbed free surface and z = -b(x) is the equation of the keel line. Now, the problem of evaluating the ship flow is reduced to determine the disturbance velocity potential, say/ $g(x, y_z)$, which satisfies Laplace's equation, $v_z^2 = 0$, in the flow field with the following exact boundary conditions as given in [6]:

(a) The kinematic boundary condition on the hull surface:

 $\phi_{\mathbf{X}}(\mathbf{x}, \underline{\pm}\mathbf{f}(\mathbf{x}, \mathbf{z}), \mathbf{z}) \mathbf{f}_{\mathbf{X}}(\mathbf{x}, \mathbf{z}) \mp \phi_{\mathbf{Y}} + \phi_{\mathbf{Z}}\mathbf{f}_{\mathbf{Z}} = -\mathbf{U}\mathbf{f}_{\mathbf{X}}$ (11)

(b) The kinematic boundary condition on the free surface:

 $\phi_{x}(x, y, \zeta(x, y)) \zeta_{x}(x, y) + \phi_{y} \zeta_{y} - \phi_{z} = -U \zeta_{x}$ (1.2)

(c) The dynamic boundary condition on the free surface: $Ug'_{\chi}(x,y,\zeta(x,y)) = \frac{1}{2} \frac{1}{2} (g'_{\chi}^2 + g'_{\chi}^2 + g'_{\chi}^2) + g \zeta(x,y) = 0$ (1.3) (d) The kinematic boundary condition on the ocean bottom, (it is assumed to be infinite): as _ z' ->

 $\phi_{\alpha}(\mathbf{x},\mathbf{y},\mathbf{z}) = 0$

(e) The radiation condition specifying that waves are not propagated upstream from the ship but only downstream.

If the disturbance velocity potential of can be found, then the disturbance velocity, $\dot{q}_{(x,y,z)}$, the wave-making resistance, R, and the wave elevation, $\zeta(x,y)$, can be calculated as follows:.

 \vec{q} (x,y,z) = $\nabla \phi(x,y,z)$ (1.5)

 $R = \iint_{hull} p \cos(n; x) ds = 2 \iint_{S_{a}} p(x_{i}f(x, z), z) f_{x}(x, z) dxdz$

 $= -2\rho \int \int \left[U\phi_{x}^{2}(x,f(x,z),z) + \frac{1}{2}(\phi_{x}^{2} + \phi_{y}^{2} + \phi_{z}^{2}) + gz \right] f_{x}(x,z) dxdz$

and $\zeta(x,y) = -\frac{1}{g} [U\phi_x(x,y,\zeta(x,y)) + 1/2(\phi_x^2 + \phi_y^2 + \phi_z^2)]$

* (1.6)

(1:4)

where S is the projection of the wetted surface on the centerplane and p is the pressure on the ship hull.

The formula for the wave elevation is an implicit form since the right hand side of (1.7) is also a function of wave elevation.

The difficulty of this "exact" problem stems from the fact that the position of the free surface and the extent of the wetted area of the hull surface are initially unknown and are to be determined as part of the solution; elso the boundary conditions are non-linear: One of the procedures for linearizing the problem begins by writing the equation of the whip hull in the form y = tf(x,z) where ε is a beam-length ratio. It is assumed that the disturbance velocity potential, wave elevation and wave-making resistance can be expanded in power series of ε as follows:

 $\phi(x,y,z;\varepsilon) = \varepsilon \phi^{(1)}(x,y,z) + \varepsilon^2 \phi^{(2)} + \ldots$

 $\zeta(\mathbf{x},\mathbf{y};\varepsilon) = \varepsilon \zeta^{(1)}(\mathbf{x},\mathbf{y},z) + \varepsilon^2 \zeta^{(2)} + \dots$

 $R(\varepsilon) = \varepsilon^2 R^{(1)} + \varepsilon^3 R^{(2)} + .$

The expansions (1,6) are now substituted into (1,1) to (1,4). After the have been expanded as a power series in e_i it is found that the velocity potential ϕ of the first grap approximation must satisfy Leplace's equation together with the following linearized boundary conditions:

(1.8

(119

(a) $\phi_{y}(x, \pm 0, z) = Uf_{x}(x, z)$

(b) $\phi_{z}(x,y,0) = Uc_{x}(x,y)$ (1.10)

(c) $\zeta(x,y) = -\frac{U}{V} \phi_x(x,y,0)$

(e) 'The radiation condition mentioned before.

The wave-making resistance is changed from (1.6) to the following form

 $R = -2\rho U \int \int \phi_{\mathbf{X}}(\mathbf{x}, \mathbf{0}, \mathbf{z}) \mathbf{f}_{\mathbf{X}}(\mathbf{x}, \mathbf{z}) d\mathbf{x} d\mathbf{z}$ (1.13) S₀

where S_0 is the ship centerplane for $-L \leq x \leq L$, and

 $-b(x) \le z \le 0$. The free-surface boundary conditions (1.10) and (1.11), are combined to give

 $\phi_{XX}(x,y,0) + K_0 \phi_z = 0$ where $K_0 = \frac{g}{U^2}$ (1.14)

2.2 Solution of linearized ship-flow problem

The linearized ship flow problem is a mathematical boundaryvalue problem which can be solved by the Green's function method (7), i.e. representing the body by a distribution of singularities. The linearized disturbance velocity potential can be expressed in the form

 $\phi(x, y, z) = \iint_{X'} 2Uf_{X'}(x', z') \cdot G(x, y, z; x', 0, z') dx' dz'$ (2.1)

where.

G(x,y,z;x',0,z') is Green's function or the unit source function

of the linearized problem.

 $f_{\chi^{\prime}}(x^{\prime},z^{\prime})$ is the longitudinal slope of ship hull. The "prime" system also denotes coordinates on the body.

In this linearized solution, equation (2.1) shows that the sources are distributed on the ship centerplane and the source strength is only dependent on the longitudinal slope of the ship hull. We define the source strength $m(x',z') = 2Uf_{\chi'}(x',z')$ and equation (2.1) becomes

 $\phi(x,y,z) = \int \int m(x',z') G(x,y,z;x',0,z') dx' dz'$ (2.2)

Green's function of the linearized problem developed by Havelock, [8] with the image method is given in the following form

 $4\pi G(x, y, z; x^{\prime}, 0, z^{\prime}) = -\frac{1}{r_{1}} + \frac{1}{r_{2}}$

+ $\frac{{}^{1}K_{O}}{\pi}$ Re{ ${}^{1}\int_{-\pi}^{\pi}$ sec² $\theta d\theta \int_{0}^{\infty} \frac{e^{K[(z+z')+i\omega]}}{K-K_{O}sec^{2}\theta} dK$ }

(2.3)

 $1 = [(x-x^{2})^{2} + y^{2} + (z-z^{2})^{2}]^{1/2}$

 $r_2 = [(x-x^2)^2 + y^2 + (z+z^2)^2]^{1/2}$

 $(x-x^2) \cos \theta + y \sin \theta$

and $K_0 = g/U^2$

where

The double integral of Green's function cannot be determined without a statement on the procedure of integration around the singularity, $X = X_0 \sec^2 \theta$. That is to say that a way (as in [9]) should be chosen such that the free waves only trail behind the ship. The radiation condition mentioned above makes the solution to this mathematical problem unique.

Let

 $I = R_{e} \left\{ \int_{-\pi}^{\pi} \sec^{2} \theta d\theta \int_{\sigma}^{\infty} \frac{e^{K[(z+z')+i\omega]}}{\kappa - \kappa_{o} \sec^{2} \theta} dK \right\}$

The integration paths, C_1 and C_2 , have to be chosen as follows:

 $= R_{e} \left\{ \begin{array}{c} \frac{\pi/2}{\int} \sec^{2}\theta d\theta \left[\int_{-\pi/2}^{\pi} \frac{e^{K\left[\left(2\pi z^{*} \right) + i\omega \right]}}{K - K_{o} \sec^{2}\theta} dK + \int_{(C_{2})}^{\infty} \frac{e^{K\left[\left(2\pi z^{*} \right) - i\omega \right]}}{(C_{2})} dK \right] \right\}$





(2.4)

(2.5)

we define

 $I_{1} = \int_{C_{1}} \frac{e^{K[(z+z')+i\omega]}}{K-K_{0}\sec^{2}\theta} dK$ and C₂ K-K_osec²0

 ${\tt I}_1$ and ${\tt I}_2$ can be treated by contour integration in the complex plane to obtain a nonoscillatory integrand.

(1) When $\omega > 0$

(a) Integral I



 $I_1 = 2\pi i \operatorname{Res}(a) -, I_s \qquad (\lim_{R^+ \infty} I_R = 0)$ (2.6)

 $2\pi i \operatorname{Res}(a) = 2\pi \{ e^{K_{o} \sec^{2}\theta (z+z')} [-\sin(K_{o} \sec^{2}\theta \cdot \omega) + i \cos(K_{o} \sec^{2}\theta \cdot \omega)] \}$

 $I_{S} = \int_{S} \frac{e^{K[(z+z') + i\omega]}}{K - K_{-} \sec^{2} \theta} dx$ (2.8)

The path S can be chosen so as to make the argument of the exponential real along the path and hence eliminating the oscillatory behaviour of the integrand in $I_{\rm e}$. So

Im $\{K[(z+z') + i\omega]\} = 0$ and $K = k_1 + ik_2$ (2.9)

(2.10)

 $k_2 = -\omega k_1 / (z+z')$, $K = k_1 [(z+z')-i\omega] / (z+z')$

Substituting (2.10) into (2.8)

$$I_{S} = \int_{0}^{0} \frac{e^{\left[\left(z+z^{\prime}\right)^{2}+u^{2}\right]} k_{1}/(z+z^{\prime})}{\left[\left(z+z^{\prime}\right)^{2}+u^{2}\right] k_{1}/(z+z^{\prime}) - \kappa_{0}\sec^{2}\theta\left[\left(z+z^{\prime}\right)+i\omega\right]}}.$$
(2.11)
since $z+z^{\prime} < 0$
changing variable let $-K = \left[(z+z^{\prime})^{2} + u^{2}\right] k_{1}/(z+z^{\prime})$
 $I_{S} = -\int_{0}^{\pi} \frac{e^{-K}}{\left[K+\kappa_{0}\sec^{2}\theta + (z+z^{\prime})+i(\kappa_{0}\sec^{2}\theta,\omega)\right]} dK$ (2.12)
Substituting (2.7) and (2.12) into (2.6) and taking the real part
 $Re\{I_{1}\} = \int_{0}^{\pi} \frac{\left[(k+\kappa_{0}\sec^{2}\theta + (z+z^{\prime}))e^{-K}\right]}{\left[(K+\kappa_{0}\sec^{2}\theta + (z+z^{\prime}))e^{-K}\right]} dK$
 $-2\pi e^{\kappa_{0}\sec^{2}\theta + (z+z^{\prime})} \sin(\kappa_{0}\sec^{2}\theta,\omega)$ (2.13)
(b) Integral I_{2}
 $ik_{2} = a = \kappa_{0}\sec^{2}\theta$

$$11$$

$$I_{2} = -2\pi i \operatorname{Res}(a) - I_{5} \qquad (\lim_{R \to a} I_{R} = 0) \qquad (2.14)$$

$$-2\pi i \operatorname{Res}(a) = 2\pi \{a^{K_{0} \otimes c^{2}\theta} \cdot (z + z^{*}) = -i \operatorname{cos}(K_{0} \otimes c^{2}\theta \cdot \omega) - i \operatorname{cos}(K_{0} \otimes c^{2}\theta \cdot \omega))\}$$

$$I_{5} = \int_{5}^{c} \frac{e^{K[(z + z^{*}) - i\omega]}}{K - K_{0} \otimes c^{2}\theta} dK$$

$$(2.15)$$

$$I_{5} = \int_{5}^{c} \frac{e^{K[(z + z^{*}) - i\omega]}}{K - K_{0} \otimes c^{2}\theta} dK$$

$$I_{5} = u k_{1} / (z + z^{*}) = 0 \quad \text{and} \quad K = k_{1} + i k_{2} \qquad (2.17)$$

$$k_{2} = u k_{1} / (z + z^{*}) \quad K = k_{1} [(z + z^{*}) + i\omega] / (z + z^{*}) \qquad (2.18)$$
Substituting (2.18) Anto (2.16).
$$I_{5} = \int_{0}^{0} \frac{e^{[(z + z^{*})^{2} + \omega^{2}]k_{1} / (z + z^{*})}}{[(z + z^{*})^{2} + \omega^{2}]k_{1} / (z + z^{*}) - K_{0} \sec^{2}\theta[(z + z^{*}) - i\omega]}$$

$$= \frac{[(z + z^{*})^{2} + \omega^{2}]}{(z + z^{*})} dk_{1} \qquad (2.19)$$
since $z + z^{*} < 0$
changing.variable let $- K = [(z + z^{*})^{2} + \omega^{2}]k_{1} / (z + z_{0})$

$$I_{5} = -\int_{0}^{z} \frac{e^{-K}}{[K + K_{0} \sec^{2}\theta \cdot (z + z^{*})] - i (K_{0} \sec^{2}\theta \cdot \omega)} dK \qquad (2.20)$$

Substituting (2.15) and (2.20) into (2.14) and taking the real part $\operatorname{Re} \left\{ \mathtt{I}_{2} \right\} = \int_{0}^{\infty} \frac{[\mathtt{K} + \mathtt{K}_{0} \sec^{2} \theta \cdot (\mathtt{z} + \mathtt{z}')] e^{-\mathtt{K}}}{[\mathtt{K} + \mathtt{K}_{0} \sec^{2} \theta \cdot (\mathtt{z} + \mathtt{z}')]^{2} + (\mathtt{K}_{0} \sec^{2} \theta \cdot \omega)^{2}} d\mathtt{K}$ $\chi_{0}^{K} \sec^{2\theta} \cdot (z+z^{2}) = \sin(K_{0} \sec^{2\theta} \cdot \hat{\omega})$ (2:21) Substituting (2.13) and (2.21) into (2.4), the integral I for ω > 0·is $\mathbf{I} = 2 \int_{-\pi/2}^{\pi/2} \sec^2 \theta d\theta \int_{0}^{\infty} \frac{[K+K_{0} \sec^2 \theta. (z+z')]e^{-K}}{[K+K_{0} \sec^2 \theta. (z+z')]^{2} + (K_{0} \sec^2 \theta. \omega)^{2}}$ $- 4\pi \int_{z}^{\pi/2} \frac{k_{o}^{2} ec^{2} \theta \cdot (z+z^{2})}{\sec^{2} \theta \cdot e} \sin(k_{o}^{2} ec^{2} \theta \cdot \omega) d\theta \quad (2.22)$ When w Similarly, the contour integrations are chosen as (a)

The following result for $\omega < 0$, can be obtained

Since most of the quantities of practical interests, such as wave-making resistance, wave elevation along the ship hull and flow around the ship hull can be obtained from flow variables evaluated at the centerplane, the linearized disturbance velocity

potential on the centerplane, $\phi(x, 0, z)$, associated with a given source distribution m(x',z'), is the most important quantity to be defined in the computational procedure: ϕ (x,0,z) - = $\iint m(x',z')$. G(x,0,z;x',0,z') dx'dz'(2.25) with $4\pi G(x,0,z;x',0,z') = -\frac{1}{r_1} + \frac{1}{r_2}$ $+\frac{4K_{o}}{\pi}\int_{0}^{\pi/2}\sec^{2}\theta d\theta \int_{0}^{\infty}\frac{[K+K_{o}sec^{2}\theta.(A+z^{\prime})]e^{-K^{\prime}}}{[K+K_{o}sec^{2}\theta.(z+z^{\prime})]^{2}+(K_{o}sec^{2}\theta\cdot\omega)^{2}}$ $-H(x-x^{\prime}) \ \text{BK} \int_{0}^{\pi/2^{\prime}} \sec^{2\theta} \cdot e^{-\frac{\pi}{2}\theta \cdot (z+z^{\prime})} \cdot \sin(\pi \sec^{2\theta} \cdot \omega) d\theta$ (2.26) where $r_1 = [(x-x')^2 + (z-z')^2]^{1/2}$ $r_2 = [(x-x')^2+(z+z')^2]^{1/2}$ (x-x') cos8 and H(x-x') is the Heaviside "unit step function" which is defined as $H(x-x') = \begin{cases} 0 & \text{for } x < x' \\ 1 & \text{for } x > x' \end{cases}$

Substituting (2.25) and (2.26) into the resistance formula (1.13), only the last integral in the expression for G leads to a nonzero term. This gives the well-known Michell's integral of ship wave-making resistance:

$$R = \frac{\rho K_0^2}{\pi} \frac{\pi/2}{\pi} \left[P(\theta)^2 + Q(\theta)^2 \right] \sec^3 \theta d\theta \qquad (2.27)$$

with $P(\theta) = \int \int m(x',z')e^{-x} \cos(K_0 \sec\theta \cdot x')dx'dz'$

and $Q(\theta) = \iint m(\mathbf{x}', \mathbf{z}') e^{K_0 \sec^2 \theta \cdot \mathbf{z}'}$. $\sin(K_0 \sec \theta \cdot \mathbf{x}') d\mathbf{x}' d\mathbf{z}'$

Similarly, substituting (2.25) and (2.26) into the wave elevation formula (1.11), the wave elevation along the ship hull can be written as

$$\zeta(\mathbf{x},0) = -\frac{U}{g} \iint_{S_{0}} m(\mathbf{x}^{*},\mathbf{z}^{*}) G_{\mathbf{x}}(\mathbf{x},0,0;\mathbf{x}^{*},0,\mathbf{z}^{*}) d\mathbf{x}^{*} d\mathbf{z}^{*}$$
(2.28)

