A METHOD FOR THE ANALYSIS OF THE MDTF DATA USING NEURAL NETWORKS

CENTRE FOR NEWFOUNDLAND STUDIES

TOTAL OF 10 PAGES ONLY MAY BE XEROXED

(Without Author's Permission)

MOHAMED IBRAHIM







INFORMATION TO USERS

This manuscript has been reproduced from the microfilm master. UMI films the text directly from the original or copy submitted. Thus, some thesis and dissertation copies are in typewriter face, while others may be from any type of computer printer.

The quality of this reproduction is dependent upon the quality of the copy submitted. Broken or indistinct print, colored or poor quality illustrations and photographs, print bleedthrough, substandard margins, and improper alignment can adversely affect reproduction.

In the unlikely event that the author did not send UMI a complete manuscript and there are missing pages, these will be noted. Also, if unauthorized copyright material had to be removed, a note will indicate the deletion.

Oversize materials (e.g., maps, drawings, charts) are reproduced by sectioning the original, beginning at the upper left-hand corner and continuing from left to right in equal sections with small overlaps.

Photographs included in the original manuscript have been reproduced xerographically in this copy. Higher quality 6" x 9" black and white photographic prints are available for any photographs or illustrations appearing in this copy for an additional charge. Contact UMI directly to order.

> ProQuest Information and Learning 300 North Zeeb Road, Ann Arbor, MI 48106-1346 USA 800-521-0600

> > **I**Mľ

A METHOD FOR THE ANALYSIS OF THE MDTF DATA USING NEURAL NETWORKS

By

© Ibrahim Mohamed, B.Eng.

A thesis submitted to the School of Graduate Studies in partial

fulfillment of the requirements for the degree of Master of Engineering

Faculty of Engineering and Applied Science

Memorial University of Newfoundland

May 2000

St. John's

Newfoundland

Canada

ABSTRACT

Numerical simulation techniques are widely used to investigate the behavior of submarines during the design stage. The accuracy of these techniques depend upon the accurate determination of the hydrodynamic coefficients for the model.

The Marine Dynamic Test Facility (MDTF) is a new-six-degree-of-freedom forced motion testing rig. The rig has the ability to test underwater vehicles in a manner that makes it possible to determine the hydrodynamic coefficients in the equations of motion. Multi-variant linear regression is used to obtain the hydrodynamic coefficients from the experimental data.

In this study a neural network technique to identify the hydrodynamic model from experimental data is investigated. The technique uses the model trajectory (motion history) to predict the hydrodynamic coefficients of the model. A single MDTF generated maneuver was used to train the network. The trained network was then tested using different maneuvers and the network predictions were compared to the actual MDTF measured forces and moments.

Results obtained from the neural network technique indicate that the technique can be used to predict the hydrodynamic model of underwater vehicles. The use of this technique can dramatically cut the running costs to conduct experiments on new models.

ACKNOWLEDGMENTS

I would like to express my endless and inexpressible gratitude to my supervisor Dr. M. R. Haddara for the financial, moral, academic support, and encouragement. I would also like to express my gratitude and appreciation to the members of the advisory committee: Dr. C. D. Williams and Mr. M. Mackay for their help and guidance during this study.

I am grateful to my course instructors Dr. L. Lye, Dr. I. Jordaan, Dr. A. Swamidas, Dr. M. Hinchey, and Dr. Haddara for their dedication and academic proficiency.

I would like to thank the staff of the Institute for Marine Dynamics especially Spence Butt, Kent Brett, Bud Mesh, and Caroline Muselet.

Finally I would like to express my gratitude to my fellow graduate students at Memorial University of Newfoundland Faculty of Engineering for their support and encouragement.

CONTENTS

Abstract
Acknowledgmentsii
Contents
List of Figuresvii
1. Introduction and Literature Survey
1.1. THEORETICAL APPROACH
1.2. EXPERIMENTAL METHODS
1.3. PARAMETRIC IDENTIFICATION APPROACH
1.4. Scope and Objectives
1.5. METHODOLOGY
1.6. THESIS OUTLINE
2. Neural Networks
2.1. BIOLOGICAL NEURAL SYSTEMS
2.2. ARTIFICIAL NEURAL NETWORKS
2.3. ANN Squashing Functions
2.3.1. STEP FUNCTIONS:
2.3.2. SIGMOID FUNCTIONS:

2.3.3. GAUSSIAN FUNCTIONS.	11
2.4. TYPES OF NEURAL NETWORKS:	12
2.4.1. LAYERED NETWORK	13
2.4.2. ACYCLIC NETWORK	13
2.4.3. FEEDFORWARD NETWORKS	14
2.5. BACKPROPAGATION TRAINING ALGORITHM	15
2.6. MOMENTUM UPDATE	
3. Mathematical formulation	20
3.1. EQUATIONS OF MOTION	20
3.2. NEURAL NETWORK MODEL	
3.3. LINEAR REGRESSION MODEL	24
3.3.1. UNCOUPLED HEAVE MODEL	25
3.3.2. UNCOUPLED PITCH MODEL	25
3.3.3. COUPLED HEAVE AND PITCH MODEL	26
4. Fresh Water Towing Tank Experiments	
4.1. MARINE DYNAMIC TEST FACILITY (MDTF)	
4.1.1. MDTF Setup	
4.1.2. Experimental Setup	33
4.2. MANEUVERS	
4.2.1. CIRCULAR ARC MANEUVERS.	37
4.2.2. LINEAR CHIRP MANEUVERS	
4.2.3. PURE HARMONICS	40
4.2.4. MULTI-DEGREE-OF-FREEDOM MANEUVERS	40

4.3. I	DATA ACQUISITION	
4.3.1.	TIME TARE AND COORDINATES TRANSFORMATION	42
4.4. F	FILTERING	43
4.4.1.	WHAT IS A WAVELET ?	
4.4.2.	FILTERING PROCEDURE	45
4.5. N	NEURAL NETWORK APPROACH	45
5. Resu	ults and Discussion	47
5.1.1.	UNCOUPLED HEAVE MOTION GENERATION	47
5.1.2.	UNCOUPLED PITCH MOTION GENERATION	51
5.1.3.	COUPLED HEAVE AND PITCH MOTION	54
5.1.4.	EFFECTS OF RANDOM NOISE	55
5.2. H	RESULTS FROM DIGITALLY GENERATED DATA	55
5.3. F	RESULTS FROM EXPERIMENTAL DATA	62
5.4. I	DISCUSSION	85
6. Con	clusions	91
7. Reco	ommendations	93
Reference	CC3	94
Appendi	ix A Numerical Results	97
Appendi	ix B Visual Basic Program "Simulation"	102
Appendi	ix C List of Runs	107

Appendix D Visual Basic Program "PrepShop"	
Appendix E MatLab Filtering Script	

LIST OF FIGURES

2

Figure 2.1 Biological neuron
Figure 2.2 Step Function 10
Figure 2.3 Sigmoid Function
Figure 2.4 Bell shape function
Figure 2.5 Layered neural network
Figure 2.6 Acyclic neural network
Figure 2.7 Feedforward neural network
Figure 3.1 Model coordinates system
Figure 3.2 Neural network structure
Figure 4.1 MDTF General Arrangement
Figure 4.3 MDTF Sub-Carriage
Figure 4.5 Lateral Motor Arrangement
Figure 4.7 Vertical Motor Arrangement
Figure 4.9 Forward Strut Universal Joint
Figure 4.11 DREA Standard submarine model dimensions
Figure 4.7 Side view of the MDTF setup
Figure 4.14 Top view of the MDTF setup
Figure 4.9 Arc maneuver trajectory in the lateral plane r' = 0.2
Figure 4.11 Pure heave chirp, frequencies 0.1 to 0.5 Hz