The disturbance velocity components around the ship hull can also be obtained in terms of Green's function and source distribution:

$$u(x,0,z) = \phi_{x}(x,0,z) = \int \int m(x^{\prime},z^{\prime})G_{x}(x,0,z;x^{\prime},0,z^{\prime})dx^{\prime}dz^{\prime}$$

So
(2.29)

$$v(x,0,z) = Uf_{x}(x,z) = \frac{1}{2} m(x,z)$$
 (2.30)

 $N_{(x,0,z)} = \phi_{z}(x,0,z) = \int m(x',z')G_{z}(x,0,z;x',0,z')dx'dz'$

(2.31)

2.3 Thin-ship-panel approximation

In order to evaluate the numerical value of wave-making resistance (2.27), wave elevation along the ship hull (2.28), and disturbance velocity gomponents around the ship hull (2.29), (2.30) and (2.31), the ship centerplane is discretized into a system of source ganels with associated strengths, m_{ij} , i = 1, 2, ..., M, j = 1, 2, ..., N. It is assumed that the strength is uniformly distributed over each source ganel, so that the strength in the above equations can be taken out of the integral sign for each source ganel. Furthermore, Green's function (2.26) can be separated into three parts as

$$\begin{split} G(x,0,z;x^{*},0,z^{*}) &= G_{1}(x,0,z;x^{*},0,z^{*}) + G_{2}(x,0,z;x^{*},0,z^{*}) + \\ G_{3}(x,0,z;x^{*},0,z^{*}), \end{split} \tag{3.1}$$

where

$$G_1(x,0,z;x',0,z') = \frac{1}{4\pi} \left(-\frac{1}{r_1} + \frac{1}{r_2}\right)$$

G2 (x,0,z;x',0,z')

$$\frac{K_0}{\pi^2}\int_0^{\pi/2} \sec^2\theta d\theta \int_0^{\infty} \frac{[X+K_0\sec^2\theta\cdot(z+z^{\prime})]e^{-K}}{([X+K_0\sec^2\theta\cdot(z+z^{\prime})]^2+(K_0\sec^2\theta\cdot\omega)^2} dK \quad (3.$$

(z+z *)

$$G_{3}(x,0,z;x',0,z') = \left| -H(x-x') \frac{\frac{2K_{0}}{\pi}}{\int_{0}^{\pi}} \int_{-\frac{K_{0}}{\pi}}^{\frac{\pi}{2}} \int_{0}^{\frac{\pi}{2}} \frac{K_{0} \sec^{2}\theta}{\sec^{2}\theta \cdot e} \right|^{2}$$

 $. sin(K_sec^2\theta/\omega)d\theta$

for G1: contribution of the radical term

G2: contribution of the double integral term

G: contribution of the single integral term ,

Let us first assume there is a single source panel (i,j) with unit strength below the undisturbed free surface in a uniform stream of velocity U in the direction of the positive x-axis and the coordinates of four corner points of this source panel are (x_i^*, z_j^*) , (x_{i+1}^*, z_j^*, t_i) and (x_i^*, z_{j+1}^*) respectively. Then the elemental quantities induced by this source panel are as follows: (1) The elemental disturbance velocity components, u_{ij}^* , v_{ij} and w_{ij} , on the centerplane.

From linearized boundary condition (1.9), once the source strength is given, the v-component velocity on the centerplane is determined. Only u-component and v-component velocities should be computed. We separate velocity components into three parts corresponding to the three parts of Green's function as in (5.1):

 $u_{ij}(x,0,z) = u_1(x,0,z) + u_2(x,0,z) + u_3(x,0,z)$

 $w_{ii}(x,0,z) = w_1(x,0,z) + w_2(x,0,z) + M_3(x,0,z)$

(3.6)

Equation (3.9) can be simplified as follows:

Let $I_1 = \int_{-\infty}^{\infty} e^{-K} \left[\log \left[\left(K + K_0 \sec^2 \theta \cdot (z + z^{-1}) \right)^2 + \left(K_0 \sec^2 \theta \cdot \omega \right)^2 \right] \right] dK$ (3.10)

. .

Integrating by parts

 $I_1 = 2 \log (K_{0} \sec^2 \theta) + \log [(z+z')^2 + \omega^2]$

 $+ 2 \int \frac{1}{(\mathbf{k} + \mathbf{K}_{O} \sec^2 \theta \cdot (\mathbf{z} + \mathbf{z}^{-})) \mathbf{e}^{-\mathbf{K}}} \frac{1}{(\mathbf{k} + \mathbf{K}_{O} \sec^2 \theta \cdot (\mathbf{z} + \mathbf{z}^{-}))^2 + (\mathbf{K}_{O} \sec^2 \theta \cdot \omega)^2} d\mathbf{k} \cdot \mathbf{e}^{-\mathbf{K}_{O}} \mathbf{e$

(3,11).

(3.12)

The integral part of I can be written in the complex form as

 $\operatorname{Re}'\left(\int^{\sigma} \frac{e^{-K}}{[K+K_{o}\operatorname{sec}^{2}\theta\cdot(z+z^{\prime})]+1}(K_{o}\operatorname{sec}^{2}\theta\cdot\omega)'\right)$

= $\operatorname{Re}\left\{e^{\lambda}\int_{1}^{\infty}\frac{e^{-K}}{K}dK\right\}$

= Re $\{e^{\lambda}E_{1}(\lambda)\}$

where.

 $E_1(\lambda)$ is a complex exponential integral

and $\lambda = K_0 \sec^2 \theta [(z+z')+i\omega]$

(a) The contribution of the radical term G_1

$$u_{1}(x,0,z) = \int_{z_{j}}^{z_{j+1}} x_{1}^{x_{1+1}} \frac{\partial G_{1}}{\partial x} dx' dz$$

$$\frac{1}{4\pi} \left\{ \log \left[(z'-z) + \sqrt{(x'-z)^2 + (z'-z)^2} \right] - \log \left[(z'+z) + \sqrt{(x'-z)^2 + (z'-z)^2} \right] \right\}$$

$$\left\{ \left(x^{-x} \right)^{2} + \left(z^{-x} \right)^{2} \right\}^{1} \left| x_{1}^{x_{1}} \right| \left| x_{1}^{z_{1}} \right| \left| z_{1}^{z_{1}} \right|$$

$$w_{1}(\mathbf{x}, \mathbf{0}, \mathbf{z}) = \begin{array}{c} \mathbf{x}_{1} + \mathbf{z}^{\mathbf{b}} & \mathbf{z}_{1} + \mathbf{1} \\ \mathbf{x}_{1} & \mathbf{z}_{1} \\ \mathbf{x}_{1} & \mathbf{z}_{1} \end{array} \quad \frac{\partial \mathbf{G}_{1}}{\partial \mathbf{z}} \quad \mathrm{d}\mathbf{z}^{*}$$

$$\frac{\frac{1}{4\pi} \left[\log \left[(x'-x) + \frac{1}{(x'-x)^2 + (x'-x)^2} \right]_1^{2} + \log \left[(x'-x) + \frac{1}{(x'-x)^2 + (x'-x)^2} \right]_1^{2} \right]_{x_1}^{x_1' + 1} \left[\frac{x'_{1+1}}{x_1'} \right]_{x_1'}^{x_1' + 1}$$

(b) The contribution of the double integral term G2

$$z_{j+1} = x_{i+1} \frac{\partial G_2}{\partial x} dx' dz'$$

 $= \frac{-1}{\log^2} \int_{0}^{\pi/2} d\theta \int_{0}^{\infty} e^{-K} \{ \log \left[\left(K + K_0 \sec^2 \theta \cdot (z + z^{-1}) \right)^2 + \left(K_0 \sec^2 \theta \cdot \omega \right)^2 \right] \}$

$$32$$
Substituting (3.11) and (3.12) into (3.9)

$$u_{2}(x,0,z) = \frac{-1}{2\pi^{2}} \int_{0}^{\pi/2} \left\{ 2 \log(K_{0} \sec^{2}\theta) + \log[(z+z^{+})^{2} + u^{2}] + 2 \operatorname{Re}\left[e^{\frac{1}{2}} \underline{r}_{1}(\lambda)\right]\right\} \left\| \begin{array}{c} x_{1}^{+1} \\ x_{1}^{-1} \end{array} \right\| \left\| \begin{array}{c} x_{2}^{-1} \\ z_{3}^{-1} \end{array} \right\| \left\| \begin{array}{c} x_{1}^{-1} \\ z_{2}^{-1} \end{array} \right\| \left\| \begin{array}{c} x_{1}^{-1} \\ z_{2}^{-1} \end{array} \right\| \left\| \begin{array}{c} x_{1}^{-1} \\ z_{3}^{-1} \end{array} \right\| \left\| \begin{array}{c} x_{1}^{-1} \\ z_{1}^{-1} \end{array} \right\| \left\| \begin{array}{c} x_{1}^{-1} \\ z_{2}^{-1} \end{array} \right\| \left\| \begin{array}{c} x_{1}^{-1} \\ z_{1}^{-1} \end{array} \right\| \left\| x_{1}^{-1} \\ x_{1}^{-1} \end{array} \right\| \left\| x_{1}^{-1} \\ x_{1}^{-1} \end{array} \right\| \left\| x_{1}^{-1} \\ x_{1}^{-1} \\ x_{1}^{-1} \\ x_{1}^{-1} \end{array} \right\| \left\| x_{1}^{-1} \\ x$$

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The elemental wave-making resistance R (2) $R_{ij} = \frac{\rho K_0^2}{\pi} \cdot \int_{\alpha}^{\pi/2} \left[P_{ij}^2\left(\theta\right) + Q_{ij}^2\left(\theta\right)\right] \sec^3\theta d\theta$ $\begin{array}{c} \mathbf{z}_{j+1} \cdot \mathbf{x}_{i+1} \cdot \mathbf{x}_{o} \sec^2 \boldsymbol{\theta} \cdot \mathbf{z}' \\ \mathbf{P}_{ij}(\boldsymbol{\theta}) &= \int \int f_i \cdot \mathbf{z}'_i \cdot \mathbf{x}'_i \cdot \mathbf{e}^{o} \sec^2 \boldsymbol{\theta} \cdot \mathbf{z}' \cdot \cos(K_o \sec^2 \boldsymbol{\theta} \cdot \mathbf{x}') d\mathbf{x}' d\mathbf{z}' \end{array}$ $= \frac{1}{K_{c}^{2} \sec^{3} \theta} \left\{ \begin{pmatrix} K_{o} \sec^{2} \theta \cdot z_{j} + 1 \\ e \end{pmatrix} - e^{K_{o} \sec^{2} \theta \cdot z_{j}} \right\}.$ $[\sin(K_{o} \sec\theta \cdot x_{i+1}) - \sin(K_{o} \sec\theta \cdot x_{i})] \}$ $Q_{ij}(\theta) = \int_{z'_1} \int_{z'_1} e^{\varphi \sec^2 \theta \cdot z'} \cdot \sin(K_0 \sec \theta \cdot x') dx' dz'$ $= \frac{-1}{K_{o}^{2} \sec^{3} \theta} \left\{ \left(e^{K_{o} \sec^{2} \theta \cdot z_{j+1}} - e^{K_{o} \sec^{2} \theta \cdot z_{j}} \right) \right\}$. $\{\cos(K_{o} \sec\theta \cdot x_{i+1}) - \cos(K_{o} \sec\theta \cdot x_{i})\}\}$ Let $P_{ij}(\theta) = \frac{1}{K_{a}^{2} \sec^{3} \theta} \overline{P}_{ij}(\theta) \text{ and } Q_{ij}(\theta) = \frac{-1}{K_{a}^{2} \sec^{3} \theta} \overline{Q}_{ij}(\theta)$ The elemental wave-making resistance becomes $R_{ij} = \frac{\rho}{\pi K_{o}^{2}} \int_{0}^{\pi/2} [\overline{P}_{ij}^{2}(\theta) + \overline{Q}_{ij}^{2}(\theta)] \cos^{3}\theta d\theta$ (3.24)

where

$$F_{ij}(\theta) = \left[e^{K_0 \sec^2 \theta \cdot \mathbf{z}_{j+1}} - e^{K_0 \sec^2 \theta \cdot \mathbf{z}_{j}}\right] \left[\sin(K_0 \sec\theta \cdot \mathbf{x}_{i+1}) - \sin(K_0 \sec\theta \cdot \mathbf{x}_{i})\right]$$

$$= \sin(K_0 \sec\theta \cdot \mathbf{x}_{i})$$

$$(\overline{o}_{ij}(\theta) = \left(e^{K_0 \sec^2 \theta \cdot \mathbf{z}_{j+1}} - e^{K_0 \sec^2 \theta \cdot \mathbf{z}_{j}}\right) \left[\cos(K_0 \sec\theta \cdot \mathbf{x}_{i+1}) - \cos(K_0 \sec\theta \cdot \mathbf{x}_{i})\right]$$

$$(3) \text{ The elemental wave elevation } \zeta_{ij}(\mathbf{x}, 0, 0)$$

$$\zeta_{ij}(\mathbf{x}, 0, 0) = -\frac{U}{g} \int_{\mathbf{z}_{j}}^{\mathbf{z}_{j+1}} \int_{\mathbf{x}_{1}}^{\mathbf{x}_{1}+1} \frac{3G}{2\pi} d\mathbf{x}' d\mathbf{z}' = -\frac{U}{g} \int_{\mathbf{u}_{1}}^{\mathbf{u}} (\mathbf{x}, 0, 0)$$

$$(3) \text{ The total quantities induced by a system of source panels (i,j) = 1, 2, \dots, M, J=1, 2, \dots, M, a speciated with a system of the elemental guantities induced by a concert panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental guantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental guantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quantities induced by each source panel as the summation of the elemental quanti$$

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follows:

(a) The disturbance velocity components u(x,0,z), v(x,0,z)and w(x,0,z)

 $u(x,0,z) = \sum_{\substack{z \\ j=1}}^{N} \sum_{\substack{i=1 \\ i=1}}^{M} u_{ij}(x,0,z)$ (3.26)

$$v(x,0,z) = Uf_{x}(x,z) = \pi(x,z)/2$$
 (3.27)

$$w(x,0,z) = \sum_{j=1}^{N} \sum_{i=1}^{M} m_{ij} w_{ij}(x,0,z)$$
(3.28)

(b) The wave-making resistance R

$$R = \frac{\rho}{\pi \kappa_{o}^{2}} \int_{0}^{\pi/2} \left[\overline{P}^{2}(\theta) + \overline{Q}^{2}(\theta)\right] \cos^{3}\theta d\theta \qquad (3.29)$$

where

$$\overline{\mathbf{F}}(\boldsymbol{\theta}) = \sum_{j=1}^{N} \sum_{i=1}^{M} m_{ij} \overline{\mathbf{F}}_{ij}(\boldsymbol{\theta}) \\ \vdots \\ \overline{\mathbf{O}}(\boldsymbol{\theta}) = \sum_{i=1}^{N} \sum_{j=1}^{M} m_{ij} \overline{\mathbf{O}}_{ij}(\boldsymbol{\theta})$$

(c) The wave elevation $\zeta(x,0,0)$

$$\zeta(x,0,0) = -\frac{U}{g}\sum_{j=1}^{N} \prod_{i=1}^{M} m_{ij} u_{ij}(x,0,0) = -\frac{U}{g} u(x,0,0)$$

(3.30)

Defining the nondimensional wave elevation/ $\eta = c/(\frac{U^2}{2g})$, then $\eta(x,0,0) = -2\frac{v \cdot u(x,0,0)}{U}$ (3.31)
2.4 Guilloton's Transformation:

Since in the thin ship theory, flow conditions on the hull surface, for example at a point P_1 in Fig. 2, are actually evaluated at P_0 on the centerplane, Guilloton argues that if a transformation is to be applied to the y_0 -direction in this way, similar transformations may be applied to the x_0 - adirections. It is assumed that the time taken by a fluid particle to traverse the isobar from the forward perpendicular (P.P.) to a point P(x,y,z) on the ship hull in the real space (RS) is approximately equal to x_0/u , the linearized estimate of flow time from P.P. to the corresponding point $P_0(x_0,0,z_0)$ in the linearized space (LS), where the flow velocity evaluated at the point P_0 should apply at the point P(as in Fig. 2)[10].

dt = dx / U in LS

 $\begin{array}{rcl} \mathrm{d} t &=& \mathrm{d} s/\left(\mathbb{U}+u\left(x,y,z\right)\right) = \mathrm{d} s/\left(\mathbb{U}+u_{0}\left(x_{0},0,z_{0}\right)\right) \text{ in RS} \\ & & & & \\ \mathrm{for } \mathrm{d} s &=& \left[1+\left(\frac{\partial y}{\partial x}\right)^{2}+\left(\frac{\partial z}{\partial x}\right)^{2}\right]^{1/2} \mathrm{d} x \stackrel{\sim}{\sim} (1+\alpha^{2}/2) \mathrm{d} x \\ & & & \\ \mathrm{where } \alpha = \frac{\partial y}{\partial x}, \text{ s is the distance along the isobar.} \end{array}$

Hence, the transformation in the x_o-direction is $x = x_{o} + \int_{P,P}^{X_{o}} \frac{u_{o}(x_{o}, \theta, z_{o})/U - \alpha^{2}/2}{1 + \alpha^{2}/2} dx_{o}$ (4.1)

The transformation in the y_0 -direction is the same as that in the thin ship theory.

Since the fluid particle should be on the isobar, the transformation in the $z_{\rm p}{-}{\rm direction}$ (refer to (1.11)) is

 $y = y_{O} + \int_{P_{O}}^{X_{O}} \frac{m(x_{O}, z_{O})}{2U} dx_{O}$ ($y_{O} = 0$)

 $z = z_0 - \frac{U}{a} u_0(x_0, 0, z_0)$ (4.3)

From the geometrical point of view, the mapping function (4.1) maps a horizontal straight line on the centerplane in LS onto a space curve, the isobar along the ship hull, in RS. The same mapping relation will transform the prescribed values of velocity components, u_0 , v_0 , and v_0 , (not velocity potential as in conformal mapping), along the straight line to corresponding values at points along the isobar. So

 $u(x, y, z) = u_0(x_0, 0, z_0)$ (4.4)

$$v(x,y,z) = v_0(x_0,0,z_0).$$
 (4.5)
 $w(x,y,z) = v_0(x_0,0,z_0).$ (4.6)

The wave elevations, $\zeta(x,y)$ and $\zeta^{0}(x_{o},y_{o})$, are defined on the undisturbed free surfaces, z=0 and $z_{o}=0$, in RS and LS respectively. So a mapping function for these two undisturbed free surfaces has only two components, $x = x(x_{o}, y_{o})$ and $y = y(x_{o}, y_{o})$. The wave elevation in RS can be written as

$$\zeta(\mathbf{x},\mathbf{y}) = \zeta[\mathbf{x}(\mathbf{x}_{0},\mathbf{y}_{0}),\mathbf{y}(\mathbf{x}_{0},\mathbf{y}_{0})] = \zeta^{0}(\mathbf{x}_{0},\mathbf{y}_{0}) \quad (4.7)$$

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(4.2) *

That means the wave elevation at the point (x,y) in RS is the same as that at the corresponding point (x_{α},y_{α}) in LS.

Similarly, the hull functions, f(x,z) and $f^{0}(x_{0},z_{0})$, are defined on the centerplanes, y=0 and $y_{0}=0$, in RS and LS respectively. The hull function in RS can be written as

 $f(x,z) = f[x(x_0,z_0), z(x_0,z_0)] = f^{O}(x_0,z_0)$ (4.8)

That means the breadth of the ship hull at point (x,z) in RS is the same as that at the corresponding point (x_0,z_0) in LS.

In fact, we can prove that this kind of transformation may make the solution in LS satisfy the exact kinematic boundary conditions, (1.1) and (1.2), in RS.

The exact and linearized kinematic boundary conditions on the free surface, (1.2) and (1.10), can be written as

 $\begin{bmatrix} 1 + \frac{u(x,y,\zeta(x,y))}{U} \end{bmatrix} \frac{\partial \zeta}{\partial x} + \frac{v(x,y,\zeta(x,y))}{U} \frac{\partial \zeta}{\partial y} = \frac{w(x,y,\zeta(x,y))}{U}$

(4.9)

 $\frac{\partial \zeta^{0}}{\partial x_{0}} = \frac{W_{0}(x_{0}, y_{0}, 0)}{U}$ (4.10)

Since the mapping function between the two undisturbed free surfaces is $x=x(x_{c_0},y_{c_0})$ and $y=y(x_{c_0},y_{c_0})$ and the wave elevations at the corresponding points, (x,y) and (x_{c_0},y_{c_0}) .

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are the same, equation (4.10) can be written as

$$\frac{\partial x}{\partial x_{o}} \frac{\partial \zeta}{\partial x} + \frac{\partial y}{\partial x_{o}} \frac{\partial \zeta}{\partial y} = \frac{w_{o}(x_{o}, y_{o}, 0)}{U}$$
(4.11)

Comparing (4.11) and (4.9), we may take

 $\begin{aligned} u(x,y,\tau(x,y)) &= u_{0}(x_{0},y_{0},0) \\ v(x,y,\tau(x,y)) &= v_{0}(x_{0},y_{0},0) \\ v(x,y,\tau(x,y)) &= v_{0}(x_{0},y_{0},0) \end{aligned} \tag{4.13}$

and equation (4.9) will become

$$\left[1 + \frac{u_{o}(x_{o}, y_{o}, 0)}{U}\right] \frac{\partial \chi}{\partial x} + \frac{v_{o}(x_{o}, y_{o}, 0)}{U} \frac{\partial \chi}{\partial y} \Rightarrow \frac{w_{o}(x_{o}, y_{o}, 0)}{U} (4.15)$$

Then the mapping function between the two undisturbed free surfaces may be written as

$$x = x_0 + \int_{-\infty}^{x_0} \frac{u_0(x_0, y_0, 0)}{U} dx_0$$

$$y = y_0 + f_{-\infty}^{x_0} - \frac{v_0(x_0, y_0, 0)}{U} dx_0$$
 (4.17)

(4.16)

If the transformation of the velocity components, (4.12) ' to (4.14), is considered the transformation in the z_0 -direction can be found from (4.10) as

 $z = z_{o} + f_{-\infty}^{o} - \frac{w_{o}(x_{o}, y_{o}, 0)}{U} dx_{o}, (z_{o} = 0)$ (4.18)

From (1.11), (4.12) and (4.18), the dynamic boundary condition on the free surface in RS satisfied by this transformation is

 $\zeta(\mathbf{x},\mathbf{y}) = -\frac{U}{g} \mathbf{u}(\mathbf{x},\mathbf{y},\zeta(\mathbf{x},\mathbf{y}))$ (4.19)

Although equation (4.19) is not the exact dynamic boundary condition (see (1.7)), it is a great improvement.

Similarly, in order to make the linearized solution satisfy the exact kinematic boundary condition on the hull surface in RS, the other set of transformations can be found as

$$x = x_{0} + \int_{-\infty}^{x_{0}} \frac{u_{0}(x_{0}, 0, z_{0})}{U^{n}} dx_{0}^{n}$$
(4.20)

(4.21)

$$y = y_{o} + \int_{-\infty}^{x_{o}} \frac{v_{o}(x_{o}, 0, z_{o})}{U} dx_{o}$$

$$\dot{z} = z_0 + \int_{-\infty}^{x_0} \frac{w_0(x_0, 0, z_0)}{U} dx_0$$
 (4.22)

and

$$\begin{aligned} u(x,f(x,z),z) &= u_0(x_0,0,z_0) \end{aligned} (4.23) \\ v(x,f(x,z),z) &= v_0(x_0,0,z_0) \end{aligned} (4.24) \\ w(x,f(x,z),z) &= w_0(x_0,0,z_0) \end{aligned} (4.25) \end{aligned}$$

Comparing (4.20) to (4.25) with (4.12) to (4.18), it can be shown that these two sets of transformation are consistent. They transformation for the whole flow field can be written as

 $x = x_{0} + \int_{-\infty}^{x_{0}} \frac{u_{0}(x_{0}, y_{0}, z_{0})}{U} dx_{0}$ (4.26)

$$y = y_{0}^{*} + \int_{-\infty}^{n_{0}} \frac{z_{0} \cdot w_{0}^{*} x_{0}^{*} x_{0}^{*}}{U} dx_{0} \qquad (4.27)$$

$$\begin{aligned} u(x,y,z) &= u_{0}(x_{0},y_{0},z_{0}) \end{aligned} \tag{4.29} \\ v(x,y,z) &= v_{0}(x_{0},y_{0},z_{0}) \end{aligned} \tag{4.30}$$

and

 $\zeta(\mathbf{x},\mathbf{y}) = \zeta^{0}(\mathbf{x}_{0},\mathbf{y}_{0})$ $f(\mathbf{x},\mathbf{z}) = f^{0}(\mathbf{x}_{0},\mathbf{z}_{0})$

= z₀ + / -

 $w(x,y,z) = w_0(x_0,y_0,z_0)$

(4.32)

(4.31)

Since only the ship hull in RS is known, the transformation . (4.26) to (4:33), can be interpreted as a kind of inverse streamline tracing method which forces the ship hull in RS to be A stream surface. But obviously, the velocity components cannot satisfy the continuity equation in RS. (refer to.conclusion) Now, we assume that only the points on the centerplane in LS are considered; that the streamlines can be replaced by the isobars along the ship hull (recall the draft-length ratio of the ship is small); that the longitudinal shift can be calculated from the P.P.; and that the longitudinal slope of the ship hull is small. Then the transformation, is found to be identical to that of Guilloton's method, (4:1) to (4+8).

In our problem, since the ship hull in RS and a specified Froude number are given, the "dimearized hull" cannot be found directly. However, from the formulas of Guilloton's method, the source strength $m(x_0, x_0)$ in LS can be expressed in terms of the slopes, $\frac{3}{\delta X}$ and $\frac{3}{\delta x}$ of the given "real hull"

$$\frac{\mathfrak{m}(\mathbf{x}_{o},\mathbf{z}_{o})}{2\mathfrak{U}} = \frac{1+\mathfrak{u}_{o}(\mathbf{x}_{o},\mathbf{0},\mathbf{z}_{o})/\mathfrak{U}}{1+\mathfrak{a}^{2}/2} \xrightarrow{\frac{\partial}{\partial \mathbf{x}}} - \frac{\mathfrak{U}^{2}}{g} \frac{\partial}{\partial \mathbf{x}_{o}} \left(\frac{\mathfrak{u}_{o}(\mathbf{x}_{o},\mathbf{0},\mathbf{z}_{o})}{\mathfrak{U}}\right) \frac{\partial f}{\partial \mathbf{z}}$$

(4:34)

Therefore, the "linearized hull" can be found by the following iterative process:

(1) Assume a trial value of the source strength for each source panel. The longitudinal local slope of the "real hull" corresponding to the centroid of each panel may be taken as the initial value of the quantity, m/2U, i.e. initially, the "linearized hull" is assumed to be the same as the diven "real hull".

(2) Calculate the u₀-component velocity (3.26) along each longitudinal straight line on the centerplane in LS.
 (3) 'Substitute the calculated u₀-component velocity into (4.1) and '(4.3) to find the profile ζ(x,y) of each isobar in RS corresponding to the straight line in LS.
 (4) Calculate the slopes; df/dx and df/dx of the "real hull" corresponding to the points on each isobar and substitute them into (4.34) to find the hew strength of each game'.
 (5) If the new strength of each source gamel is the same, as the trial value, the obscuration stops. Otherwise, the new strength of each game a the new strength of each game date is the same date that value and the calculation repeated.

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After the "linearized hull" is found, the flow quantities can be calculated by the thin ship theory and transformed to that in RS. The wave-marking resistance in RS actually should be calculated by integrating the pressure around the real hull as (1.6), but if we neglect the higher order term (as below), the wave-marking resistance of the "linearized hull" can be taken as that of the "real hull".

The transformation of the points on the centerplane in LS can be written as

x

$$A(x_0, z_0)$$
, $A(x_0, z_0) = \int_0^{x_0} \frac{u_0(x_0, 0, z_0)/U - \alpha^2/2}{1 + \alpha^2/2} dx_0$ (4.35)

 $z_{o} + C(x_{o}, z_{o})$, $\frac{1}{C}(x_{o}, z_{o}) = -\frac{U}{q} u_{o}(x_{o}, 0, z_{o})$ (4.36)-

and equation (4.23) to (4.25)

According to Bernoulli's equation, the pressure at the point

 $P(x, f(x, z), z) = -\rho[Uu(x, f(x, z), z) + \frac{1}{2}(u^2 + v^2 + w^2) + gz] \quad (4.37)$

Substituting the corresponding linearized quantities into RHS of (4.37).

 $P(x, f(x, z), z) = -\rho\{U | u_0(x_0, 0, z_0) + \frac{1}{2} (u_0^2 + v_0^2 + w_0^2) + g[z_0 + C(x_0, z_0)]\}$

(4.38)

Expanding the longitudinal slope of the "real hull", $f_{\chi}(x,z)$, with respect to the linearized quantities, we can obtain:

$$f_{x}(\vec{x},z) = f_{x_{o}}^{o}(x_{o},z_{o}) + (-f_{x_{o}}^{o}\lambda_{x_{o}} - f_{z_{o}}^{o}C_{x_{o}}) + \dots$$
 (4.39)

and

$$\begin{aligned} x_{\alpha}^{dz} &= |x_{\alpha}^{z} z_{\alpha}^{-x_{\alpha}} z_{\alpha}^{-x_{\alpha}} | \frac{dx_{\alpha}^{d} dz_{\alpha}}{dz_{\alpha}} \\ &= |1 + C_{\alpha}^{z} + x_{\alpha}^{z} + x_{\alpha}^{z} z_{\alpha}^{-z} - C_{\alpha}^{z} A_{\alpha}^{z} | \frac{dx_{\alpha}^{d} dz_{\alpha}}{dz_{\alpha}} \end{aligned}$$

$$(4.40)$$

Substituting (4.38), (4.39) and (4.40) into (1.6), the wavemaking resistance of the real hull can be written as

$$R = -2\rho U \iint_{O} u_{O}(x_{O}, 0, z_{O}) f_{X_{O}}^{O}(x_{O}, z_{O}) dx_{O} dz_{O}$$

 $= 2\rho \iint_{S_{o}} [U u_{o}(x_{o}, 0, z_{o}) + gC(x_{o}, z_{o})](C_{z_{o}}f_{x_{o}}^{o} - C_{x_{o}}f_{z_{o}}^{o})dx_{o}dz_{o} (4.41)$

The first term of (4.41) is the wave-making resistance, R_o, of the linearized hull (see (1.13)), and since $C(x_{o}, z_{o}) =$ $-\frac{U}{q}u_{o}(x_{o}, z_{o})$, we find the second term is zero. Then the difference in the wave-making resistance between the "linearized hull" and the "real hull" is of the fourth order, i.e.

 $R = -2\rho U \int \int u_o(x_o, 0, z_o) f_{x_o}^o(x_o, z_o) dx_o dz_o + O(\varepsilon^4)$ (4.42)

For certain nonlinear problems, we may find a transformation and then transform the linearized solution from the "linearized space" to the "real space". In this way, we may obtain a "better" solution. At least the solution satisfies the field equation and boundary conditions to the same order. But this is not the case for the threedimensional steady ship-flow problem. Therefore the solution obtained from Guilloton's method can only be justified by comparing the computed results with the experimental results.

2.5 Cubic spline curve fitting[11]

Ordinarily, the shape of the ship hull is defined by the hull offsets. In order to find the slopes, $\frac{3f}{3\chi}$ and $\frac{3f}{2g}$, of the ship hull, we should find the equations of the smooth ship lines i.e. waterlines and framelines, passing through the diven ship-offsets.

Let us consider a single-valued curve with continuous first and second derivatives passing through the given

. 35

points, say (x_1, y_1) , i=1,2,...N. This curve can be divided into (N-1) segments corresponding to the given (N-1) intervals. . It is assumed that the equation of each segment is a threedegree polynomial, for example: the equation of ith segment is:

 $f_{i}(x) = A_{i}(x-x_{i})^{3} + B_{i}(x-x_{i})^{2} + C_{i}(x-x_{i}) + D_{i}$ (5.1)

Hence, there are 4(N-1) unknowns, A_{1} , B_{1} , C_{1} and D_{1} = 1,2,... N-1. We can find 4(N-1) equations from the following conditions to solve for these 4(y-1) unknowns:

(a) The curve should pass through N given points (N equations) $f_i(x_i) = x_i$, i=1,2,...N-1 (5.2)

$$f_{N-1}(x'_N) = \bar{y}_N$$
 (5.3)

(b) The curve is continuous, (N-2 equations)

$$f_i(x_{i+1}) = f_{i+1}(x_{i+1})$$
 $i=1,2,...,N-2$ (5.4)

(c) The first derivative of the curve is continuous (N-2 equations)

$$f'_{i}(x_{i+1}) = f'_{i+1}(x_{i+1}) \quad i=1,2,...N-2$$
 (5.5)

 (d) The second derivative of the curve is continuous (N-2 equations)

$$f_{i}(x_{i+1}) = f_{i+1}(x_{i+1})$$
 i=1,2,...N-2

(c) Assume second derivatives of the ends are zero (2 equations)

 $f_{1}^{\prime}(x_{1}) = 0$

36

(5.6)

(5.7)

X

Solving this system of simultaneous equations is very tedious, after some manipulations, we can obtain the following formulas:

 $A_{i} = \frac{1}{6\Delta x_{i}} (y_{i+1} - y_{i}^{*})$ $B_i = \frac{1}{2} y_i^*$ (5.9) $C_{i} = \frac{\Delta y_{i}}{\Delta x_{i}} - \frac{1}{6} \Delta x_{i} (y_{i+1} + 2y_{i})$ Di Yi



37

(5.8)

$$\begin{split} & 6 \left(\Delta y_2 / \Delta x_2 - \Delta y_1 / \Delta x_1 \right) - \Delta \dot{x}_1 y_1^{-1} \\ & 6 \left(\Delta y_3 / \Delta x_3 - \Delta y_2 / \Delta x_2 \right) \\ & 6 \left(\Delta \dot{y}_4 / \Delta x_4 - \Delta \dot{y}_3 / \Delta x_3 \right) \\ & & \\$$

(5.10)

where

$$\begin{split} \Delta x_{i} &= x_{i+1} - x_{i} \quad , \quad \Delta y_{i} &= y_{i+1} - y_{i} \\ \vdots &\vdots &\vdots \\ y_{i}^{\prime} &= f_{i}^{\prime}(x_{i}) \quad , \quad y_{i+1}^{\prime} &= f_{i}^{\prime}(x_{i+1}) \end{split}$$

and $y_i = f_i(x_i)$

A special feature of equation (5.9) is that four coefficients of arbitrary segment i only depend on the two given points, (x_i, y_i) and (x_{i+1}, y_{i+1}) , and the two second derivatives, $y_i^{\prime\prime}$ and $y_{i+1}^{\prime\prime}$, at given points. Hence, once equation (5.10) has been solved, the whole curve can be specified and the slope at any point of the curve can easily be calculated.