Figure 4.12 Model configurations
Figure 5.1 Hydrodynamic Force vs. Acceleration at 0.5 Hz uncoupled heave48
Figure 5.2 Hydrodynamic force vs. velocity at 0.5 Hz uncoupled heave
Figure 5.3 Hydrodynamic force vs. displacement at 0.5 Hz uncoupled heave49
Figure 5.4 Hydrodynamic force vs. acceleration at 1.5 Hz uncoupled heave49
Figure 5.5 Hydrodynamic force vs. velocity at 1.5 Hz uncoupled heave
Figure 5.6 Hydrodynamic force vs. displacement at 1.5 Hz uncoupled heave 50
Figure 5.7 Pitch moment vs. acceleration at 0.5 Hz uncoupled pitch
Figure 5.8 Pitch moment vs. velocity at 0.5 Hz uncoupled pitch
Figure 5.9 Pitch moment vs. displacement at 0.5 Hz uncoupled pitch
Figure 5.10 Pitch moment vs. acceleration at 1.5 Hz uncoupled pitch
Figure 5.11 Pitch moment vs. velocity at 1.5 Hz uncoupled pitch
Figure 5.12 Pitch moment vs. displacement at 1.5 Hz uncoupled pitch
Figure 5.13 Comparison between least square estimation and neural net prediction
(uncoupled heave at 0.6 Hz)
Figure 5.14 Comparison between least square estimate and neural net prediction
(uncoupled heave at 1.5 Hz)
Figure 5.15 Plot of actual force vs. neural predicted force (uncoupled heave at 0.7 Hz).57
Figure 5.16 Plot of actual force vs. least squares estimated force (uncoupled heave at 0.7
Hz)
Figure 5.17 Comparison between least square estimation and neural network prediction
(uncoupled pitch at 0.7 Hz)

Figure 5.18 Comparison between least square estimation and neural network prediction
(uncoupled pitch at 1.2 Hz)
Figure 5.19 Plot of actual pitching moment vs. neural predicted pitch moment (uncoupled
pitch at 0.7 Hz)
Figure 5.20 Plot of actual pitching moment vs. least squares estimated pitch moment
(uncoupled pitch at 0.7 Hz)60
Figure 5.21 Comparison between least squares estimation and neural network prediction
(coupled heave-pitch at 0.5 Hz)60
Figure 5.22 Comparison between least squares estimation and neural network prediction
(coupled heave-pitch at 0.5 Hz)61
Figure 5.23 Comparison between least squares estimate and neural prediction (coupled
heave and pitch at 0.4 Hz with noise)61
Figure 5.24 Comparison between least squares estimate and neural prediction (coupled
heave and pitch at 0.4 Hz with noise)62
Figure 5.25 Modular neural network architecture
Figure 5.26 Plot of sway force vs. training (horizontal circular arc r' = 0.2)65
Figure 5.27 Plot of yaw moment vs. training (horizontal circular arc r' = 0.2)65
Figure 5.28 Plot of roll moment vs. training (horizontal circular arc r' = 0.2)66
Figure 5.29 Plot of pitch moment vs. training (horizontal circular arc r' = 0.2)66
Figure 5.30 Plot of heave force vs. training (horizontal circular arc r' = 0.2)67
Figure 5.31 Neural network training of the sway force (horizontal circular arc r' = 0.2) 67
Figure 5.32 Neural network training of the yaw moment (horizontal circular arc r' = 0.2)

Figure 5.47 Plot of yaw moment vs. training (sway chirp $F= 0.1$ to 0.3 Hz, $V= 500$ mm/s)
Figure 5.48 Plot of roll moment vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)
Figure 5.49 Plot of pitch moment vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500
mm/s)76
Figure 5.50 Plot of heave force vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)
Figure 5.51 Neural network training of the sway force (sway chirp F= 0.1 to 0.3 Hz, V= $$
500 mm/s)77
Figure 5.52 Neural network training of the yaw moment (sway chirp F= 0.1 to 0.3 Hz,
V= 500 mm/s)

Figure 5.58 Plot of roll moment vs. prediction (sway chirp F= 0.1 to 0.3 Hz, V= 250
mm/s)
Figure 5.59 Plot of pitch moment vs. prediction (sway chirp F= 0.1 to 0.3 Hz, V= 250
mm/s)
Figure 5.60 Plot of heave force vs. prediction (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s)
Figure 5.61 Neural network prediction of the sway force (sway chirp F= 0.1 to 0.3 Hz V=
250 mm/s)
Figure 5.62 Neural network prediction of the yaw moment (sway chirp F= 0.1 to 0.3 Hz
V= 250 mm/s)
Figure 5.63 Neural network prediction of the roll moment (sway chirp F= 0.1 to 0.3 Hz $$
V= 250 mm/s)
V= 250 mm/s) .83 Figure 5.64 Neural network prediction of the pitch moment (sway chirp F= 0.1 to 0.3 Hz .84 V= 250 mm/s) .84 Figure 5.65 Neural network prediction of the heave force (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s) .84 Figure 5. 66 Comparison between neural network training and least squares estimate of the sway force (horizontal circular arc r' = 0.2) .85 Figure 5. 67 Comparison between neural network prediction and least squares estimate of
 V= 250 mm/s)
V= 250 mm/s) .83 Figure 5.64 Neural network prediction of the pitch moment (sway chirp F= 0.1 to 0.3 Hz .84 V= 250 mm/s) .84 Figure 5.65 Neural network prediction of the heave force (sway chirp F= 0.1 to 0.3 Hz .84 Figure 5. 66 Comparison between neural network training and least squares estimate of the sway force (horizontal circular arc r' = 0.2) .85 Figure 5. 67 Comparison between neural network prediction and least squares estimate of the sway force (horizontal circular arc r' = 0.1) .85 Figure 5. 68 Comparison between neural network training and least squares estimate of the sway force (horizontal circular arc r' = 0.1) .85

Figure 5. 69 Comparison between neural network prediction and least squares estimate of
the yaw moment (horizontal circular are r' = 0.1)
Figure 5. 70 Comparison between neural network training and least squares estimate of
the roll moment (horizontal circular arc r' = 0.2)
Figure 5. 71 Comparison between neural network prediction and least squares estimate of
the roll moment (horizontal circular arc r' = 0.1)
Figure 5. 72 Comparison between neural network training and least squares estimate of
the pitch moment (horizontal circular arc r' = 0.2)
Figure 5. 73 Comparison between neural network prediction and least squares estimate of
the pitch moment (horizontal circular arc r' = 0.1)

1. INTRODUCTION AND LITERATURE SURVEY

The motion of a submarine is a very complicated process that involves many factors such as the submarine shape and depth of operation. In the early 1940's naval researchers needed to predict the motion of naval submarines in the design stage to evaluate the vehicle's performance and ability to carry out a set of prescribed maneuvers. Numerical simulation techniques were widely used during that time.

Due to the development in naval submarine design, the shape of the vehicle became no longer standard, in addition the type and shape of the hydroplanes that control the motion of the boat changed dramatically from one type to another. These changes introduced new challenges to the process of estimating the hydrodynamic coefficients.

Currently there are three major approaches to investigate the motion of a submarine. These are the theoretical approach, the experimental approach, and the parametric identification approach. Parametric identification methods provide new tools that have been used recently to solve a number of ship motion problems. In this research a new tool for predicting the submarine motion, based on a parametric identification technique, is presented.