CHAPTER 3

COMPUTATIONAL METHOD AND RESULTS

We would like efficient computation and accurate results not only for wave-making resistance but also for flow quantities around the "real hull". The major differences in the computational scheme used from that of others were firstly using the source strength as the convergence criterion for spline function for fitting the given ship-offsets. The computer programs were set up, taking into consideration the symmetric and antisymmetric properties of the element disturbance velocity components induced by the source panels. The whole computational scheme can be separated into two parts. One is to compute the disturbance velocity components, $u_0(x_0, 0, z_0)$, and $w_0(x_0, 0, z_0)$, induced by the source panels with "unit" strength, and the other is to find the source strength in LS as mentioned in section 2.4.

For the techniques used in computing the first part, we assume that the area of the centerplane of the "linearized hull" is the same as that of the "real hull". The centerplane is divided into 200 rectangular source panels (twenty-one stations including F.P. and A.P., and eleven waterlines including the base line and design waterline). The centroid of each panel is chosen as the control point (field point), so that there are 40,000 elemental disturbance velocities to be calculated, i.e. the elemental disturbance velocity of each source panel with respect to each control point. It is a very tedious work. But as mentioned before, we can take advantage of symmetric and antisymmetric properties and the Heaviside function in the formulas of the elemental disturbance velocity components to reduce the laborious work considerably. For example: there are four source panels, A,B,C, and D in longitudinal direction such as

1	2	3	4 ⁴
A	в	с	D

The corresponding control points are 1,2,3 and 4 respectively. There are 16 elemental disturbance velocities to be calculated. From (3.5), (3.7), (3.14) and (3.21), we know the elemental disturbance velocity of u-component includes two parts, one is the symmetric part, $u_g = u_1 + u_2$, and the other is the free wave part, $u_g = u_3$. So in this example, the 16 elemental disturbance velocities of u-components can be written as

 $u(I,J) = u_g(I,J) + u_f(I,J)$ I=A,B,C, and D, J=1,2,3 and 4

Since u_{g} is symmetric and the area of each source panel is the same, we have:

 $u_{g}(A,1) = u_{g}(B,2) = u_{g}(C,3) = u_{g}(D,4)$

 $u_{g}(A,2) = u_{g}(B,3) = u_{g}(C,4) = u_{g}(B,1) = u_{g}(C,2) = u_{g}(D,3)$

$$u_{s}(A,3) = u_{s}(B,4) = u_{s}(C,1) = u_{s}(D,2)$$

and $u_{e}(A, 4) = u_{e}(D, 1)$

Hence, only $u_{g}(\lambda,4)$, $u_{g}(B,4)$, $u_{g}(C,4)$ and $u_{g}(D,4)$ will be calculated. If the control point is in front of the source panel, the free wave part, u_{g} , has no contribution. We also have

$$u_{f}(B,1) = u_{f}(C,2) = u_{f}(D,3) = u_{f}(C,1) = u_{f}(D,2) = u_{f}(D,1) = 0$$

and similarly

$$u_{f}(A,1) = u_{f}(B,2) = u_{f}(C,3) = u_{f}(D,4)$$

$$u_{f}(A,2) = u_{f}(B,3) = u_{f}(C,4)$$

 $u_{f}(A,3) = u_{f}(B,4)$

Only $u_f(h, 4)$, $u_f(B, 4)$, $u_f(C, 4)$ and $u_f(D, 4)$ will be calculated. From (3.6), (3.8) and (3.20), $w_1 + w_2$ has the antisymmetric property, and the same technique can be used to calculate the elemental disturbance velocity of w-component. Thus only the elemental disturbance velocities of each panel with respect to the last control point have to be calculated. In the case of 200 panels with 200 control points, the number of calculations will be reduced from 40,000 to 2,000. In the second part of the computational scheme, we first find the second derivatives, $\frac{3^2}{3\chi^2}$ and $\frac{3^2}{3z^2}$, at each intersecting point of waterlines and stations, thus the coefficients of each segment function can be calculated. Then the y-coordinate and the first derivatives, $\frac{3\gamma}{3x}$ and $\frac{3\gamma}{3z}$, at any point on the ship hull can be obtained by interpolation. If the ship hull is smooth, we can generate the ship lines very accurately with this method. The number of iterations for finding the "linearized hull" depends on the value of the Froude number and the shape of the ship hull. To save computer time, we can use the "linearized hull" of a lower Froude number as the trial value for a higher Froude number. Generally, the number of, iterations is between 40 and 60 for the convergence criterion 1 x 10⁻⁴.

Two models have been selected for computation: Wigley model 3012, a mathematical hull form, and Series 60 block 60, a conventional merchant ship hull. The geometries of the models are given as follows:

(1) Wigley model 3012

 $B/L = 0.1, H/L = 0.0625, C_{\rm B} = 0.444, C_{\rm PR} = 0.667$ $C_{\rm X} = 0.667, C_{\rm B} = 0.661 \text{ and } L/L_{\rm PP} = 1.000 \text{ (where L=LWL)}$ The hull surface is defined by

 $y = \frac{B}{2} [1 - (\frac{2x}{L})^2] [1 - (\frac{z}{H})^2]$

(2) Series 60 block 60

$$\begin{split} B/L_{\rm PP} &= 0.1333, \quad B/L_{\rm PP} = 0.0533, \quad C_{\rm B} = 0.600; \quad C_{\rm PR} = 0.614 \\ &* \\ C_{\rm w} &= 0.977, \quad C_{\rm w} = 0.710 \quad \text{and} \quad L/L_{\rm PP} = 1.0167 \; (\text{where } L = LML) \end{split}$$

The ship-offsets are in table 1, the bow and "stern contours and lines are shown in Fig. 3 and Fig. 4.

The computed results of the wave-making resistance, wave profile, isobars and flow directions along the ship hull are shown in Fig. 5 to Fig. 21. The wave resistance and wave profile curves are plotted over the experimental curves from reference [12] for comparison.

Generally speaking, Guilloton's method gives very good results which are close to the experimental results for Frome number from 0.25 to 0.35 approximately. Especially, in the wave resistance curves, there are no large humps and bollows which usually exist in Nichell's resistance curve (see Fig. 5 and Fig. 12). Unfortunately, there are no experimental results to compare with the calculated isobars and flow directions, but from the tendency of the isobars and flow directions, it appears in the correct sense because at the free surface the streamline and isobar coincide, below the free surface, the streamline have a stronger tendency to go down near the bow and come up near the stern as in (13]. Comparing with merice 60 block 60, Wieley model 3012 has smaller "breadth"

and simpler geometrical shape, the variation of its isobars and flow directions are smaller, especially around the stern.

In the last two figures, Fig. 22 and Fig. 23, the calculated wave-making resistance of Wigley hull and Series 60 by Guilloton's method are compared with the results obtained by other researchers. The computational method developed in this thesis has demonstrated its effectiveness and the computed results are quite consistent with that of others, even showing some improvement! The deviations may be due to different numerical techniques for computation, such as the number of source puels, the method of curve fitting, the convergence criterion, etc.

CHAPTER 4

DISCUSSION AND CONCLUDING REMARKS

The main purpose of this thesis is to account for some nonlinear offects of steady ship-flow problem by Guilloton's transformation. Although there is no rigorously theoretical background for Guilloton's method, the computed results have shown that the prediction of the ship flow for a certain Froude number range is very good. In the range of Froudé numbers, roughly between 0.25 and 0.35, we may infer that just considering the flow in the vicinity of the ship hull, it could be more important to satisfy the hull and free . surface boundary conditions than the field equation. The nonlinear effects included in Guilloton's method are to reduce the oscillatory behaviour of the wave resistance curve based on the thin ship theory and to shift the phase of the wave elevation along the ship hull as that of other higher order theories. [14]. From the definition of the fluid domain in the steady ship-flow problem, Guilloton's method seems more reasonable than the thin ship theory, since the domain is defined below the "disturbed" free surface and out of the interior region of the ship. Another feature of Guilkoton's method is to correct the paradox of the thin ship theory which implies that the wave resistance is the same no matter which direction the ship moves, bow or stern ahead. But due to the results of the transformation, the wave-making resistances for these two cases, will be different.

and reliable methods to obtain reasonable results for the stage of preliminary design of conventional ships.

The reasons why the calculated results do not match the experimental results at high Froude number may be due to:

- (a) The sinkage and trim are not considered by Guilloton's method.
- (b) The isobars calculated by equation (4.3) are no longer correct.
- (c) The thin ship theory may not apply to the linearized hull
 Since the distortion of hull geometry is too excessive.
 (d) It can be erroneous for the linearized solution to satisfy

the field equation in RS.

For a ship with a flat bottom, such as Series 60 block 60, the bottom part of the hull can not be described by the hull equation, y = f(x, z), so that the calculated flow hear the bottom can not exactly correspond to the real flow, even though good results for wave-making/resistance are obtained. The calculated flow based on the thin ship theory or Guilloton's method may not be good enough to form the starting point of the, boundary layer calculation for ship hulls.

It appears that Guilloton's method for solving the steady ship-flow problem has many disadvantages. The difficulties of the flow problem'still can not totally be resolved. However, comparing with other sophisticated methods, for example: higher order thory, finite slemmin method and finite difference method, we may say that Guilloton's method is one of the simplest

REFERENCES

- Michell, J.H., "The wave resistance of a ship", Philos. Mag: (5) 45, 1898, pp. 106-123.
- Guilloton, R., "L'étude théorique du bateau en fluide parfait", Bull. Ass. Tech. Mar. Aeronaut. 64, 1964, pp. 538-561.
- Van Dyke, M., "Perturbation methods in fluid mechanics" Academic Press, New York, 1964.
- Noblesse, F., "A perturbation analysis of the wave-making resistance of a ship, with an interpretation of Guilloton's method", J. Ship Res. Vol. 19, 1975, pp. 140-148.
- Dagan, G., "A method of computing nonlinear wave resistance of thin ships by coordinate straining", J. Ship Res. Vol. 19, 1975, pp. 149-154.
- Wehausen, J.V., "The wave resistance of ships", Advances in Applied Mechanics, Academic Press, New York, Vol. 13, 1973.
- "Kellog, O.D., "Foundation of potential theory" Berlin; Springer, 1929.
- Havelock, T.H., "The theory of wave resistance", Proc. Roy. Soc. Ser., A.138, 1932, pp. 339-348, Coll. papers, pp. 377-389.
- 9. Eggers, K., Shama, S., Ward, L., "An assessment of some experimental methods for determining the wave-making characteristics of a ship form", Trans. Soc. Nav. Arch., Mar. Eng. 75, 1967, pp. 112-144.
- Gadd, G.E., "Wave resistance calculations by Guilloton's method", Tran. Royal Inst. Naval Arch. Vol. 115, 1973, pp. 377-384.
- Spath, H., "Spline algorithms for curves and surfaces", Translated by Haskins, W.D., and Sager, H.W., Utilitas Mathematica Publishing Inc., 1974.
- "Proceedings of the workshop on ship wave-resistance computation", Washington, D.C., 1979.
- Misra, S.C., "The calculation of potential flow on ship hulls" Royal Inst. Naval Arch., 1983 (issued for written discussion)."
- Hong, S.Y., "Numerical calculation of second-order wave resistance" J. Ship Res. Vol. 21, 1977, pp. 94-106.



x, y, z Translating coordinate system with x in the opposite direction to the ship's forward motion, z vertically upward, and the originat the intersection of the planes of the undisturbed free-surface and the midship section.⁴

x', y', z' Coordinate system fixed in ship and coinciding with the x-y-z system.

*Midship section is, by definition, at the midpoint between perpendiculars.

FIGURE 1

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. 1



TABLE 1 - TABLE OF OFFSETS

SERIES 60, $C_{B} = 0.60$ (FROM TODD, 1953)

Half breadths of waterline given as fraction of maximum beam on each waterline

Model = 4210W W.L. 1.00 is the designed load waterline Forebody prismatic coefficient = 0.581 Atterbody prismatic coefficient = 0.646 Total prismatic coefficient = 0.614

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				Wate							
Sta.	Tan.	0.075	0.25	0.50	0.75	1.00	1.25	1.50 /	1.00 W.L		
FP	0.000	0.000	0.000	10.000	0.000	0.000	0.020	0.042	0.000		
%	0.009	0.032	0.042	0.041	0.043	0.051	0.076	0.120	0.042		
1	0.013	0.064	0.082	0.087	0.090	0.102	0.133	0.198	0.085		
1,16	0.019	0.095	0.126	0.141	0.148	0.160	0.195	0.278	0.135		
2 -	0.024	0.127	0.17B	0.204	D.213	0.228	0.270	0.360	0.192		
3 /	0.055 -	0.196	0.294	0.346	0.368	0.391	0.440	0.531	0.323		
4	0.134	0.314	0.436	0.502	0.535	0.552	0.607	0.683	0.475		
5	0.275	0.466	0.589	0.660	0.691	0.718	0.754	0.804	0.630		
6	0.469	0.630	0.733	0.802	0.824	0.841	0.862	0.889	0.771		
7	0.666	0.779	0.854	0.906	0.917	0.926	0.935	0.946	0.880		
8	0.831	0.898	0.935	0.971	0.977	0.979	0.981	0.982	0.955		
9 .	0.945	0.964	0.979	0.996	1.000	1.000	1.000	1.000	0.990		
10	1.000	1.000	1.000	1.000 -	1.000	1.000	1.000	1.000	1.000		
11	0.965	0.982	0.990	1.000	1.000	1.000	1.000	1.000	Q.996		
12	0.882	0.922	0.958	0.994	1.000	1.000	1.000	1.000	0.977		
13	0.767	0.826	0.892	0.952	0.987	0.994	0.997	-1.000	0.938		
14	0.622	0.701	0.781	0.884	0.943	0.975	0.990	0.999	0.863		
15	0.453	0.550	0.639	0.754	0.857	0.937	0.977	0.994	0.750		
16 .	0.309	0.413	0.483	0.592	0.728	0.857	0.933	0.975	0.609		
17	0.168	0.257	0.330	0.413	0.541	0.725	0.844	0.924	0.445		
18	0.065	0.152	0.193	0.236	0.321	0.535	0.709	0.E34	0.268		
18%	0.032	0.102	0.130	0.156	0.216	0.425	0.626	0.769	0.187		
19 \	0.014	0.058	d.076	0.085	0.116	0.308	0.530	0.686	0.109		
19%	0.010	0.020	0.020	0.022	0.033	0.193	0.418	0.579	0.040.		
AP	0.000	0.000	0.000	0.000	0.000	0.082	0.270	0.420	0.004		
Max half	0.710	0.866	0.985	. 1.000	1.000	1.000	1.000	1.000	,		

*As fraction of maximum load waterline beam.

51 '



FIGURE 3 -- Bow and Stern Contours (from Todd, 1963)





BODY 075

53

1.50 W.L.

1.25 W.L 1.W 00. L W GR

0.75 W.L

1.075 W.L

0.25 W.L

WIGLEY HULL - RESISTANCE COEFFICIENT



south the second lower that standard interview

WAVE PROFILE. FOR FN=0.266 I MIGLEY HULL



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- GUTLLOTON NETHOD





FIGURE 7

WIGLEY HULL - ISOBARS FOR FN=0.266

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AP B BB					1	T	T		1	I
8 48	T	1	1	1	1	1	1	1	Ī	T
a 7a	t	1	1	1	1	1	1	+	T	T
a fa	T	-	1	1	1	T	-	-	1	
8 50			-	1	1	-	1	1		
. 40	1		and a	1	1	1	1			
05.0	-									
8 28	1	+		-	1		1			
8 19	t	+	1	1	t	1	1	1	1	-
8										

88.6 -0.20 -0.30 -0.40 -0.50 -0.60 -0.78 -0.60 -0.30

	-	_	_	-	-	-	_	_	-	-
0	1	t	1	1	t	t	t	t	t	t
-0.10	t	t	1		1	1	t	t	i	i
-0.20	1	1	1		1	1	1	t	1	t
-0.30							1		-	
4		1								
9		1		r	i	t	1	t	t	
-0.50		-			+	t	t	+	+	
-9.69	_					1				
78	1	1	1	1	1	1	ł	t	t	
01	1	t	1	t	t	t	t	t	t	l
-0.60	t	t	+					-	+	,
-0,90	-								1	
8.						P		1	1	1

WIGLEY HULL - FLOW DIRECTIONS FOR FN=0.266

i









FLOW DIRECTIONS FOR FN=0:348 HULL WIGLEY



8

8.30

3.20

0.10

AP

96.9


SERIES 60 BLOCK 60 - WAVE PROFILE FOR FN=0.220





SERIES 60 BLOCK 60 - FLOW DIRECTIONS FOR FN=0.220



- WAVE PROFILE FOR FN=0.280 SERIES 60 BLOCK 60



K THIN SHIP THEORY



FIGURE





FIGURE 17



- FLOW DIRECTIONS FOR FN=0.280 SERIES 60 BLOCK 60 WAVE PROFILE FOR FN=0.350 1 SERIES 60 BLOCK 60

EXPERIMENTAL RESULT

THEN SHEP THEORY

BUTLLOTON NETHOD





ISOBARS FOR FN=0.350 . SERIES 60 BLOCK 60 -

ł

70 AP 1.80 g SERIES 60 BLOCK 60 - FLOW DIRECTIONS FOR FN=0.350 0, 30 -0.20 9.60 0.30 8.78 * 11-+++++ 0.60 ******** -0.50 0.50 FIGURE WAVE PROFILE 01 · 10 0.60 0.70 0.30 -0.60 90.90 8.0





APPENDIX : COMPUTER PROCHAM

TITLE OF THE THESIS : ANALYSIS OF SHIP FLOW IN AN IDEAL FLUID USING GUILLOTON'S HETHOD AND SPLINE FUNCTIONS FUNCTION: THIS PROBRAM COMPUTES THE WAVE RESISTANCE COEFF. AND VAVE PROFILES FROM THE RIVEN SHIP-OFFSETS AND THE FROM NUMBERS BY THEN SHEP THEORY AND BUTLLOTON'S METHOD. WAVE RESISTANCE COEFFICIENT IS CH-RV/(8.5+RHO+U+VS) NONDIMENSIONAL WAVE ELEVATION IS ETA=Zu/(U/(2+8)) DINENSION ETA (28), ETA 1 (28), FIL 1 (4), SH (28, 18), SH 1 (28, 18) OOMHON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), Z((18) 1.XKD. WS.XS. XE CONMON /8A/ NFN, FN(28) CONHON /SC/ DFY(22,28), XA(22), ZA(28), YX2(22,28), YZ2(22,28) CONHON /SD/ SHIP(28), XLL, B, TD, VSI CONHON /S/ S(20, 10), S1 (20, 10), S2(20, 10), UI(20, 10) NX-21 NX1=NX-1 NZ=11 NZI-NZ-1 1-2.0 TYPE ., 'ENTER OUTPUT DATAFILE NAME' ACCEPT . 1. FIL1 . FORMAT CAA4) CALL ASSIGN(2, FILI) CALL INPUT CALL POINT TYPE +, 'POINT, FINISHED' OUTPUT : SHIP, SHICI, J) WRITE (2, 108) SHIP FORMAT CIX, 28A4D WRITE(2.m) / · WRITE(2,+) 'L-',XLL,' T-',TD,' WRITE(2,+) WRITE (2, +) ' SOURCE STRENGTH BY THIN SHIP THEORY! RITE(2, H) / 00 5 1=1,101 WRITE(2,+) (SH(1, J), J=1,18) CONTINUE NPH-1 FNC13-0.228 DO 18 I-1,NFN XK8-1./(2. 00 20 11-1, NXI DO 28 JU-1, NZI SCII, JUD-SHCII, JUD SICIT, JUS-SHCIT, JUS S2(II, JJ)-SMCII.JJ) CONTINUE CALL FULTONCENIS CALL HICHCSH, CW) -ALL WAVECSH, SHI, ETA, ETAI

OUTPUT FR, SHI, CW, CWI, ETA, ETAI ETTE(2, 48) WRITE(2, +) 'SOURCE STRENGTH BY BUILLOTON HETHOD. FOR FIN-', FR WRITE(2, +) ' DO 30 11-1, NX1 WRITE(2, +) (SHICIT, JUD, JU-1, NZ1) CONTINUE WRITE(2, 1) WRITE(2, +) 'FR-', FR. 1 CH-', CV. ' CWI-', CWI WRITE(2, H) " WRITE(2, W) 'CW : WAVE RESISTANCE COEFF. BY THIN SHIP THEORY' WRITE(2, W) 'CWI : WAVE RESISTANCE COEFF. BY GUILLOTON HETHOD' WRITE(2.48) FORMATCINIO WRITE(2, +) 'WAVE PROFILE FOR FN-',FR WRITE(2, #) ' ' DO 58 J-1, NX1 WRETE(2, +) "X/L=", XC(J)," ETA=", ETA(J)," ETA1-", ETA1(J). CONTINUE WRITE(2, +) ' ' WRITE(2, *) 'ETA . WAVE PROFILE BY THIN SHIP THOERY' WRITE(2, +) 'ETAI : WAVE PROFILE BY BUILLOTON METHOD' CONTINUE 1000 STOP END SUBRICUTINE POINT COMMON /A/ NX. NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1.XX8, WS, XS, XE SX=XL/CNX-13 ST=T/(NT-1) DO 18 I-1,NX X(I)=-1.+5X#(I-1) IFCI.ED.NOO GO TO 18 XCCID=-1+8X+CI-8.53 CONTINUE DO 28 1-1,NZ Z(ID--T+SZHCI-1) IFCI.ED.NZ3 00 TO 20 ZCCI)-T+8Z+CI-8.5) CONTINUE RETURN END SUBROLITINE DIPUT FUNCTION: THIS SUBROUTINE READS INPUT DATA FROM INPUT DATAFILE AND NORMALIZES THE SHIP-OFFICES. THE NONDIMENSIONL LOP IS 2. DIHENRITON FILE(4) CONHON /A/ NO, NO1, HX2, HZ, HZ1, HZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1, XX8, N8, X8, XE CONHON /84/ NPN, FH(28) CONHON /84/ NPT, FH(28) CONHON /84/ NPT, OFF(28), OF7(28, 28), OF(28, 28), NOF(25) CONHON /84/ NPT, OFFRET DATA/12, B, TD, NB1 ACCEPT 1, FILE FORMATC4443 CALL ADDING, FILED CADCI, 2003 BHEF

18

c

c

C C

EAD(1, +) NEN READ(1, H) (FNCI), I-1, NFN)* READ(1, H) XLL, B, TD, WS1 SCALE-XLL/2. WS-WSI/(SCALENSCALE) T-TD+2./XLL READ(1, #) NST DO 18 I-1, NST READ(1, +> OFXCI), NOFCI NI-NOFCID DO 28 J-1,11 READ(1,+) OFZCI,JD, OFYCI,JD OFZCI, J>=COFZCI, J>-TD>=2./XLL OFYCI, J>-OFYCI, J>=2./XLL CONTINUE CONTINUE CALL CLOSE(1) RETURN END SUBROUTINE CURFITCEND DEMENSION SH(28, 18) DEMENSION FILE(4), XX(26), YY(25), Y2(26) DEMENSION YXX(25), YX(22, 28), OFY(26, 28) CONHON_/A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1,XKB, CONHON NST, 0X(25), 0Z(25, 28), 0Y(25, 28), N(25), C(25) COHHON J OFYY(22,28), XA(22), ZA(28), YX2(22,28), YZ2(22,28) NC2=NX+1 NZ2-NZ+0 NOCK-NOCZ NZZ=NZ2 XL1=XL TIT CALL PNTOLI, TI, NOC, NZZO DO 38 I-1,NST NI-NCID DO 48 J-1,NI XXCJD-OZCI, JD YYCJD-OYCI, JD CONTINUE CALL CUBICIONI, XX, YY, Y2) ID-1 CALL INTRPCED, NZ2, ZA, NI, XX, YY, Y2, YXX DO 59 J-1,NZ2 OFYCI, J>-YXXCJ) CONTINUE CONTINUE DO 68 J=1, NZ2 DO 78 I=1, NST YYCIJ=0FYCI, JJ CONTINUE CALL CUBICI (NST. OX, YY, Y2) ID-1 CALL INTRP CID, NOC2, XA, NST, OX, YY, Y2, YXXX DO 89 1-1, 102 OFYYCI, J)=YXXCI) CONTINUE CONTINUE DO 100 J-1, NZ2 DO 100 J-1, NZ2 CUD-XACUD CUTO-OFYYCU

188 CONTINUE CALL CUBICI (NOC2, XX, YY, Y2) -ID-2 CALL INTRPEID, NX2, XX, NX2, XX, YY, Y2, YXX DO 118 J=1,102 YXCJ, I)-YXCU) 118 CONTINUE CONTINUE II-8 DO 128 1-1, NO2 IFCI.EQ. 13 60 TO 128 IF(I.E0.NX2) 60 TO 128 II-II+1 JJ-8 DO 158 J-1, NZ2 IFCJ. BE. 1. AND. J.LE. 63 60 TO 13 IFCJ.EQ.73 80 TO 138 IF(J. 9E. NZ2-3) 60 TO 198 JU-JU+1 SHCII, JUD-2. WYXCI, J) CONTINUE 139 128 CONTINUE DO 148 J=1, NZ2 DO 158 I=1, NC2 XXCTD-XACTD YYCID-OFYYCE, JD 159 CONTINUE CALL CUBICI (NOC2, XX, YY, Y2) 00 100 I-1, NC2 YX2(I, J)=Y2(I) 1.6 CONTINUE CONTINUE 140 DO 178 1-1, NC2 DO 1880-1, NZ2 XX(J)-ZA(J) YYCUD-OFYYCI, JD 188 CONTINUE CALL CUBICI (NZ2, XX, YY, Y2) DO 198 J-1, NZ2 YZZCI, JD=YZCJD 198 CONTINUE 178 CONTINE RETURN END SUBROUTINE INTRPCID, N2, ZA, NI, XX, YY, Y2, OUTO DIMENSION ZA(N2), XX(NI), YY(NI), Y2(NI), OUT(N2) DIMENSION H(26), HY(26), A(26), B(26), C(26), D(26) DO 60 11-1,N1-1 HCIID-00XCII+1D-XXCIID HYCIIS-YYCII+IS-YYCIIS CONTINUE DO 78 II=1,NI-1 A(II)=(Y2(II+1)-Y2(II))/(8.#H(II)) 'B(II)=8.5#Y2(II) C(II)-HY(II)/H(II)-H(II)=(Y2(II+1)+2.=Y2(II)) DUID-YYCIID CONTINUE DO 18 1-1,N2 ZZ-ZACI) DO 20 J=1,NI-1 IFCZZ. OF .XXCJD. AND . ZZ ILE .XXCJ+133 8 CONTINUE

37 DEL #77-XXC.ID IFCID.EQ. 1) OUTCID=CCCACUD#DEL3+BCUDD#DEL+CCUDD#DEL+DCUD IF CID.EQ.23 DUTCID=CC3. #ACJD3#DEL+2.#BCJD3#DEL+CCJD CONTINUE 18 RETURN END SUBROUTINE PHTCKL, T, NO2, NZ2) COMMON /SC/ OFYYC22, 28), X(22), Z(28), YX2(22, 28), YZ2(22, 28) SX=XL/CN0(2-2) SZ-T/(NZ2-18) DO 18 1-1, NX2 J-I-I IFCI.EQ. ID XCID-1.8 IFCI.EQ.NX2) XCID-1.8 IFCI.NE. 1. AND. I.NE. NO23 XCI3-1.+8X+(J-8.53 CONTINUE ZCID-T ZC22-ZCID+5Z/16. 2(3)-2(2)+82/18. 2(4)-2(8)+67/8. 2(5)-2(4)+82/8. Z(6)-Z(5)+SZ/8. 2(7)=2(6)+82/2. 2(8)=2(7)+62/2. DO 28 1-0,NZ2 2(1)=2(1-1)+82 CONTINUE RETURN END SUBROUTINE BULTONCONS FUNCTION: THIS SUBROUTINE COMPUTES NEW SOURCE STRENGTH BY BULLOTON'S HETHOD. DIHENSION FILE(4), SHI C28, 18) CONNON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1, XX8, WS, XS, XE COHMON /C/ UTC28, 18, 18), UL (28, 18, 18) COHMON /C/ UTC28, 18), 81(28, 18), 82(28, 18), UL (28, 18) COHMON /8/ S(28, 18), 81(28, 18), 82(28, 18), UL (28, 18) COHMON /S/ OFY(22, 28), XA(22), ZA(28), YZ2(22, 28), YZ2(22, 28) X8-1.0 XE-1.8 CALL INDUR ' ID=1 TYPE +, 'ITERATION'7ED CALL CHANG IR-0 CALL TRANCIR, ID) IFCIR.NE. 13 80 TO 38 IFCID.ED. 1883 80 TO 38 TD-ID+1 90 TO 29 DO 48 I-1,NX1 8 DO 49 J-1, NZ1 SHICT, J)-61CT, J) CONTINUE RETURN SUBROUTINE CHUNG DINENSION UC28, 183 CONNIN /A/ HOL, HOL, HOLE, HE, HE XC213. ZC113, XCC283, ZCC183

CONHON /C/ UT (28, 18, 180, UL (28, 18, 180 CONHON /S/ 8(28, 18), 51 (28, 18), 52 (28, 18), UI (28, 18) DO 28 J=1,NZ1 DO 28 J=1,NX1 UTCJ. TD-8.8 HO-CT-IDHK(I+J DO 38 II-1, NO 181-101-1+11 HAIN-II DO 58 JU-1, HZ1 NOI=CUL-IDHNYI+II IFCII.LE.JD UCII, JD-UTCISI, JJ, ID IFCII.8T.JD UCII.JUD-ULCIS2.JU, ID CONTINE DO 48 11-1, KK1 DO 48 JU-1, KK1 ULL, IDIG, IDHUCI, LOBICIT, JO . CONTINUE CONTINUE RETURN END SUBROUTINE TRANCER, ID) SUBROUTHE TRANSLIK, JUS / W(21), ZH(21), UP (28), TH(28), TX(28), DITENSUON Y(2(28), VH(28), YH(21), ZH(21), UP (28), TH(28), TX(28), DITENSUON YZI (28), VH(28, 18), ZH(28, 18), ZH(28, 18) COMMON YA/ NK, NKI, NG2, NZ, NZ1, NZ2, NZ, T, X(21), Z(11), XT(28), ZC(18) 1, X000, 148, X8, XE CONTON /8/ 8(28, 18), \$1 (28, 18), \$2(28, 18), UT(28, 18) FICAL, CID=CI.+AID/SORTCI+CI=CID DWX-0.8 DO 18 3-1-NZ1 DO 28 J-1, NO AI-UICJ, ID CI-BIGJ.D/2. THEUD TICAL, CID YGD-THGD CONTINUE TDX-1 CALL XHCAL CEDX. Y. XHO DO 38 J=1, NKI XHCJD-ODICJD-I CONCI. ID-IONCID CONTINE DO 48 J=1,NKI YGUD-81GJ, 10/2 2HGD-2CCD-U ZHIG, IS THIG CONTINUE CALL XHCALCIDX, Y, YHO CALL PARTLEYXI, YZI, XH, ZHO DO 50 J=1,NXI YCJ-UICJ,ID CONTINUE IDX-0 CALL XHCALCIDX, Y, UP) 00 60 J-1, NKI YCJD-2, HCTHCJDH SIG. D-YGD CONTINUE 78 J-1, NKI YGD-82(J, I) -----

CX-ABS(62(J, 1)/61(J, 1)-1.) IFCCX.ST. ENAX) ENAX-CX IFCCX.OT. I.E-40 IR=1 \$2(J, I)-61(J, I) CONTINUE CONTINUE TYPE . 'ERRHAX-', ENX IFCIR.EQ. 1) 60 TO 188 WRITE(2,+) ' ' WRITE(2, +) 'ISOBARS' WRITE(2,+) DO 119 1-1,NZI WRITEC2, #) " WRITEG2, #) 'No. ',I WRITEC2, +) " WRITECZ, N) "X-COOR." WRITECZ, #) CONH(J,I), J=1, NO(1) WRITEC2, N) ' ' WRITEC2, +) 'Z-COOR.' WRITEC2. +) #ZHHGJ.ID. J=1. NKID CONTINUE RETURN . END SUBROUTINE PARTL CYXI, YZI, XH, ZHO DIMENSION YX1(280, YZ1(280, YT(220, YT(220, YT2(220) CONNON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, 2, T, X(21), Z(11), XC(28), Z((18) 1,XX8,WS,XS,XE CONNON /8C/ OFY(22,28),XX(22), ZZ(28), YX2(22,28), YZ2(22,28) DO 38 1-1, NO.1. XI-XHOD) ZI-ZHCI) DO 49 J-1,102-1 IFOU. . . XXCJ) AND . XI.LE . XXCJ+133 BO TO 5 CONTINUE TYPE ",'OLT OF RANGE XX=',XI IFCXI.GT.XX(NX2) J=NX2-1 IFCXI.GT.XX(NX2) J=NX2-1 IFCXI.GT.XX(NX2) DELX=XX(NX2)-XX(NX2-1) IFOG.LT.XXCI33 J=1 FOG.LT.XXCIDD DELX YZICID-1.E-19 90 TO 125 DELX-DE-XXCD 181-J HI-OXCIEID-XXCIBID DO J=1,HZ2 WY2-OFYCIEL, JD YI-OFYCESI JD Y22-YX2CIEL, J Y12-102CTS1, J HY-Y2-Y A-(122-112)/CB. HII) 5-0.5=Y12 * CHY/HI-HI+(Y22+2.+Y12)/6. TCJD=CCCAMDELX3+B3HDELX+C3HDELX+C INC CUBICI CHEZE, ZZ, YT, YT2) 180 4-1,1002-1 CONTINUE