1.1. THEORETICAL APPROACH.

Numerous studies to calculate the hydrodynamic coefficients of submarines can be found in the literature. Bohlmann (1990) utilized the three dimensional flow theory to calculate the hydrodynamic coefficients of a submarine in all six degrees of freedom. The study solved the potential flow problem using a singularity distribution and was not limited to slender bodies. Watt (1988) developed an analytical method to estimate the value of the added mass coefficients of the submarine. The method calculates the added mass of the submarine by dividing the submarine into several geometrical components, e.g. sail, tail, fins,..., etc. The added mass was calculated for each component by calculating the added mass for each representative ellipsoid.

Mackay (1988) developed a semi-empirical method for calculating the out-of-plane heave force and pitch moment for a submarine. The method is based on potential flow theory and a first order panel method. The method over-predicts the out-of-plane component due to the absence of the modeling of the cross flow separation in the after-body of the submarine. Mackay and Conway (1990) modeled the cross flow separation by introducing a single doublet sheet along an experimentally determined separation line.

Papoulias and Mckinley (1994) studied the stability of a submarine during its steady state vertical ascent. They considered a free positive ascent case to investigate the response with respect to the stern and the bow plane deflections, excess buoyancy, and relative position between the center of gravity and the center of buoyancy. A nonlinear study of the dynamic stability of a submarine in a dive maneuver was also presented by Papoulias and Papadimitriou (1995). The researchers presented a framework to calculate the critical

2

speed of the vehicle in terms of its metacentric height, the longitudinal separation of the center of gravity and center of buoyancy, and the dive plane angle.

1.2. Experimental Methods

Captive model tests are used to determine the coefficients in the equations of motion of a model. The use of the rotating arm and planar motion mechanism (PMM) allowed the incorporation of some nonlinear terms and time histories effects, see Feldman (1995) and Kalske (1992). Multi-degree-of-freedom test rigs are being used at present to determine these coefficients, see Williams et al. (1999). Experimental methods are expensive to use and their results suffer from scale effects.

An alternative to the captive model tests is the wind tunnel test. Experiments on a deeply submerged submarine model can be conducted. The advantage of this procedure over conventional captive model tests is that in the wind tunnel the duration of the test can be extended to a much longer time than in the case of towing tank experiments. A wind tunnel experiment can also be used for flow visualization and for studying the effects of propulsion on the submarine model hydrodynamics, see Watt et al. (1993).

1.3. Parametric Identification Approach

Parametric identification techniques provide another way for determining the hydrodynamic model of the submarine. Parametric identification approaches use the relation between the input and the output to estimate the hydrodynamic forces and moments while in the experimental approach these forces and moments are measured directly. The method assumes a certain structure for the mathematical model. The coefficients of the mathematical model are then estimated such that the model produces an output which matches the measured output. Artificial neural networks (ANN) have been used for many surface ships as a parametric identifier of the vehicle's hydrodynamics.

Neural networks have been shown to yield robust models for ship motions. Haddara (1995) used the technique to analyze the rolling motion of a ship at sea. He also used neural networks to characterize the ship coupled heave and pitch motions, see Haddara and Xu (1999), and to analyze the free roll decay curve, see Haddara and Hinchey (1995). Hinchey also used this technique to fit ship resistance data for an R-Class icebreaker ship model, see Hinchey (1994), and to predict the loads on sub-sea robots, Rivera and Hinchey (1999). Haddara and Wang (1996) used this technique to identify the coupled sway and yaw motion for a ship undergoing a series of standard maneuvers. Lainiotis and Plataniotis (1994) used an adaptive neural network to predict the current as well as future ship position as a space vector.

Multi-linear regression may not yield accurate estimates. The accuracy of the technique decreases as the number of variables increases. Neural networks have been shown to yield a robust result regardless of the number of variables in the functional relation. However the classical division of force into components which are functions of added masses and damping coefficients is usually lost.

1.4. Scope and Objectives.

The objective of this study was to develop a parametric identification tool for predicting the hydrodynamic forces acting on a submarine model using the model motion history. The proposed tool uses a neural network technique to identify the hydrodynamic forces and moments. Data obtained from multi degree-of-freedom tests were used to train the network.

The fully trained network was then used to generate more maneuvers with a limited computational demand. This will reduce the cost associated with experimental testing of submarine models since only a limited number of maneuvers have to be actually performed to obtain the full hydrodynamic model of the submarine.

1.5. Methodology

A neural network model was developed. Digitally generated data and experimental data were used to train and validate the model. The motion of a submarine undergoing a coupled heave and pitch sinusoidal motion was numerically generated at different frequencies using a Runge-Kutta algorithm. Experimental data were obtained from the Marine Dynamic Test Facility (MDTF). The maneuvers considered were horizontal circular arcs, and sway chirp maneuvers. A three-layer feedforward backpropagation neural network was used for system identification. The network prediction was then compared to a multiple linear regression estimate of the model hydrodynamic forces and moments.

1.6. THESIS OUTLINE

Chapter 2 gives background information about neural networks and their architecture; it also discusses some of the training algorithms. Chapter 3 describes the mathematical formulation of the equations of motions, the neural network algorithm, and the multivariate linear regression. Chapter 4 describes the experimental setup and the neural network approach used. Results obtained using experimental data as well as digitally generated data are included in Chapter 5 while Chapter 6 outlines the conclusions. Some recommendations for future work are stated in chapter 7.

2. NEURAL NETWORKS

Tasks that involve pattern recognition or intelligence are very difficult to automate; such tasks are performed easily by animals in their daily activities. Understanding how the biological neural system works allowed researchers to develop artificial systems that mimic the biological brain in performing a variety of computations and intelligent tasks.

2.1. BIOLOGICAL NEURAL SYSTEMS

A biological neural system consists of a number of neurons; each neuron is composed of a cell body, a tubular axon, and a number of dendrites, see Figure 2.1. Data propagates from the dendrites of one neuron to the other through a gap synapse. The magnitude of the signal received by a neuron depends upon the strength "efficiency" of the synaptic connection between that neuron and the one that is sending the signal. A neuron will fire a signal if its excitation exceeds a critical amount, called the threshold. It will then send that signal along its axon. A signal propagates down the axon and reaches the synapses, sending signals of various strengths to other neurons.



Figure 2.1 Biological neuron

2.2. ARTIFICIAL NEURAL NETWORKS

An Artificial Neural Network (ANN) consists of a number of processing elements (nodes) equivalent to the neurons in biological systems. Synapses are modeled by links between these nodes while the synaptic efficiencies are replaced by weights. Nodes at the same level form a layer. Each ANN consists of an input layer, output layer, and a number of hidden layers. Inputs to each node are summed up and the node then fires an output according to the assigned activation function.

All ANN models proposed so far are based on the following assumptions

1. The position of the node of the incoming connection is irrelevant.

 Each node has a single output value, which is distributed to other nodes via connections irrespective of their position.

 All inputs to the same level come at the same time or remain active long enough for computations to occur, Mehrotra et al (1997).

2.3. ANN SQUASHING FUNCTIONS

Squashing functions can be classified into differentiable and non-differentiable functions. Differentiable and non-differentiable functions can be defined according to the function shape. A differentiable function has a smooth shape and it is needed for some adaptive learning algorithms. A non-differentiable, discontinuous, function gives a true binary output. Discontinuous functions can be used in classification networks.

2.3.1. STEP FUNCTIONS:

A step function is defined as

$$f(net) = \begin{cases} a & \text{if } net < c \\ b & \text{if } net > c \end{cases}$$
 2.1

This function is easy to implement. The net threshold is represented by c, see Figure 2.2, and the function has only two states ON if net > c and OFF otherwise.