IF(ZI.8T.ZZ(NZ2)) JH022-1 IF (ZI. ST. ZZ(NZ2)) DELZ-7Z(NZ2)-7Z(NZ2-1) JFCZE.LT.ZZCIDO YZICID=I.E-18 IFCZI.LT.ZZCIDO GO TO 125 DELZ-21-22(J) ISA IE-MI H-ZZCIE-ZZCIS) HY-YTOD-YTOS A=CYT2CIED-YT2CI8DD/C6.HU 0.5HYT2CIS) 0+11/1+ 1= (YT2(IE)+2.=YT2(I8))/8 Devit (TR) YZICID-((S. MADHDELZ+2. HD)HDELZ+C DO 148 JH1, NZ2-1 IF CZI. BE. ZZ(J). AND. ZI. LE. ZZ(J+13) 80 TO 158 CONTINUE IF(ZI. ST. 72()(22)) JH(22-1 IF(ZI.81.72(422)) DEL2=72(422)-72(422-1) IF(ZI.LT.ZZ(1)) YXICID-1.E-18 IF(ZI.LT.ZZ(1)) 80 TO 38 DELZ-ZI-ZZCJD I81-J IEI-J+1. HI-72(1E1)-72(181) DO 108 JH1, 102 Y2-0FY(J, 1E1) Y1-0FY(J, 151) Y22=Y22(J, IEI) Y21=YZ2CJ. 1613 HY-Y2-Y1 A=CY22-Y123/(6.mH13 -8.5-Y12 DHY/HI-HI#(Y22+2.#Y12). D-YI YTCJD=CCCAMDELZD+BDHDELZ+CDHDELZ+D CONTINUE CALL CUBICI (NO2. XX. YT. YT2) DO 288 J-1, NO2-1 IFOT.9E.XX(J).AND.XI.LE.XX(J+13) 80 TO 218 CONTINUE TYPE +, 'OUT OF RANGE XX+', XI IF COL. 81. XXC00233 DELX-00000023-XXC002-13 IFOULLT.XXX(I)) JH IFOULLT. XX(13) DELX-YXICD-1.E-18 90 TO 58 90 TO 211 COXC-TO-XLED IS-J IE-J+I HY-YTCED-YTCES) CYT2CIED-YT2CIED)/C8.HE .5+YT2(18) +1//+++(YT2(12)+2,+YT2(18))/8. CSEDTY-Q YXI CID=CCB. HADHDELX+2. HBD CONTINUE

125

118

128

144

158 228

SUBROUTIDNE XHCALCIDX, Y, XH) DIMENSION H(280, HY(28), Y(280, Y2(28), XH(21) COMMON /A, NX, NI, NZ, NZ, NZ, NZ, NZ, XL, T, X1(21), Zi(11), X(28), Z(18) 1, XK8, WS, XS, XE С TYPE . 'X' ř TYPE .X NH-NIAI DO 18 1-1,NN II=I+I HCID-XCIID-XCID HYCID=YCID-YCD CONTINUE CALL CUBICI (NI, X, Y, Y2) \$1=HY(1)/H(1)-H(1)+(Y2(2)+2.+Y2(1))/8. DH=XC12-XS IFCIDX.NE.8) XHCID=S1+DH1/2.+CYCID-S1+XCIDD+DH DO 28 1-2,NI II-I-I A=(Y2(11+1)-Y2(11))/(8.+H(11)) 8-8.5+Y2(I1) C+HY(I1)/H(I1)-H(I1)+(Y2(I1+1)+2.+Y2(I1))/8. D-YCII) HIHCID IFCIDX.EQ.8> XHCI1>=C IFCIDX.NE.8) XN(I)=XN(I)+CCCCA/4.)+HI+B/3.)+HI+C/2.)+HI 1+0)#HI CONTINUE 28 DH-XE-XCN1) S2=((3.=A)=DH+2.=B)=DH+C IFCIDX.EQ.8) XHCN12-82 DH1=XE+XE-XCN1 D+XCN12 IFCIDX.NE.0) XHCN1+1)=XHCN1>+82+DH1/2.+CYCN1>-S2+XCN1>>+DH RETURN END SUBROUTINE INDUZ COMMON /A/ NX, NX1, N(2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1.XK8.WS.XS.XE CONNON /C/ UT(28, 18, 18), UL(28, 18, 18) COMMON /D/ VIC28, 18), V2(28, 18), V3(28, 18) Y-8.8 XX=XCONX13 DO 28 L-1,NZ1 ZZ-ZOCL) CALL SUI COX, Y, ZZ) CALL SUZCXX, Y, ZZ) CALL SUSCOX, Y, ZZ) DO 38 JU-1,NZ1 DO 38 II-1, NXI ULCII, JJ, L)=VICII, JJ)+V2CII, JJ) UTCII, JJ, L)=ULCII, JJ,L)+V2CII, JJ) CONTINUE CONTINUE RETURN END SUBROUTINE HICH(85, CW) č FUNCTION: THIS SUBROUTINE CALCULATES THE WAVE RESISTANCE COEF BY NICHELL INTERAL. DIMENSION \$5(28,18) COMMON /A/ NX,NX1,NX2,NZ,NZ1,NZ2,XL,T,X(21),Z(11),XC(28),Z((18)

1, XKB, WS, XS, XE COMMON /SH/ SH(28, 18) EXTERNAL RT DO 1 I-1, NXI DO 1 J-1.NZ1 SHCI, J)-SSCI, J) CONTINUE ST-0.8 EN-89.995=3.1418/188. CALL SINPSN(ST, EN, RT, VAL) CC=2./(WS+3.1416+XKB+XK8) CV-VAL+CC RETURN END FUNCTION RECTHETAD DIMENSION XH(28), YH(28), ZH(18), TEMP(28) COMMON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1, XK8, WS, XS, XE COMMON /SH/ SH(20, 10) F1=COS(THETA) B-XK8/F1 A-B/FI ZN=Z(NZ)=A D-EXP(ZN) DO 18 1-1,NZL K=NZ1+1-I T-A+ZCK) DI-EXPCTO ZHCK)-D-D1 D=D1 CONTINUE XN=X(NX)=B D-SINCXN) E=COSCXND DO 28 1-1, NXI K=NX1+1-3 T-B+XCKX DI-SINCTO EI-COS(T) XHCK3-D-DI YHCK3-E-EI D-DI E-EI CONTINUE DO 30 2-1,NX1 TEMP(I)-8.8 DO 48 J-1,NZ1 TEMPCID-TEMPCID+SHCI, JD+ZHCJD CONTINUE CONTINUE PS-8.8 8.8 DO 68 I-I, NXI PS-PS+TEMPCID+XHCID 09-08+TEHPCID=YHCID CONTINUE RT=(PS=PS+QS=QS)=F1=F1=F RETURN END SUBROUTINE WAVECON, SHI, ETA, ETAI) DIMENSION, UC20, 180, ETAC280, SHC28, 180, ETAI (280, SHI (28, 18) CONHON /A/ NO. NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(1), XC(20), Z((

1, XK8, WS, XS, XE COMMON /D/ V1(28, 18), V2(28, 18), V3(28, 18) XX=XC(NX1) YY-8.8 ZZ-0.8 CALL SUI CXX, YY, ZZ) CALL SUZCXX, YY, ZZ) CALL SUSCXX, YY, ZZ) DO 18 1-1, NX1 DO 18 J-1,NZ1 VICI, JD=VICI, JD+V2CI, JD VSCI, JD-VICI, JD+VSCI, JD CONTINUE DO 28 J-1, NX1 ETACU>=8.8 00 38 II-1,NX1 ISI-NX1-J+II IS2-NX1+J-II DO 38 JU-1, NZI IF(II.LE.J) U(II,JJ)=V3(IS1,JJ) IF(II.BT.J) U(II,JJ)=-V1(IS2,JJ) CONTINUE 00 40 II-1.NXI DO 40 JU-1,NZI ETACJJ-ETACJJ+UCII,JJJNSH(II,JJ) CONTINUE CONTINUE DO 58 I=1,NXI ETACID-2. HETACID CONTINUE DO 129 J-1, NX1 ETAI CUD#8.8 DO 138 II-1, NX1 IS1-WX1-J+II IS2-NX1+J-II DO 198 JU-1, NZ1 IF(II.LE.J) U(II,JD=VS(ISI,JJ) IF(II.8T.J) U(II,JD=VI(IS2,JJ) 132 CONTINUE DO 140 II-1, NX1 DO 148 JU-1,NZI ETA1 (J)-ETA1 (J)+U(II, JJ)*SHI (II, JJ) CONTINUE 140 CONTINUE 128 DO 158 I-1.NX1 ETAICID=2. HETAICID 158 . . CONTINUE RETURN END SUBROUTINE SUICXX, Y, ZZ) CONHON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), Z(18 1,XK0, WS, XS, XE CONNON /D/ VIC28, 18), V2(28, 18), V3(28, 18) CONNON /F/ F(21, 11) DOUBLE PRECISION F1, F DO 18 J-1.NZ ZI-ZCJ) DO IS I-LINX XI=XCID CALL COEFICXX, Y, ZZ, XI, ZI, XK8, FI) FCI.JOFT CONTINUE

CC=1./(4.+3.1410) DO 38 J-1,NZ1 JI=J+1 DO 38 1-1.NXI I1=I+1 P F(I1, J1)+F(I, J)-F(I, J1)-F(I1, J) VICI, JD-PHCC CONTINUE RETURN END SUBROUTINE COEFICXX, Y, ZZ, XI, ZI, XK8, F1) DOUBLE PRECISION RI, R2, F1, D1, D2, XY, YZ DOUBLE PRECISION DX1.C1.C2 DX1=X1-XX C1=Z1-ZZ C2=Z1+ZZ IFCC1.EQ.8.8) C1-1.E-4 IF(C2.E0.8.8) C2-1.E-4 XY=DXI=DXI+Y=Y RI-SORT CXY+CI+CI) R2=SORT CXY+C2+C2) / IFCXY: LE. 1.E-18) F1-0L08(ABS(C2)/ABS(C1)) DI-CI+RI D2=C2+R2 . IFCXY.GT.1.E-18) FI-DLOG(D1/D2) RETURN END SUBROUTINE SUZCXX, Y, ZZD CONHON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1, XKB, WS, XS, XE COMMON /D/ V1 (28, 18), V2(28, 18), V3(28, 18) COMMON /F/ F(21, 11) DO 18 J-1.NZ ZI=ZCJ) DO 18 1-1,NX TYPE #, 'SU2 1.1.1 I.',I XI-X(I) CALL COEFCXX, Y, ZZ, X1, Z1, XK8, F FCI, JD-FI CONTINUE CC=-1./(4.#9.1416#9.1416) DO 38 J-1.NZ1 J1=J+1 DO 38 1-1, NX1 II-I+I 0=F(I1,J1)+F(I,J)-F(I,J1)-F(I1,J) V2(I,J)-0+CC CONTINUE RETURN END SUBROUTINE COEFOX, Y, ZZ, XI, ZI, XK8, FI) DIMENSION SF1(3), SF2(3) COMMON /A1/ Y1, XK, DX1, C1 YI-Y XK-XKB DX1=XX-X1 CI=ZZ+ZI Y1-Y XXXXXXXX ST-8.8

DI=CEN-STO/NI DO 18 J-1,5 SFICUD-8.8 CONTINUE DO 28 1-1, NI+1 THETA-ST+DI#CI-I) CALL CONCTHETA, F) II-I/2#2 IFCI.EQ.I.OR.I.EQ.NI+ID IC-I IFCIT.NE.I.AND.I.NE.1.AND.I.NE.NI+1) IC=3 SFICIC2-6FICIC2-F CONTINUE FSUH1=(SF1(1)+4,#SF1(2)+2.#SF1(3))#D1/3. FSUH2-FSUN1 ICC=1 IFCICC.EQ.13 GO TO 118 K=1 K-K+1 SF2(1)-SF1(1) SF2(3)-SF1(2)+SF1(3) N2-N1 02-01/2. SF2(2)-8.8 DO 78 I-1,N2 THETA=ST+D2+C2+I-1) CALL CONCTHETA, F) SF2(2)=SF2(2)+F CONTINUE FSUM2=(SF2(1)+4.#SF2(2)+2.#SF2(3))#D2/3. IF(FSUH1.E0.8.0) CXF-0.0 IF(FSUH1.NE.8.0) CXF=ABS(FSUH2/FSUH1-1.) IF(CXF.LE.1.E-3) 00 TO 118 FSUM1-FSUM2 DO 188 J-1,3 SF1CJD=SF2CJD CONTINUE N1-2.#N2 D1-02 IFCK.GT.73 80 TO 118 60 TO 45 FI-FSUM2 RETURN SUBROUTINE CONCTHETA, YFD DIMENSION B(2) COMMON /A1/ Y,XK8,DX1,C1 T=TANCTHETAD FF1=COSCTHETAD CO2=FF1=FF1 F2-SINCTHETAD F3-Y+F2 A=XK8/CO2 BC12=DX1=FF1+F3 B(2)40X1#FF1-F3 XT-CI+A E-9.8 CABSCYD LE. I.E-183 IE-IFCABSCYD. GT. I.E-18) IS DO 28 I-1, 18 YT-BCIDBA

FS=XT=XT+YT=YT GS-XT+8.82+XT+XT+8.82+YT+YT IF(F3.6T.1.AND.83.8T.8.) CALL SIMP(XT,YT,VAL,VAL1) IF(F3.LE.1.0R.6S.LE.0.) CALL SCONCXT,YT,VAL,VAL1) YF1=2. #VAL+ALOB(C1#C1+B(I)#B(I)) YF=YF+YF1 CONTINUE & RETURN END SUBROUTINE SIMPCTCI, TBI, VALR, VALID DIMENSION \$1(3), \$2(3), \$A1(3), \$A2(3), CX(2) N1-28 D1=3.1418/(2. =N1) K-I DO 18 1-1,3 SICI3-8.8 SAICED-8.8 CONTINUE DO 28'I=1,N1+1 ALPHA=DI=(I-1) IFCI.EQ.N1+1) ALPHA-60.805+3.1418/18 T-TANCALPHAD CS-COS(ALPHA) 1223 A1=T+TCI XII-EXPC-T2/(CS+CS) XIR-AI +XII XII-TBI=XII XI2=CA1=A1>+CTB1+TB1> VS=XIR/XI2 VSI-XII/XI2 II=I/2#2 IF(I.EQ. 1. OR. I.EQ. N1+1) IC=1 IFCII.EQ.ID ID-2 IFCIT.NE.I. AND.I.NE.I. AND.I.NE.NI+1) IC-S SICICO-SICICO+VS SAICICO-SAICICO+VSI CONTINUE VALT-CBI (1)+4. #\$1(2)+2. #\$1(3))#01/3. VA1=(SA1(1)+4, #SA1(2)+2, #SA1(3))#01/9 K=K+1 \$2(1)=\$1(1) \$2(3)=\$1(2)+\$1(3) 8A2(1)=8A1(1) SA2(3)-SA1(2)+SA1(3) N2=N1 D2-D1/2. \$2(2)-0.8-SA2(2)-8.8 DO 78 I-1,N2 ALPHA=02+(2+1-1) T-TANCALPHAD CS-COS(ALPHA) AI-T+TCI XII-EXPC-T)/(CS+CS) XIR-AI #XII XII-TBI +XII XI2-CAI#AID+CTBI#TBID VS=XIR/XIZ VSI-XII/XIZ \$2(2)=\$2(2)+YS SA2(2)-842(2)+V81

CONTINE VAL 2=(\$2(1)+4 =\$2(2)+2 =\$2(3))=02/3 A2=(SA2(1)+4.#SA2(2)+2:#SA2(3))#D2/3 IF(VAL1.EQ.8.8) CK(1)-8.8 . IF(VAL1.NE.8.8) CX(1)=ABS(VAL2/VAL1-1.) IF(VA1.ED.8.8) CX(2)=0.8 IF(VA1.NE.8.8) CX(2)=0.8 IF(CX(1).LE.1.E-3.AND.CX(2).LE.1.E-3) GO TO VAL 1-VAL 2 VA1-VA2 DO 188 J=1,3 S1(J)-S2(J) SAICJD-SA2CJD CONTINUE N1-2-N2 D1=02 IFCK.9T. 183 60 TO 118 80 TO 45 VAL R-VAL 2 VALI-VA2 RETURN END SUBROUTINE SCONCXT, YT, VALR, VAL COMPLEX+8 Z, VN, ZI VNR=8.8 VNI-8.8 Z=CHPLXCXT, YT) R-ABS(Z) IFCXT.NE.8.8) TH-ATANCABSCYT/XTDD IF(XT.EQ.8.8) TH-3.1416/2. IFCXT. SE. 8. 8. AND. YT. ST. 8. 8) THETHIN. 8 IFCXT. GE. 8. 8. AND. YT. LT. 8. 8) TH-TH IFCXT.LT.8.8.AND.YT.GT.8.80 TH-3.1418-TH IF(YT.E0.8) 60 TO 18 Z1-Z VN-9.5772157-CHPLX(ALOBCR), TH)-ZI DO 28 1-2, 1888 XN-FLOATCID Z1=CQ+1)=Z1=C-Z3/OQ+200 VN-VN-Z1 ARL-REAL (VND ADI-ADHAGCYND IF (ARL. EQ. 8: 8: AND. ATH. EQ. 8. 8) 60. TO 25 BRL-ABS(I .- VNR/ARL) BIN-ABS(I.-VNC/AIN) IF(ABS(BRL), LE. I. E-5) AND ABS(BIN), LE. I. E-5) YNWMEDP(Z) IF(ABS(BRL), LE. I. E-5, AND, ABS(BIN), LE. I. E-5) GO TO 100 VNRMARI VNT-ATH CONTINUE VN-VN-EXP(Z) WRITE(5, +) 'UNCONVERGENCE Z=',Z 90 TO 199 X1-ABS(XT) 48.5772157-ALOQ(X1)-X1 DO 38 1-2, 1888 XN-FLOATCED X1=COH-1>=X1=ABSCXT>/CO WN-XI ARL-REAL CYND

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ATH-ATHAS(VN) BRL-ABS(1.-ARL/VNR) BIN-ABS(1, -AIN/VNI) IF (ABS(BRL), LE. 1.E-3, AND ABS(BDO, LE. 1.E-3) VIEVNEDP(Z) IF (ABS(BRL), LE, 1, E-3, AND, ABS(BIH), LE, 1, E-3) GO TO 188 VNR-AR VNTRATH CONTINE TYPE ... 'UNCONVERGENCE X-', X VALR-REAL CVND VAL T-ATHAR(VN) RETURN FND SUBROUTINE SUSTXX.Y.772 COMMON /A/ NOL NOL NOZ NZ NZI NZZ XL T.XC213, ZC113, XCC283, ZC(18) 1.XKB. WS. XS. XE 1,X80,W5,X5,XE COMMON /D/ V1(29,10),V2(28,10),V3(28,10) (COMMON /A// Y1(28,10),V2(28,10) COMMON /A// Y1(XK,DX1,C1,II) VI-V XK-XKB DO 18 J-1.NZ Z1-ZCJ) DO 18 1-1.NX TYPE . 'SUS ,J. * Ter ÷. XI-XCD DX1=XX-XI C1=77+71 IF CABS(C1).LE.1.E-0) C1-1.E-4 IF CABS(Y).GT.1.E-10) CALL INTI(F1) IF CABS(Y).LE.1.E-10) CALL INTI(F1) FCI, JD-FI CONTINUE CC=1./3.1418 DO 58 J-1,NZ1 J1-J+1 DO 38 1-1,NX1 I1=I+1 P-FCI1, J12+FCI, J2-FCI, J12-FCI1, J2 VSCI.JD-P-CC CONTINUE CONTINUE RETURN FND SUBROUTINE INT2CEID CONHON /A1/ Y, XKB, DXI, CI, II -IFCOXI .LE.8.83 DX1-8. SUN-9.8 SUN1-0.8 THI-0.8 DO 10 I-1, 100 SC-FLOAT(I) XK8-DX1/CSC=9. 1418) TECS.GT. 13 60 TO 18 TH2-ACOS(S) -IF(TH2.0T.3.1416/2.) TH2-3.1416/2. CALL SIMPSNCTHI, TH2, FU, VALD IFCTH2.8E.3.1416/2.3 GO TO 2 IFCSUM.EQ.8.83 CX-8.8

IF(SUM.NE. 8.8) CX=ABS(SUM1/SUM-1.) IF(CX.LE.1.E-3) 60 TO 28 SUH!-SUH THI-TH2 CONTINE ANG-TH2/3.1416=188. F1-SUN=2. RETURN SUBROUTINE INTICEID DIHENSION T(18) COMMON /A1/ Y, XX8, DX1, C1, II EXTERNAL FUI FCO-X=188./3.1416 GGCA, B, THETA) - A=COSCTHETA) -B-TANCTHETA) PT-3.1416 B-OX1/Y R=SORT(DX1=DX1+Y=Y) ALPHA=ACOS(DX1/R) THF=PI/2. F1-8.8 THI -- PI/2. +ALPHA IFCTH1.6T.8.82 60 TO 28 TT-FCTHID SUM1-0.8 N-0 " THETA-- 60.=3.1410/180. N-N+1 BB-FLOATON) . A-RR PT/(YKR Y) A-BOHL/LARGETS TH2=ATANCA+COSCTHETA)-8) IF(ABS(THETA/TH2-1.).LE.I.E-2) TS=(THETA+TH2)/2. IF CABSCINETA/TH2-1.3.LE.1.E-2) CALL STACK(N, TS, T) IF CABSCINETA/TH2-1.3.LE.1.E-2) GO TO 10 THETA=(TH2+THETA)/2. IFCTHETA.LT.8.80 GO TO 5 N-N-1 IFCN.EQ.80 N=1 IFCN.GT.18) NH-18 AU-0.8 DO 15 I-1.NN NI=NN-I+I AL-TONID IFCAL.LT. THID AL-THI . IFCN.EQ. 1) AL-THI CALL SIMPSNCAL, AU, FUI, VALD A1-FCAUD A2-FCAL) F1-F1+VAL IF(ABS(AL-THI).LE.1.E-8) 60 TO 2 IF(F1.E0.8.8) CX-8.8 IF(F1.NE.8.8) CX-ABS(SUHI/F1-1.) IF(CX.LE. 1.E-4) 60 TO 28 SUNI-FI AU-AL CONTINUE IFCTHI .LT.8.83 THI-8. XL-TH1 XU-89.99-3.1416/188. FLOATON

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A-BB-PI/CXX8-Y) XHe(YI +YII)/2 YL=GGCA, B, XL) YU-GGCA, B, XU) YH-GGCA, B, XH) IF CYH-YL . OE . 8.85 XL-XH IF CYH-YL . LT . 8.85 XU-XH TI-FOR) T2 FCXU) IF CABSCKU-XL).LE.1.E-6) TH2-CXL+XU)/2. IF CABSCAU-XLD.LE.I.E-60 GO TO 38 GO TO 25 IF CTH2:LT. THID GO TO 50 CALL SIMPSNCTHI, TH2, FUI, VALD A1-FCTH12 A2=F(TH2) F1=F1+VAL IFCTHI . GT . F(80) . AND . ABS(VAL) . LE. 1 . E-28) GO TO 7 IF(F1.E0.8.8) GO TO 55 -IF(F1.NE.8.8) CX-ABS(SUH1/F1-1.) IFCCX.LE.1.E-47 GO TO 78 SUM1-F1 THI-TH2 N-N+1 XL-THI IFCN.LE. 1888) 60 TO 25 RETURN END SUBROUTINE STACK(N. TS. T) DIMENSION T(18) IF(N.LE. 18) 60 TO 18 DO 28 1-1,9 II-I+I TOD-TOTO CONTINUE TCI8)=TS GO TO 38 TCND-TS RETURN 20 FND SUBROUTINE SIMPSNCA, B, F, VAL) DIMENSION SI(3), S2(3) N1-18 DI=CB-AD/NI K=1 DO 18 1-1,3 SICID-0.8 CONTINUE DO 28 1-1.NI+1 ALPHA#A+DI#CI-13 VS-FCALPHA) ·II-I/2+2 IFCI.EQ. 1. OR. I.EQ.NI+13 IC-1 . IF(II.EQ.I) IC=2 IF(II.NE,I.AND.I.NE.I.AND.I.NE.NI+1) IC=3 SICICO-SICICO+VS CONTINUE VAL1=(\$1(1)+4.#81(2)+2.#\$1(3))#01/3 K=K+1 52(1)-51(1) 52(3)=61(2)+51(3) N2=N1

02=01/2. \$2(2)-0.8 DO 78 I-1.N2 ALPHA-A+02=(2=I-1) VS-FCALPHAD" \$2(2)-\$2(2)+VS CONTINUE VAL2=(52(1)+4.=52(2)+2.=52(3))=02/3. VAL2-US2(1)44, HS2(2)42, HS2(3) HS2(3) IF(VAL1.E0.8.8) CX=0.8 IF(VAL1.HE.8.8).CX=ABS(VAL2/VAL1-1:) IF(CX.LE.1.E=4) G0 T0 118 VAL I-VAL2 00 100 J 1,3 CONTINE N1=2mN2 D1-02 IFCK.GT. 18) 60 TO 118 GO TO 45 VAL-VAL2 RETURN END FUNCTION FUCTHETAD DOUBLE PRECISION XII.FI.F2.BI.B2.A CONHON /A1/ Y, XK8, DX1, CI, I FI-COSCTHETAD F2=SINCTHETAD A=XK8/(F1=F1) XII-EPCA-CI) BI-YKRDYL/FI FU-XII-SIN(B1) RETURN . FND FUNCTION FUICTHETA) COMMON /AL/ Y, XK8, DX1, CI, I F1=COSCTHETA) F2-SINCTHETAD A-XK8/(F1-FI) XT1=EXPCA=CID B1-A=(DX1=F1+Y=F2) FUT=XII=SIN(B1) RETURN END SUBROUTINE CUBICI (N, X, Y, Y2) DIMENSION XCN), YCN), Y2CN), FC30), GC30) Y2(1)-8.8 Y2CN3-8.8 N1-N-I 8(1)-8. F(1)-0. DO 2 K#1.NI J2-K+1 H2=X(J2)-X00 R2=(Y(J2)-Y(K))/H2 IF(K.E0.1) 60 TO 1 Z=1./(2.#(HI+H2)-HI#6(J1)) G(K)-ZHH2 H=0. +(R2-R1) IF(K.EQ.2) HHI-HIWY2(1) IF(K.EQ.N1) HHI-HIWY2(1) FCKD=Z=CH-HI=FCJIDD

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JI-K HI-H2 RI-H2 V2(NI)-F(NI) T2(NI)-F(NI) T2(NI)-E,2) FETURN T2(NI)-E,2) FETURN N2(NI)-I DI JI-2,N2 N4(NI) Y2(C)-F(C)-8(C)+Y2(C)-1) Y2(C)-F(C)-8(C)+Y2(C)-1) Y2(C)-F(C)-8(C)+Y2(C)-1) Y2(C)-F(C)-8(C)+Y2(C)-1)

PROGRAM VLCTY " THIS PROGRAM CALCULATES THE NONDIMENSIONAL VELOCITY COMPONENTS ALONG THE ISOBARS WHICH ARE IN THE OUTPUT DATA OF PROGRAM "THINGUL" THPUT DATA (1) FROUDE NUMBER, DRAFT AND LEP OF THE SHEP (2) SOURCE- STRENGTH OF EACH SOURCE PANEL WHICH IS ALSO, IN THE OUTPUT DATA OF PROGRAM "THNGUL" DIMENSION FILE(4), UU(20), U(20, 10), WW(20), SH(20, 10), FIL1(4) COMMON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1, FR, VEL, XS, XE, XKB CONMON /D/ VIC28, 18, 33, V2(28, 18, 3), V3(28, 18, 3) TYPE . 'ENTER OUTPUTFILE NAME' FORMAT (4A4) CALL' ASSIGN(1, FILE) TYPE ., 'ENTER INPUTFILE NAME ACCEPT 1, FIL1 CALL ASSIGN(2, FIL1) XL-2.8 NX-21 NZ=11 NX1=NX-1 NZ1=NZ-1 READ(2, +) FR, TD, XLL DO 3 I=1.NXI READ(2,+) (SH(I,J),J=1,NZ1) CONTINUE CALL CLOSE(2) T=2. TD/XLL XK0-1./(2. +FR+FR) WRITECI, #2'FN = ',FR CALL POINT DO 189 K#1.NZ1 ZZ-ZC(K) XX=XC(NX1) ICP=3 YY=8.8 CALL SUPICXX, YY, ZZ, ICP) CALL SUP2CXX, YY, ZZ, ICP) CALL SUPSCXX, YY, ZZ, ICP) DO 18 I-1, NX1 DO 18 J=1,NZ1 VJ CI, J, 13-VICI, J, 13+V2CI, J, 13 VB(I,J, 1)=VI(I,J, 1)+V3(I,J, 1) Vh(I,J, 3)=VI(I,J, 3)+V3(I,J, 1) V3(I,J, 3)=VI(I,J, 3)+V3(I,J, 3) V3(I,J, 3)=VI(I,J, 3)+V3(I,J, 3) CONTINUE 18 DO 28 J=1, NX1 UUCJD-0.8 ISI-NXI-J+II IS2-NX1+J-II DO 38 JU-1,NZI IFCII.LE.JD UCII, JUD=VSCISI, JJ, 1) IFCII.0T.J) UCII.JJD-VICIS2.JU.1)

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CONTINUE DO 48 .II-1 .NX1 DO 48 JU-1,NZ1 UUCJ>-UUCJ>+UCII, JJ>+SHCII, JJ) CONTINUE CONTINUE DO 58 J=1,NX1 WVCJD-8.8 DO 68 11-1, NX1 IS1-NX1-J+II IS2=NX1+J-II DO 68 JU-1, NZI IFCII.LE.J) UCII.JJ)=V3(IS1.JJ,3) IFCII.GT.J) UCII.JJ)=V1(IS2.JJ,3) CONTINUE DO 78 II=1,NX1 DO 70 JJ-1, NZI WWCJD-WWCJD+UCII, JUD+SHCII, JUD CONTINUE CONTINUE WRITECI,=)'' WRITECI, #) ' ' WRITE(1,+) 'ISOBAR No. '. WRITECI,+) ' WRITE(1, *) 'NONDIMENSIONAL DISTURBANCE VELOCITY W/U WRITECI, +) CUUCID, I=1; NX1) WRITE(1,+) ' WRITE(1, *) "NONDIMENSIONAL DISTURBANCE VELOCITY w/U" WRITECI (+) CUNCIS, I-1, NX1) WRITECI, A CONTINUE STOP END SUBROUTINE POINT COMMON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1, FR, VEL, XS, XE, XKB SX=XL/(NX-1) S7=T/(NZ-1) DO 18 I-1,NX XCID=-1.+SX#CI-ID IFCI.EQ.NX) GO TO 18 XCCI)-1+SX+CI-8.5) CONTINUE DO 28 I=1,NZ ZCI3-T+SZ=CI-1) IFCI.EQ.NZ) 80 TO 28 ZCCI)=-T+SZ#CI-8.5) CONTINUE . RETURN FND SUBROUTINE SUPICXX, Y. ZZ. ICP) COMMON /A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), Z(18) 1, FR, VEL, XS, XE, XKB CONHON /D/ VI (28, 18, 3), V2(28, 18, 3), V3(28, 18, 3) CONHON /F/ F(21, 11, 3), F1(3) DOUBLE PRECISION FI,F DO 18 J-1.NZ ZI=Z(J) DO 18 1+1.NX XI-XCI) CALL COEFICXX, Y, ZZ, XI, ZI, XK8, FI, ICPS TYPE .,FI

DO 28 II-1, ICP FIL, J, II)-FICID CONTINUE CONTINUE CC=1./(4.#3.1418) DO 38 J-1,NZI J1=J+1 DO 38 1-1,NX1 I1-I+1 DO 48 II-1. 1CP P=F(II, JI, II)+F(I, J, II)-F(I, JI, II)-F(II, J, II) VICI, J, II)-PHCC CONTINUE CONTINUE RETURN FND SUBROUTINE COEFICXX, Y, ZZ, X1, Z1, XK8, F1, ICP) DIMENSION FICED DOUBLE PRECISION RI, R2, FI, DI, D2, XY, YZ DOUBLE PRECISION DX1, C1, C2 DX1-X1-XX CI-ZI-ZZ C2=Z1+ZZ IF(C1.E0.8.8) C1-1.E-4 IF(C2.E0.8.8)-C2-1.E-4 XY=DX1=DX1+Y=Y R1-SORT(XY+C1+C1) R2=SORT(XY+C2+C2) IF(ABS(Y).LE.1.E-10) F1(2)=0.0 IF(ABS(Y).ST.1.E-10) F1(2)=ATANC(DX1=C1)/(Y=R1) 1-ATANCCDX1+C2)/(Y+R2)) IFCXY.LE.1.E-10) F1C1D=DL00CABS(C2)/ABS(C1)) D1-C1+R1 D2=C2+R2 IF(XY.GT. 1.E-18) F1(1)=0L08(01/02) YZ=Y#Y+CI#CI IF(YZ.LE.1.E-18) F1(3)=-2.+DLOG(ABS(DX1)) D1=0X1+R1 D2=DX1+R2 IFCYZ. 8T. 1.E-10) F1(3)=0L08(D1+02) IFCICP.EQ.12 F1(2)-0.8 IFCICP.E0.1> FIC32-0.8 RETURN END SUBROUTINE SUP2CXX, Y, ZZ, ICP) CONHON -/A/ NX, NX1, NX2, NZ, NZ1, NZ2, XL, T, X(21), Z(11), XC(28), ZC(18) 1, FR, VEL, XS, XE, XKO CONNON /D/ V1(28, 18, 9), V2(28, 18, 3), V3(28, 18, 3) CONHON /F/ FC21, 11,30, F1(3) DO 18 J=1,NZ 21=2(J) DO LA Tel NX TYPE #, 'SU2 J=', J;' I=', I VI-Y(T) CALL COEFCXX, Y, ZZ, XI, ZI, XK8, FI, ICP) DO 28 II-1, ICP FCI, J, II)-FICII) CONTINUE CONTINUE CC-1./(4.#3.1416#5.1416) DO 38 J=1,NZ1) J1-J+1