The step function is used in class identification where the input belongs to a certain class if its value is greater than a certain value.



Figure 2.2 Step Function

2.3.2. SIGMOID FUNCTIONS:

This is the most commonly used function, also called the S shaped function; the

activation of the node is as follows:

$$f(net) = Z + \frac{1}{1 + e^{-a(net) + b}}$$
2.3

A typical sigmoid function is shown in Figure 2.3. The advantage of such a function is its smoothness.



Figure 2.1 Sigmoid Function

2.3.3. GAUSSIAN FUNCTIONS.

Another continuous function that is used in the ANN is known as the bell shaped function, see Figure 2.2

$$f(net) = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{1}{2} \left(\frac{mt-\mu}{\sigma}\right)^2}$$
 2.4

Such a function requires prior knowledge of certain statistical values such as the mean and the variance of the input, which imposes some limits on its application. The bell shaped function can be used in class identification depending on how close the input is to the mean value μ .



Figure 2.2 Bell shaped function

2.4. Types of Neural Networks:

A single node neural network is insufficient for most practical problems and a multi-node network is normally used. The way those nodes are connected to each other determines how the computational tasks are performed by the network. Neural networks are classified according to their architectural design. This section discusses some of the most popular designs.

2.4.1. LAYERED NETWORK

This type of ANN, also called recurrent neural network, is partitioned into layers. There is no connection between layer k to j if k > j, see Figure 2.3; connections between nodes in the same layer exist except for the input layer.



Figure 2.3 Layered neural network

2.4.2. ACYCLIC NETWORK

This is a subclass of the layered network with no intra-layer connections i.e. no connections between nodes in the same layer. These are simpler nets than the recurrent ones with less computational demands, which make them easy to implement. Figure 2.4 shows an acyclic neural network.



Figure 2.4 Acyclic neural network

2.4.3. FEEDFORWARD NETWORKS

Again this is another subclass of layered networks, where the only connections exist between layer j and k if k = j + 1. These are the most in-use networks and they are described by the number of nodes in each layer. For example, Figure 2.5 shows a 3.2.3.2 feedforward net. In general feedforward networks have one or two hidden layers.

From this point forward only feedforward neural networks with one hidden layer will be considered.



Figure 2.5 Feedforward neural network

2.5. Backpropagation Training Algorithm

The objective of a supervised training algorithm such as the backpropagation algorithm is to minimize the mean square error between the desired output and the network one. To elaborate on this one can consider the framework proposed by Mehrotra et al. (1997).

The input pattern to the network is P. For each input vector x_P there is a desired output

$$\mathbf{d}_{\mathbf{P}}=(d_{\mathbf{P},1}; d_{\mathbf{P},2}; \dots; d_{\mathbf{P},k})$$
 2.5

One would expect some error between the desired output and the network output. The algorithm objective is to manipulate the weights so that this error would be minimal. If the network output is:

$$O_P = (O_{P,1}; O_{P,2};; O_{P,k})$$
 2.6

Then the network error is

$$Error = \sum_{p=1}^{p} Err(\mathbf{o}_{p}, \mathbf{d}_{p})$$
 2.7

The function Err(0₉, d₉) should be a nonnegative function. One way of computing this function is to express

$$Err(\mathbf{o}_{P}, \mathbf{d}_{P}) = (\ell_{P,j})^2$$
 where $\ell_{P,j} = |\mathbf{o}_{P,j} - \mathbf{d}_{P,j}|$

This function is a differentiable function. Moreover it is easy to apply to the backpropagation algorithm since the derivative of the resulting quadratic function is linear and easy to compute.

To discuss the backpropagation in depth one can assume the following case for a three laver network.

Each node receives an input vector of $x_{P,i}$ where 'p' represents the pattern number while 'i' represents the ith node in the layer.

The input to the jth node in the hidden layer is net $\int_{j=0}^{n} \omega_{i,j} x_{p,i}$

The output of the jth node $x_{P,i} = \delta(\text{net }_i)$, where δ is a sigmoid function.

The input to the kth node in the output layer is net $k = \sum_{i} \omega_{k,i} x_{p,i}$

The output of the kth node in the output layer is $O_{P,k} = \delta(net_k)$.

One way to minimize the Mean Square Error (MSE) is to apply the gradient descent method. Since the net output depends on the net weights, the MSE is also a function of the weights w. According to the gradient descent the direction of the weights change is the same as $-\frac{\partial E}{\partial w}$, see Widrow and Lehr (1990). Following this scenario the weight change can be described as follows

$$\Delta \omega_{k,j} \propto \left(-\frac{\partial E}{\partial \omega_{k,j}}\right)$$
 2.8

$$\Delta \omega_{l,i} \propto \left(-\frac{\partial E}{\partial \omega_{l,i}}\right)$$
 2.9

Since the change in the weights results in changing the net output, one can write

$$\frac{\partial E}{\partial \omega_{k,j}} = \frac{\partial E}{\partial o_k} \frac{\partial o_k}{\partial net_k} \frac{\partial net_k}{\partial \omega_{k,j}}$$
2.10

Equation 2.10 can be simplified into

$$\frac{\partial E}{\partial \omega_{k,j}} = -2(d_k - o_k)\delta^{\prime}(net_k)x_j \qquad 2.11$$

Now let us consider the weights between the input and hidden layers.

$$\frac{\partial E}{\partial \omega_{i,j}} = \sum_{k=1}^{k} \frac{\partial E}{\partial o_k} \frac{\partial o_k}{\partial net_k} \frac{\partial net_k}{\partial x_j} \frac{\partial net_j}{\partial net_j} \frac{\partial net_j}{\partial \omega_{i,j}}$$
2.12

$$\frac{\partial E}{\partial \omega_{i,j}} = \sum_{k=1}^{K} \left\{ -2(d_k - o_k)\delta'(net_k)\omega_{k,j}\delta'(net_j)x_i \right\}$$
2.13

The change of weight is then calculated for the weight between the output and hidden layer using the actual error while the change of weight for the lower level is calculated using the weighted sum of errors coming to the hidden node from the output node. The error at a node is calculated in the direction opposite to the propagation of the node output. Applying this analogy to equations 2.11 and 2.13 one can write the change of weight for network training using the pth pattern as:

$$\Delta \omega_{k,j} = \eta \delta_{p,k} x_{p,j} \qquad 2.14$$

$$\Delta \omega_{i,j} = \eta \mu_{p,j} \, x_{p,i} \tag{2.15}$$
where

$$\delta_{p,k} = (d_{p,k} - o_{p,k})^* o_{p,k}^* (1 - o_{p,k})$$
2.16

and

$$\mu_{P,j} = \sum_{k} \delta_{P,j} a_{k,j} * x_{P,j} * (1 - x_{P,j})$$
2.17

Training using equation 2.14 and 2.15 results in the manipulation of the network weights to achieve the optimum weights that result in the minimum error. Weights can be updated after each pattern (training per pattern) or after all the training patterns pass through the net (training per epoch). The criteria for terminating the training and the choice of the suitable training rate "n" depends on the user's experience.

2.6. Momentum Update

Backpropagation leads the neural network error to a certain minimum. There is a chance that this minimum is a local minimum different than the global minimum. The network then will stick to this local condition and the algorithm will prevent the error from decreasing further. One can prevent this by forcing the algorithm to update the weights depending on the average gradient of the MSE of a small region rather than at a certain point. Averaging $\frac{\partial E}{\partial w}$ in a small region allows the algorithm to update the weights in the general direction avoiding local minima.

Averages can be very expensive in calculation. Rumelhart et al. (1986) suggested a shortcut using a momentum term as follows:

$$\Delta \omega_{k,j}(t+1) = \eta \delta_k x_j + \alpha \Delta \omega_{k,j}(t)$$
 2.18

The term α is a momentum term yet its optimum value is not known. With the addition of this term the weight change is influenced by the weight change from the previous step as well as the change suggested by the gradient descent.

The effect of the use of a momentum term in a weight update depends upon the value chosen for α . A well-chosen value can significantly reduce the time needed for training the network. A value of 0 implies that the past step does not affect the current update while a value closer to 1 suggests that the current error does not affect the training. Since the weight update in this algorithm depends upon the direction of the previous weight update, the direction chosen in an early stage of the training procedure can strongly bias future weight updates and can restrict the network to a certain region preventing the algorithm from exploring other regions.

3. MATHEMATICAL FORMULATION

3.1. Equations of Motion

The equations describing submarine motion can be obtained using Newton's second law.

$$MX = F$$
 3.1A

where M is the mass matrix and X and F are the displacement and the force vectors respectively.

One can expand on equation 3.1A to describe the motion of an underwater vehicle as:

$$(I + A)\dot{x} = F(x) + X(x) + S(x)$$
 3.1B

where x is the extended state vector containing the vehicle's translation and rotational velocities, Euler angle displacements, and control deflections, see Figure 3.1. I is a matrix representing the inertial properties of the vehicle, A is the added mass matrix, F is the hydrodynamic force vector, X represents the force vector arising from axis rotation, buoyancy, gravity, and, propulsion, and S represents other external force vectors.

For small amplitude motion of a submarine model attached to a forced motion testing rig with port - starboard symmetry, and using the coordinate system shown in Figure 3.1, equation 3.1B can be expressed in a component form as:

$$\ddot{x}_3 + b_{33}\dot{x}_3 + b_{35}\dot{x}_5 + c_{35}x_5 = F_{30}\sin(\omega t)$$
 3.2

$$\ddot{x}_{s} + b_{ss}\dot{x}_{s} + b_{ss}\dot{x}_{s} + c_{ss}x_{s} = F_{ss}\sin(\omega x)$$
3.3

where x_3 and x_5 are the heave and pitch displacements respectively, \dot{x}_1 and \ddot{x}_2 are the first and second derivative of the displacement, F_{30} and F_{50} are the heave force and pitch moment amplitudes, ω is the exciting frequency, and t is time.



Figure 3.1 Model coordinates system

The hydrodynamic coefficients b_{ij} , where i, j = 3, 5, represent the submarine damping coefficients. The coefficients c_{ij} are the pitch restoring coefficients which act to return the submarine to the position of vertical equilibrium. The right hand sides of equations 3.2 and 3.3 represent the heave force and pitch moment that are imposed on the submarine model by the forced-motion apparatus as the submarine follows the path. For

the validation of the proposed technique a generic submarine with the following arbitrary hydrodynamic coefficients was used to generate the numerical motion data.

b33	b35	b55	b53	C55	C35	F ₃₀	F50
0.234	0.158	0.222	0.58	30.78	0.238	3	2

Table 3.1 Numerical model coefficients

Equations 3.2 and 3.3 were solved numerically using a Runge-Kutta algorithm to obtain the time series of the heave and pitch displacements, velocities, and accelerations.

3.2. NEURAL NETWORK MODEL

The neural network model used in this study consists of an input layer, hidden layer, and an output layer. Figure 3.2 shows the details of the neural network structure.

The input to the jth node in the hidden layer consists of the weighted sum of the ith components in the input vector:

$$M_j = \sum_{i=1}^{6} w_{ij}h_i \qquad 3.6$$

where w_{ij} is the weight between the ith node in the input layer and the jth node in the hidden layer, $h_1 = \dot{x}_3$, $h_2 = \ddot{x}_3$, $h_3 = \dot{x}_3$, $h_4 = \ddot{x}_3$, $h_5 = x_5$, and $h_6 = 1$. The input to the jth node in the hidden layer is transformed via a squashing function as:

$$G(M_i) = \frac{1}{1 + e^{-M_i}}$$
 3.7



Figure 3.2 Neural network structure

The output of the kth node in the output layer is given as:

$$f^{(k)} = \sum_{j=1}^{16} \lambda^{(K)} \ j \ G(M_j)$$
3.8

where k is either 3 or 5, and $\lambda^{(n)}_{j}$ is the network weight between the jth node in the hidden layer and the kth node in the output layer.

3.3. LINEAR REGRESSION MODEL

Multiple linear regression is often called "model fitting". It depends upon the assumption of a mathematical model that fits the data at hand. The adequacy of the technique depends upon the accuracy of the assumed model.

Considering the model described in Equation 3.9 there are k regressors and i is the number of observations, i = 1, 2, ..., n.

$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_k x_{ik} + \varepsilon_i \qquad 3.9$$

$$y_i = \beta_0 + \sum_{j=1}^k \beta_j x_{ij} + \varepsilon_i \qquad 3.10$$

One can express equation 3.10 in a matrix form as

$$y = X\beta + \varepsilon$$
 3.11

where

$$\mathbf{y} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}, \quad \mathbf{X} = \begin{bmatrix} 1 & x_{11} & x_{12} & \cdots & x_{14} \\ 1 & x_{21} & x_{22} & \cdots & x_{24} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & x_{n1} & x_{n2} & \cdots & x_{n4} \end{bmatrix}, \quad \boldsymbol{\beta} = \begin{bmatrix} \boldsymbol{\beta}_0 \\ \boldsymbol{\beta}_1 \\ \vdots \\ \boldsymbol{\beta}_n \end{bmatrix}$$

and $\boldsymbol{\varepsilon} = \begin{bmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \vdots \\ \varepsilon_n \end{bmatrix}$

The least squares method determines the value of the parameters β_k so that the sum of the squares of the error is minimized. The least squares function is

$$L = \sum_{i=1}^{n} \varepsilon_i^{2i} = \varepsilon' \varepsilon = (\mathbf{y} - \mathbf{X}\boldsymbol{\beta})'(\mathbf{y} - \mathbf{X}\boldsymbol{\beta})$$
 3.12

equation 3.12 can be rewritten as

$$L = \mathbf{y}'\mathbf{y} - 2\mathbf{\beta}'\mathbf{X}'\mathbf{y} + \mathbf{\beta}'\mathbf{X}'\mathbf{X}\mathbf{\beta}$$
 3.13

in order for the function L to be minimized with respect to β , the least squares estimator

 $\hat{\boldsymbol{\beta}}$ must satisfy.

$$\frac{\partial L}{\partial \beta}\Big|_{\hat{\beta}} = -2\mathbf{X}'\mathbf{y} + 2\mathbf{X}'\mathbf{X}\hat{\beta} = 0 \qquad 3.14$$

From equation 3.14 the least squares estimator is

$$\hat{\boldsymbol{\beta}} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{y} \qquad 3.15$$

Montgomery (1997) presented this framework of least squares as an unbiased estimator of the parameter β in the linear regression model.