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ICNT=1 F1-COSCTHET) F2=SINCTHET) A=XX2/(FI=FI) BC12-DX1+Y+F2 B(2)-DY1-Y-F2 IF(B(1)-B(2).LT.8.) THETA-THEND IF(8(1)=8(2).LT.8.) G0 T0 188 IF(B(1).0E.8.8) TI-3.1418-2. IF(8(1),LT.8.8) T1=3.1416=2. XT=C1=A TEMP-0 DO 48 I-1.2 YT-BCIDAA FS-XT+XT+YT+YT GS=XT+0.82=XT=XT+0.82=YT=YT -IF(FS.0T.1.AND.0S.0T.0.) CALL SIMP(XT,YT,VAL,VAL)) IF(FS.LE.1:0R.0S.LE.0.) CALL SCOM(XT,YT,VAL,VAL)) TEHP-TEHP+CATANCBCID/CID+VAL10/TI CONTINUE A1-ALOGCTEMPD/CI CX1=ABS(A1/A-1.) A-AI IF(CX1.GT.1.E-4) GO TO 38 12-XKR/41 IFCABSCA2). GT. 1.) THETA=THEND IF (ABS(A2) . LE. 1 .) THETA=ACOS(SORT(A2)) CX2=ABSCTHETA/THET-1.) THET-THETA ICNT-ICNT+1 IF(ICNT.ST.58) 60 TO 100 IFCTHETA .NE. THEND. AND. CX2. ST. 1. E-43 RD TO 20 RETURN END SUBROUTINE INT(NI, ST, EN, YF, ICP, ICC) DIMENSION YF(3), F(3), SF1(3, 3), SF2(3, 9), FSUMI (3), FSUM2(3), CXF(3) COMMON /A1/ Y, XK8, DX1, CI WRITE(4, +) / DI-CEN-STO/NI DO 18 I=1, ICP DO. 18 J-1,3 SF1(I.J)-8.8 CONTINUE DO 28 I=1,NI+1 THETA-ST+D1+CI-1) ANG=THETA=180./3.1416 CALL CONCTHETA, F, JOP) WRITEC4, #) ANG, F II=1/2=2 IF(I.EQ. |. OR. I.EQ. NI+1) IC=1 IF(II.ED.I) IC-2 IFCII.NE. I.AND I NE. 1. AND. I.NE. NI+12 IC-3 DO 38 J-1, ICP SFICH, IC)-SFICH, IC)+FCU2 CONTINUE CONTINUE DO 48 I-1, ICP FSUMICID=(SFICI, 1)+4. #SKICI, 2)+2. #SFIEI, 3)+01/5 FSUM2CID=FSUMICID CONTINUE TYPE ., FSUMI IFCICC.EQ.1> GO TO IIS
K-K+1 58 I=1,ICP SF2(I;1)=8F1(I,1) SF2(I;3)=8F1(I,2)+8F1(I,3) CONTINUE . N2=NI Ma-01 /2 DO 08 1-1.10P SF2(1,2)-8.8 CONTINUE 78 I-1.N2 00 78 1-1, N2 THETA-ST+D2#(2*I-1) CALL CONCTHETA, F, ICP) D0 88 J=1, ICP) SF2(J,2)=SF2(J,2)+F(J) CONTINUE CONTINUE 'n 20 98 I-1.ICP 00 00 - 01-07 F #342C1-9478(1)>4.4F72C1,2>4,4F72C1,3>>402/3, FF (584)(C1 581,8,0) 07(2)-4,8 FF (584)(C1 581,8,0) 07(2)-4,8 FF (584)(C1 + 584)(C1 + 584) · CONTINUE 184 N1=2.=N2 D1=D2 -IF(K.GT.7) G0 T0 118 G0 T0 45 c 00 128 1-1, ICP 118 128 CONTINUE RETURN RETURN END SUBROUTINE COMMITTER, YF, ICP) DIMENSION YF(C3), B(2) COMMON /AI/ Y, XOB, DX1, C1 TETANCITETAS FFI-COSCINETAS CO2+FFI-FFI F2=SDIKTHETAS F2=SDIKTHETAS F3=YeF2 A=XK8/C02 BC12-DX1+FF1+F3 BC22-DX1+FF1-F3 XT-C1+A 00 18 I-1, ICF ۵ CONTINUE 18 IFCABSCY) .LE. I.E-8) IS-IFCABSCYD. ST. 1.E-8) DO 28 I-1,IS YT-BCIDHA FS-YTAYTAYTAYT

65-XT+8-82-XT=XT+8.82-9T=YT IF(FS.GT.1.AND.GS.GT.8.) CALL SIMP(XT,YT,VAL,VAL)) IF(FS.LE.1.0R.6S.LE.0.) CALL SCON(XT,YT,VAL,VAL)) YF1=2 #VAL+ALOR(C1+C1+B(I)+B(I)) YFCID=YFCID+YFI IF(ICP.EQ.1) 60 TO 28 IFCIS.EQ.2.AND.I.EQ. 1) YFC2)=YFT IF(IS.EQ.2.AND.I.EQ.2) YF(2)-YF(2)-YF IF(IS.E0.1) YF(2)-0.8 IF(YT.LT.0.8) T1-3.1416 INCYT. 6T. 8.83 T1-3.1416 YRS-ATANCE(T)/CI)+TI PERCYT) YF(3)-YF(3)+VAL (+Y83 CONTINUE YF(2)-YF(2)aT YF(3)=YF(3)/FFI IF(IS.E0.2) GO TO 38 DO 38 141,ICP YFCD-2. YFCD CONTINUE RETURN END SUBROLITINE SIMPCTCL. TBL. VALR. VALLD DIMENSION \$1(3), \$2(3), \$41(3), \$42(3), CX(2) N1-28 D1=1 1410/(2 =N1) K=1 DO 18 I-1.3 \$1(D-0.8 SAICT2=0.8 CONTINUE DO 28 1=1,NI+1 ALPHA=D1=(I-1) IFCI.ED.NI+1) ALPHA 9.995#3.1416/11 T-TANCALPHA> CS=COS(ALPHA) A1-T+TCI XII-EXP(-T)/(CS=CS) XTR-A1eXTI XTT=TB1=XT1 XI2-CA1=A12+CTB1=TB12 VS-YTP/YT2 VS1-XII/XI2 II=1/2=2 IF(I.EQ. | . OR. I.EQ. NI+1) . IC=1 IFCII.EQ.ID IC-2 IFCII.NE.I.AND.I.NE.I.AND.I.NE.NI+1) IC-S SICTC2=SICTC2+VS SAICICD=SAICICD+VSI CONTINUE VAL1=(S1(1)+4.#S1(2)+2.#S1(3))#D1/3. VA1=(SA1(1)+4: #SA1(2)+2. #SA1(3))=D1/3. K=K+1 S2(1)=S1(1) \$2(3)=\$1(2)+\$1(3) SA2CID-SA1CID SA2(3)-SA1(2)+SA1(3) N2-NI D2=01/2. \$2(2)-8.8 SA2(2)=0.0 DO 78 I-1,N2

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ALPHA-02+(2+I-1) T-TANCALPHA) CS-COSCALPHA) AI-T+TCI XII-EXP(-T)/(CS+CS) XIR-A1-XII XII-TB1+XII XI2-CAIMAID+CTBINTBID VS-XIR/XIZ \$2(2)=\$2(2)+VS \$A2(2)=\$A2(2)+VS1 CONTINUE VAL2=(52(1)+4:#52(2)+2.#52(3))#02/3 VAL2*(52(1)+4, #52(2)+2, #52(3)+#223. #7(VAL1.10, 8,0) CX(1)=0.8 IF(VAL1.NE.0.0) CX(1)=0.8 IF(VAL1.NE.0.0) CX(1)=ABS(VAL2/VAL1-1.) IF (VAL 1. HE. 8.8) CX(2)-8.8 IF (VAL 1.60.8.8) CX(2)-8.8 IF (VAL 1.6E.8.8) CX(2)-8.8S(VA2/VA1-1. IF (CX(1)_LE.1.E-3.AND.CX(2)_LE.1.E-VALI-VALZ D0 188- J-1,3 S1(J)-S2(J) SA1(J)-SA2(J) CONTINUE N1-2-N2 D1=02 IFCK.ST. 18) GO TO ITE GD TO 45 VAL R-VAL 2 VALI-VA2 RETURN ĐØ SUBROUTINE SCONOT, YT. Y R.VALTT COMPLEXIES Z, VN, ZI VNR=0.8 VNI=0.8 Z=CHPLX(XT, YT) R=ABS(Z) 4 IFOT.NE.8.8) ATANCABS(YT/XT)) JFCXT. FQ. 8. 83 TH-9. 1416/2 IFOT. BE. 8. 8. AND. CB. 8. TP. IFCXT. 6E. 8. 8. AND. YT LT. 8:85 TH-TH IFCXT. LT. 8. 8. AND. YT LT. 8:85 TH-TH IFCXT. LT. 8. 8. AND. YT. 8T. 8. 80 TH-5. 1418-TH IFCXT. LT. 8. 8. AND. YT . LT. 8. 80 TH-5. 1418-TH TO .EQ.83 GO TO 18 8.5772157-CHPLXCALOBCRD, THD-ZI VA 28 1=2,1888 XH-FLOATCD Z1-CON-13=Z1=(-Z3/CON=300 WH-WH-ZI ARL REAL CYND ATH-ATHACKNY IFCARL.EQ.8.8.AND.ATH.EQ.8.89 GO TO 26 BRL-ABSCI.-WRVARLS BTH-ABSCI.-WRVARLS . IF CABS(BRL). LE. I.E-E ND. ABSCOTHD . LE. L E-6) (2) IFC S(BRL), LE. 1.E-6.AND, ABS(BDD), LE. 1.E Èn. c'n 70

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VNTHATH CONTINUE VN=VN=EXPCZ) WRITE(5, +) 'UNCONVERGENCE Z='.Z 60 TO 188 X1-ABS(XT) VN=-0.5772167-AL09(X1)-X1 DO 38 1-2, 1888 XN-FLOATCT) X1-CXN-12+X1+ABSCXT2/CXN+XN2 VNeVN-X1 ARL-REAL CVND AIM-AIMABOWND BRL=ABSCI .- ARL/VN BIN-ABS(1 .- ADH/VNI) IF CABS CBRUD. LE. 1. E-3. AND. ABSCRIND. LE. T. E-80 VN=VN+EXPCZ IF (ABS(BRL).LE.1.E-S.AND.ABS(BIN).LE.I.E-S) 60 TO 189 VNR-ARL VNI-AIH CONTINUE . TYPE +, 'UNCONVERGENCE X=', X VN-VN-EXPCZD VALR-REAL CVND VALI-AIMAG(VN) RETURN END SUBROUTINE SUPSCXX, Y, ZZ, ICP) COMMON /A/ NX, NXI, NXZ, NZ, NZI, NZZ, XL, T, X(21), ZC(1), XC(28), ZC(18) 1, FR, VEL, XS, XE, XKB COMMON /D/ VI(28,18,3),V2(28,18,3),V3(28,18,3) COMMON /F/ F(21,11,3),F1(3) COMMON /A1/ Y1,XX,DX1,C1,II Y1-Y YKHYKR DO 18 J-1.NZ ZITZCJD DO 18 I-1,NX TYPE . 'SUS XI-XCID DX1=XX-X1 C1=77+71 IFCABS(CI).LE.1.E-8) C1-1.E-4 IFCABS(Y).GT.1.E-8) CALL INTICF(,ICP) IFCABSCYD.LE. I.E-OD CALL INT2(F1, ICP) DO 28 II-1. ICP FCI, J, IID-FICID CONTINUE CC=1./3.1410 DO 38 J=1,NZ1 Jim.Ht DO 38 1-1, NX1 3 II-I+I DO 48 11-1, ICP P=F(I1, J1, II)+F(I, J, II)-F(I, J1, II)-F(I1, J, II)-V3(I, J, II)+F+CC CONTINUE CONTINUE RETURN END. SUBROUTINE INTZEFI, ICP DIHENSION FICED

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COMMON /A1/ Y, XK8, DX1, CI, II EXTERNAL FU DO 5 II-1. ICP IFCOXI.LE.8.83 FICED-8.8 IFCOM LE.8.83 60 TO 5 TFCTT.ED.2) F1CTT2=8.8 IFCIT.E0.22 GO TO 5 IF(DX1.LE.0.8) DX1-0.8 SUM-8.8 . SIMI-R R THI-8.8 DO 18 I-1.1888 IF CIT . EQ. 13 SC-FLOATCES IFCII.NE.1) SC FLOATCID-2 S=XX8=DX1/(SC=S, 1418) TF(S. MT. 1) BO TO 18 TH2=ACOS(S) IF (TH2. BT. 3. 1416/2.) TH2-3. 1416/2 G1=TH1=188./3.1416 62-TH2-168./3.1416 CALL SIMPSNCTHI, JH2, FU, VALD SUM-SUM+VAL IF (TH2.8E.3.1418/2.) 60 TO 28 IF (SUH, EQ.8.8) CX-0.8 IF (SUH, NE.8.8) CX-0.8 IF (SUH, NE.8.8) CX-ABS(SUH1/SUH-1.) IF (CX.LE.1.E-4) 60 TO 28 SHI-SH TH1=TH2 CONTINUE ANG=TH2/3: 1416=188 FICETO-SUNA2. CONTINUE RETURN END SUBROUTINE INTICEI, ICP) DIMENSION FICED, TCIED COHHON /A1/ Y, XK8, DX1, C1, II EXTERNAL FUT PCXD-X=188./3.1418 AUCOSCINETA)-8-TANCINETA) PI-3.1416 B-DXI/Y SORT(DXI=DXI+Y=Y) ALPHA=ACOSCOX1/R> AA=FCTH15 THE PL/2. DO 188 11-1, ICP TYPE's, 'samall', HI FICILID-8.8 THI-PI/2.+ALPHA TYPE ., 'THI ... THI IFCTH1.8T.8.8) 60 TO 28 TT-FCTHI) TYPE ., 'II THUL', TT SUM1-0.8 THETA- 68.=9.1416/188. N-N+1 BB-FLCATCND A-BB+PI/COKB+Y) TH2=ATANCA=COSCTHETAD-BD IF (ABS(THETA/TH2-1.).LE.1.E-2)

IF CABSCTHETA/TH2-1.).LE.I.E-2) CALL STACKON, TS, TO. IF(ABS(THETA/TH2-1.).LE.I.E-2) GO TO 18 THETA=CTH2+THETA3/2. IF (THETA.LT. 8.8) GO TO 5 N-N-1 TYPE ., 'THE NUMBER OF ZERO POINT N-', N IF(N.E0.8) N=1 IF(N.GT. 18) NN=18 IF(N.LE. 18) NN=N AU-8.8 DO 15 1=1, NN NI=NN-I+I AL-TONID IFCAL.LT. THID AL-THI IFCN.EQ. 1) AL-THI CALL SIMPSNCAL, AU, FUI, VALD A1=FCADO A2-FCAL) TYPE +, 'AU-', A1, 'AL-', A2, 'VAL-', VAL FICID-FICID+VAL FICID= IF(CX.LE.1.E-4) 60 TO 28 SUH1-FICITS AU-AL CONTINUE IF(TH1 .LT.8.8> TH1-8.8 XL-TH1 XU-89.99#3.1416/188. BB=FLOAT(N) A-BB+PI/(XKØ+Y) YH=(YI +YII)/2 YL-GBCA, B, XL) YU-BBCA, B, XUD YH-GGCA, B, XH) TYPE *, 'XL-', XL, 'YL-', YL TYPE *, 'XL-', XL, 'YL-', YL TYPE *, 'XU-', XN, 'YM-', YN TYPE *, 'XU-', XU, 'YU-', YU IF(YH-YL.GE.8.8) XL-XH IF (YHWYL.LT. 8,8) XU-XH TI-FCXI) TRECKIN IF CABS (XU-XL).LE. 1.E-8) TH2=(XL+XU)/2. IF CABS (XU-XL).LE. 1.E-8) 80 TO 38 GO TO 25 IFCTH2.LT.THID GO TO 50 IFCABSCTH1-TH23.LE.I.E-63 TH2-60.00+8:141 CALL SIMPSNCTH1, TH2, FU1, VALD. A1-FCTHI) A2-FCTH2) TYPE ... THI-', A1, 'TH2-', A2, 'WAL-', VAL IF(TH1.GT.F(88), AND. ABS(VAL).LE. 1.E-20) 60 TYPE W, 'FICID-', FICID IF(FICID.EQ.8.8) 60 TO 55 IF(FICIT) NE. 8. 8) CX=ABS(SUMI/FICIT)-(.) IF(CX.LE.1.E-4) GO TO 188 SUNI-FICITS THI-TH2 N-N+

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XI =THI IF (N.LE. 1888) 60 TO 23 CONTINE RETURN END SUBROUTINE STACK(N. TS. T) DIMENSION T(18) IF(N.LE. 18) 60 TO 18 DO 28 I-1,9 · I1-I+! . TCD=TCI1) CONTINE TCI82-TS 60 70 38 TCND=TS RETURN END SUBROUTINE SIMPSNCA, B, F, VALD DIMENSION SI(3), S2(3) NI-18 DI-CB-AD/NI K-1 DO 18 I-1,3 St CID-8.8 CONTINUE DO 28 I=1.N1+1 ALPHA=A+D1#CI-1) VS-FCALPHAD II-I/2-2 IFCI.ED. 1. OR. I.EQ. N1+13 IC=1 IFCII.EQ.ID ID-2 IF(II.NE.I.AND.I.NE.I.AND.I.NE.NI+1) IC-S SICICO-SICICO+VS CONTINUE VAL1=(\$1(1)+4,#\$1(2)+2,#\$1(3))#01/3, K=K+1 \$2(1)=\$1(1) \$2(3)=\$1(2)+\$1(3) N2-N1 D2=01/2. \$2(2)-0.8 00 78 1-1.82 ALPHA=A+D2=(2=I-1) VS-FCALPHAD a \$2(2)-\$2(2)+VS CONTINUE VAL2=(82(1)+4.=82(2)+2.=52(3))=02/3. IF(VAL1.ED.8.8) CX-8.8 IF(VAL1.NE.8.8) CX-ABS(VAL2/VAL1-1.) IFCCX.LE.1.E-40 80 TO 118 VAL1-VAL2 00 100 J=1,3 \$1(J)=\$2(J) CONTINUE N1=2=N2 D1=02 IFCK. 8T. 18> 80 TO GO TO 45 118 VAL-VAL2 288 RETURN FND

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