3.3.1. UNCOUPLED HEAVE MODEL

Given n points, the linear regression model for the uncoupled heave force estimate is.

$$F_i = \beta_0 + \beta_1 \dot{x}_i + \beta_2 \ddot{x}_i$$
 $i = 1, 2, 3, ..., n$ 3.16

3.3.2. UNCOUPLED PITCH MODEL

Using the least squares method the pitch moment is assumed to follow the mathematical model shown:

$$F_i = \beta_0 + \beta_1 x_i + \beta_2 \dot{x}_i + \beta_3 \ddot{x}_i$$
 i=1.2,...,n 3.17

3.3.3. COUPLED HEAVE AND PITCH MODEL

The coupled heave and pitch digitally generated motion can be expressed in the following linear equations:

$$F_{3i} = \beta_{03} + \beta_{31} \dot{x}_{3i} + \beta_{32} \ddot{x}_{3i} + \beta_{33} x_{5i} + \beta_{34} \dot{x}_{5i}$$
 3.18

$$F_{5i} = \beta_{05} + \beta_{51} \dot{x}_{3i} + \beta_{52} x_{5i} + \beta_{53} \dot{x}_{5i} + \beta_{54} \ddot{x}_{5i} \qquad i=1,2,...,n \qquad 3.19$$

Rearranging equations 3.23 and 3.24 into matrix form yields:

$$\mathbf{F}_3 = \mathbf{X}_3 \mathbf{\beta}_3 \tag{3.20}$$

$$\mathbf{F}_{5} = \mathbf{X}_{5}\mathbf{\beta}_{5}$$
 3.21

where

$$\boldsymbol{\beta}_{n} = \begin{bmatrix} \boldsymbol{\beta}_{n} \\ \boldsymbol{\beta}_{n} \\ \boldsymbol{\beta}_{n2} \\ \boldsymbol{\beta}_{n3} \\ \boldsymbol{\beta}_{n4} \end{bmatrix}$$
 3.22

$$\mathbf{X}_{3} = \begin{bmatrix} 1 & \dot{x}_{31} & \ddot{x}_{31} & \dot{x}_{31} & \dot{x}_{31} \\ 1 & \dot{x}_{32} & \ddot{x}_{32} & \dot{x}_{32} & \dot{x}_{32} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & \dot{x}_{3*} & \ddot{x}_{3*} & \ddot{x}_{3*} & \dot{x}_{5*} \end{bmatrix}$$
3.23

and

$$\mathbf{X}_{5} = \begin{bmatrix} 1 & \dot{x}_{31} & x_{31} & \dot{x}_{31} & \ddot{x}_{31} \\ 1 & \dot{x}_{32} & x_{32} & \dot{x}_{32} & \ddot{x}_{32} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & \dot{x}_{3s} & x_{3s} & \dot{x}_{5s} & \ddot{x}_{5s} \end{bmatrix}$$

$$3.24$$

Results obtained from the neural network technique and the linear regression calculations are shown in Chapter 5. Least squares calculations are shown in Appendix A.

4. FRESH WATER TOWING TANK EXPERIMENTS

4.1. MARINE DYNAMIC TEST FACILITY (MDTF)

The MDTF is a multi-degree-of-freedom forced-motion test rig. It has the capability of forcing the test model in an arbitrary motion trajectory, within the rig and the towing tank limits. The motion parameters as well as the forces acting on the model are measured. The MDTF is part of the testing facilities at the Institute for Marine Dynamics (IMD). The MDTF was commissioned in early 1999 after its performance had been evaluated through a prototype rig (1993 to 1996).

During the period from October to December 1999 maneuvers were conducted using a standard submarine model. The MDTF description, experiment setup, and the maneuvers performed will be briefly presented in the following sections.

4.1.1. MDTF SETUP

The general arrangement of the MDTF with the model mounted on it, is shown in Figure 4.1. The whole configuration is mounted on the carriage of the towing tank with the model deeply submerged. The MDTF rig consists of two lateral railed carriages supporting two vertical telescopic struts: a picture of the sub-carriage is shown in Figure 4.2. Two lateral servomotors, shown in Figure 4.3, drive the lateral struts sideways parallel to the carriage transverse centerline while two other servomotors, Figure 4.4, drive the telescopic struts in the vertical direction. A universal joint, see Figure 4.5, connects the sting to the struts. The sting is connected to the model via a six component internal balance. The six components of the reaction loads were measured at the model balance-resolving center (BRC). For detailed information on the MDTF and its setup see Williams et al. (1999).



Figure 4.1 MDTF General Arrangement



Figure 4.2 MDTF Sub-Carriage



Figure 4.3 Lateral Motor Arrangement



Figure 4.4 Vertical Motor Arrangement



Figure 4.5 Forward Strut Universal Joint

4.1.2. EXPERIMENTAL SETUP

The model, IMD 497 Standard submarine model, was 4.445 m in length and 0.5 m in diameter at the mid-body. The BRC is located 5.453 m from the aft strut. The forward and afterward struts are 2 m apart. Model dimensions and coordinate system are shown in Figure 4.1 to Figure 4.8. The model displacements were calculated from the strut displacements as shown in equations 4.1 to 4.4.





Figure 4.1 DREA Standard submarine model dimensions



Figure 4.7 Side view of the MDTF setup



Figure 4.8 Top view of the MDTF setup

$$Z_{BBC} = Z_{H^{0}} - \left(\left[\frac{a+b}{b} \right] [Z_{H^{0}} - Z_{He}] \right)$$

$$4.1$$

$$\theta = \sin^{-1}\left(\frac{[z_{ab} - z_{bad}]}{b}\right)$$
 4.2

$$y_{BRC} = y_{ab} + \left(\left[\frac{a+b}{b} \right] \left[y_{bed} - y_{ab} \right] \right)$$

$$4.3$$

$$\psi = \sin^{-1} \left(\frac{\left[y_{\text{twid}} - y_{\text{twid}} \right]}{b} \right)$$
4.4

The above equations are based on a "rigid" sting assumption and they describe the model displacements relative to a set of axes which are fixed to the towing carriage but which translate longitudinally relative to a fixed earth reference point.

4.2. MANEUVERS

The design of the MDTF allows the model to perform non-conventional maneuvers. The maneuvers that have been conducted can be divided into four categories. These are described as follows:

4.2.1. CIRCULAR ARC MANEUVERS.

In these maneuvers the model is forced to move in a series of arcs separated by transition regions. The model has a constant speed, u, and a constant pitch rate, q, during the vertical arc maneuvers and constant yaw rate, r, during the horizontal arc maneuvers. Heave and sway displacements may have nonzero values. The arcs have a non-dimensional turning rate, t', defined as.

$$t' = L/R$$
 4.5

where L is the model length, R is the turning radius. $R = \frac{u}{r}$ in the horizontal plane and

 $R = \frac{u}{q}$ in the vertical maneuvers. t' represents the non-dimensional turning rate (r' in the horizontal plane and q' in the vertical plane). Figure 4.9 shows a plot of the aft strut displacement, forward strut displacement, and model trajectory for an arc maneuver in the horizontal plane.

4.2.2. LINEAR CHIRP MANEUVERS

Chirps are harmonic maneuvers with constant amplitude and varying frequency. The frequency ranged from 0.1 up to 0.5 Hz. These frequencies were swept in the form of low-high-low sawtooth shape. Figure 4.10 shows a chirp maneuver in the vertical plane.



Figure 4.9 Arc maneuver trajectory in the lateral plane r' = 0.2



Figure 4.10 Pure heave chirp, frequencies 0.1 to 0.5 Hz

4.2.3. PURE HARMONICS

A series of harmonic runs were performed during the testing period. The frequency ranged from 0.15 to 0.25 Hz with amplitude range of 0.07 to 0.4 m.

4.2.4. MULTI-DEGREE-OF-FREEDOM MANEUVERS

A limited number of maneuvers were tried with the model moving in three, four, and five degrees of freedom; most of these were chirps. During the testing period a set of nonconventional maneuvers such as cone helical maneuvers were also tried. More information on these can be found in Williams et al (1999).

The above mentioned maneuvers were performed with four different configurations of the submarine. These configurations, shown in Figure 4.11, were bare hull sub; hull and sail; hull and tail; and hull sail and tail (full configuration). A list of all maneuvers performed is given in Appendix C.



Figure 4.11 Model configurations

4.3. Data Acquisition

Data from load cells, accelerometers, and potentiometers were sampled at 50 points/sec frequency. The GEDAP[®] software stored all measured time series in binary format. A split routine was then used to split each run file into separate run channels and preliminary statistical calculations and corrections were performed. An export routine was then applied to transfer the run at hand to ASCII format. The exported file had the format shown in Table 4. 1.

4.3.1. TIME TARE AND COORDINATES TRANSFORMATION

During testing, data collection started before the actual maneuver started, moreover the maneuvers started some time before the carriage reached its constant speed. Time before the steady speed is considered tare time and all data collected during that time segment had to be removed.

The six force components were measured at the model BRC located at 5.453 m from the aft strut. A simple transformation of the struts displacements, based on equations 4.1 to 4.4 and assuming a rigid sting, was needed to obtain the model linear and rotational displacements at the BRC.

Column #	GEDAP Channel #	Variable	Units
1	Implicit Variable	Time	sec
2	ch.031	Carriage speed	m/s
3	ch-sname.001	Fx	N
4	ch-sname.002	Fy	N
5	ch-sname.003	Fz	N
6	ch-sname.004	Mx	N-m
7	ch-sname.005	Му	N-m
8	ch-sname.006	Mz	N-m
9	ch.022	FV. Pos.	m
10	ch.024	AV Pos.	m
11	ch.026	FL Pos.	m
12	ch.028	AL Pos.	m
13	ch.007	Fwd. Ax	g
14	ch.008	Fwd Ay	g
15	ch.009	Fwd Az	g
16	ch.010	Aft Ax	g
17	ch.011	Aft Ay	g
18	ch.012	Aft Az	g

Table 4. 1 ASCII file format "HST_xxxxx. asc"

MDTF Prepshop is a Windows application written by the author to perform the above mentioned steps, tare removal and coordinate transformation. It allows the user, through a graphic interface, to select the ASCII run file, the time segment, and the output file name. The program will then run the scenario mentioned earlier. The program also calculates the model's heave, pitch, yaw, and sway rates at the BRC. Prepshop was written in Visual Basic[®] 6 and its code is shown in Appendix D.

4.4. Filtering

The data were then filtered using the Matlab[®] Wavelet toolbox. A wavelet filter allows the use of a variable-sized windowing technique where a long time interval is used when

we want more precise low frequency information and shorter interval where high frequency information is needed.

4.4.1. WHAT IS A WAVELET ?

A wavelet is a waveform with a limited duration that has a zero average value. While Fourier analysis breaks the signal into sine waves with different frequencies, wavelet analysis breaks the signal into shifted and scaled versions of the original wavelet. A continuous wavelet is the sum over time of the original signal multiplied by a scaled,

shifted version of the chosen wavelet function ϕ .

$$C(scale, shift) = \int f(t)\varphi(scale, shift)dt$$
 4.6

Equation 4.6 results in many wavelet coefficients C. These coefficients are a function of the shift and scale of the function.

Matlab[®]decomposes the wavelet signal into two components, a high frequency and a low frequency component, by removing the high frequency component. Each wavelet performs a single level filtering. To obtain a smoother signal the filtering process can be repeated a number of times on the low frequency component. This is called multilevel decomposition. Matlab[®] includes a number of wavelet families, see the Wavelet Toolbox user guide (1997).

4.4.2. FILTERING PROCEDURE

The wavelet used in these runs was a Daubechies 'db5' with a decomposition level 6. This filter worked fairly well in eliminating most of the noise of the signal while preserving the general form of the data. The filtering script, which is called *clean.m*, is a Matlab M-file that reads all the channels from the Prepshop file; filters them, then exports the output to a *filename*.flt file. The procedure is to split the file into individual channels and perform the following steps.

1- Decompose the signal using Daubechies wavelets with six levels and calculate the scale and position.

2- Determine the default values for de-noising the signal.

3- De-noise and compress the signal using a global positive threshold.

The filtering script *clean.m* as well as a number of selected runs with filtering are shown in Appendix E.

4.5. Neural Network Approach

Tow different neural networks were used to describe the horizontal and the vertical maneuvers. In the case of horizontal maneuvers the input consisted of the sway velocity, \dot{x}_2 , the sway displacement, x_2 , the yaw rate, \dot{x}_6 , and the yaw angle, x_6 . The input to the jth node in the hidden layer, M_{in} is given by:

$$M_{I} = \sum_{i=1}^{5} w_{ij} h_{i}$$

where , $h_1 = \dot{x}_2$, $h_2 = x_2$, $h_3 = \dot{x}_6$, $h_4 = x_6$, $h_5 = 1$.

45

The output from the jth node in the hidden layer, G (M_i) is given by

$$G(M_i) = \frac{1}{1 + e^{-M_i}} \qquad j = 1, 2, \dots, 17 \qquad 4.8$$

finally, the network output, F^(k), is given by.

$$F^{(k)} = \sum_{j=1}^{18} \lambda^{(k)} G(M_j) \qquad k=2,3,4,5,6 \qquad 4.9$$

In the vertical plane there would be no out of plane forces and moment. The reason for that is the sub is symmetrical around the vertical axis and asymmetrical around the horizontal axis. The presence of the sail in the horizontal plane, see Mackay (1988), Mackay and Conway (1990 and 1991), while the sub is turning, produces a drift angle, which results in a positive heave force on the after body of the sub and a positive pitch moment at the nose which attempts to lift the nose up.

After some preliminary trials it has been found that a three-layer feedforward net with 15 hidden nodes would be sufficient in the case of predicting the forces in the arc maneuver. On the other hand more hidden processing elements, namely 17 nodes, were needed to obtain the relation in the case of chirp maneuvers.

5. RESULTS AND DISCUSSION

5.1.1. UNCOUPLED HEAVE MOTION GENERATION

The equation of uncoupled heave motion for the model can be written as follows.

 x₃₁ + b₃₁x₃₂ = F₃₀sin(ax.)
 5.1

 Using this equation, 20 time histories were generated at the frequencies: 0.5, 0.6, 0.7, ...,
 2.4 Hz. The heave force is plotted as a function of the displacement, velocity, and

 acceleration for different frequencies. The results are shown in Figure 5.1 to Figure 5.6



Figure 5.1 Hydrodynamic force vs. acceleration at 0.5 Hz uncoupled heave



Figure 5.2 Hydrodynamic force vs. velocity at 0.5 Hz uncoupled heave



Figure 5.3 Hydrodynamic force vs. displacement at 0.5 Hz uncoupled heave



Figure 5.4 Hydrodynamic force vs. acceleration at 1.5 Hz uncoupled heave



Figure 5.5 Hydrodynamic force vs. velocity at 1.5 Hz uncoupled heave



Figure 5.6 Hydrodynamic force vs. displacement at 1.5 Hz uncoupled heave

5.1.2. UNCOUPLED PITCH MOTION GENERATION

As in uncoupled heave, the equation of motion for a submarine model undergoing pitch motion can be written as follows

$$\ddot{x}_{5i} + b_{55}\dot{x}_{5i} + c_{55}x_{5i} = F_{5o}\sin(\omega t_i)$$
5.2

The model motions were generated at frequencies of 0.5, 0.6, 0.7,..., 2.4 Hz. The pitch moment is plotted as a function the motion. Plots are shown in Figure 5.7 Pitch moment vs. acceleration at 0.5 Hz uncoupled pitch to Figure 5.12.



Figure 5.7 Pitch moment vs. acceleration at 0.5 Hz uncoupled pitch



Figure 5.8 Pitch moment vs. velocity at 0.5 Hz uncoupled pitch



Figure 5.9 Pitch moment vs. displacement at 0.5 Hz uncoupled pitch



Figure 5.10 Pitch moment vs. acceleration at 1.5 Hz uncoupled pitch

25 -



Figure 5.11 Pitch moment vs. velocity at 1.5 Hz uncoupled pitch


Figure 5.12 Pitch moment vs. displacement at 1.5 Hz uncoupled pitch

5.1.3. COUPLED HEAVE AND PITCH MOTION

Uncoupled heave and uncoupled pitch motions are theoretical motions. In this section the more realistic coupled motion will be considered. The motion for the same generic submarine model was generated undergoing regular coupled heave and pitch. The model motion is described by equations 3.2 and 3.3.

As in the previous sections these equations can be solved using a Runge-Kutta method. Simulated data were obtained for 0.5, 0.6,....., 2.0 Hz for the coupled motion. The displacement, velocity, and acceleration time series were obtained at these frequencies. To validate the proposed technique the numerically generated force was compared to the predicted and least square estimated force.

5.1.4. EFFECTS OF RANDOM NOISE

Direct measured values, experimental values, often contain a noise component either from instrumental errors or mechanical noise from the experimental apparatus. In the following section the coupled heave pitch motion is generated as in the previous section but with the addition of a 20 % random noise term to the motion displacement, velocity and acceleration.

The motion of the submarine was modeled using equations 3.2 and 3.3. Applying the same procedures as before the numerically generated data were obtained for the same range of frequencies. The random noise was then added to the time series.

The reason for adding the noise after the time series has been generated is that the noise simulated here was due to instrumentation errors. Once again the generated hydrodynamic force and moment force were compared to the estimated force from the least squares method and the predicted one using a neural network.

5.2. RESULTS FROM DIGITALLY GENERATED DATA

Figure 5.13 and Figure 5.14 show a comparison between a least squares estimate and a neural network prediction for the heave force for the uncoupled heave case. Figure 5.15 shows a plot of actual force vs. the neural predicted force (uncoupled heave at 0.7 Hz) while Figure 5.20 is a plot of actual pitching moment vs. least squares estimated pitch moment (uncoupled pitch at 0.7 Hz). Figure 5.17 and Figure 5.18 show the comparison between a least squares estimate and a neural network prediction of the pitch moment for the uncoupled pitch motion. Figure 5.19 is a plot of actual pitching moment vs. a neural predicted pitch moment (uncoupled pitch at 0.7 Hz). Figure 5.17 and Figure 5.19 is a plot of actual pitching moment vs. a neural predicted pitch moment (uncoupled pitch at 0.7 Hz). 5.20 is a plot of actual pitching moment vs. a least squares estimated pitch moment (uncoupled pitch at 0.7 Hz).

Figure 5.21 and Figure 5.22 show a comparison between a least squares estimate and a neural network prediction of the coupled heave-pitch motion. The effect of randomly generated noise on the least squares and the neural prediction is show in Figure 5.23 and Figure 5.24.



Figure 5.13 Comparison between least square estimation and neural net prediction (uncoupled heave at 0.6 Hz)



Figure 5.14 Comparison between least square estimate and neural net prediction (uncoupled heave at 1.5 Hz)



Figure 5.15 Plot of actual force vs. neural predicted force (uncoupled heave at 0.7 Hz)



Figure 5.16 Plot of actual force vs. least squares estimated force (uncoupled heave at 0.7 Hz)



Figure 5.17 Comparison between least square estimation and neural network prediction (uncoupled pitch at 0.7 Hz)



Figure 5.18 Comparison between least square estimation and neural network prediction (uncoupled pitch at 1.2 Hz)



Figure 5.19 Plot of actual pitching moment vs. neural predicted pitch moment (uncoupled pitch at 0.7 Hz)



Figure 5.20 Plot of actual pitching moment vs. least squares estimated pitch moment (uncoupled pitch at 0.7 Hz)



Figure 5.21 Comparison between least squares estimation and neural network prediction (coupled heave-pitch at 0.5 Hz).



Figure 5.22 Comparison between least squares estimation and neural network prediction (coupled heave-pitch at 0.5 Hz)



Figure 5.23 Comparison between least squares estimate and neural prediction (coupled heave and pitch at 0.4 Hz with noise)



Figure 5.24 Comparison between least squares estimate and neural prediction (coupled heave and pitch at 0.4 Hz with noise)

5.3. RESULTS FROM EXPERIMENTAL DATA

A number of neural networks were trained to identify the hydrodynamic forces acting on the submarine model during different types of maneuvers. Two of the categories described in section 4.2 and the model in its full configuration were considered. The two maneuvers were the horizontal circular arc and sway chirp maneuver.

A single run from each maneuver was used in training. The number of data points used in the training process was enormous. 2501 x 4 data points were used in training the chirp networks and 1920 x 4 data points were used in training the circular arc networks. After a number of preliminary trials the author found that training the network in a modular architecture gives better results. Each module has three layers and 15 hidden nodes in the case of the arc maneuvers

and 17 hidden nodes in the chirp maneuvers. Figure 5.25 shows the proposed network architecture. The network consists of small modules each module was trained separately then the final net was then assembled.

Figure 5.26 to Figure 5.30 show plots of the hydrodynamic loads computed by the net vs. the actual component measured for the training data set. The deviation around the diagonal line represents the network error. Figure 5.31 to Figure 5.35 show the same results in a different way. In these set of plots the neural network training and the actual force were plotted vs. time. The network was trained with the horizontal circular arc r' =0.2, and β =0.0 file name "HST_SV2000H_001.DAC; 1".

Figure 5.36 through Figure 5.45 show the same results described above for the trained network applied to a new data file. The run chosen to apply the net to was a horizontal circular arc r' = 0.1, and $\beta=0.0$ file name "HST_SVA1000H_001.DAC; 1".

The sway chirp network was trained using sway run "HST_F1t3V500S_001.DAC;1" where the sway frequency ranged from 0.1 to 0.3 Hz with strut velocity 500 mm/sec and sway amplitude of 1.85 m. Figure 5.46 to Figure 5.50 show plots of the neural training verses the actual hydrodynamic loads on the model while Figure 5.51 to Figure 5.55 show the same training results and actual hydrodynamic loads plotted in a time series format.

Figure 5.57 to Figure 5.73 show a comparison between results obtained by neural networks and multi-linear regression for the circular arc maneuvers.



Figure 5.25 Modular neural network architecture



Figure 5.26 Plot of sway force vs. training (horizontal circular arc r' = 0.2)



Figure 5.27 Plot of yaw moment vs. training (horizontal circular arc r' = 0.2)

65



Figure 5.28 Plot of roll moment vs. training (horizontal circular arc r' = 0.2)



Figure 5.29 Plot of pitch moment vs. training (horizontal circular arc r' = 0.2)



Figure 5.30 Plot of heave force vs. training (horizontal circular arc r' = 0.2)



Figure 5.31 Neural network training of the sway force (horizontal circular arc r' = 0.2)



Figure 5.32 Neural network training of the yaw moment (horizontal circular arc r' = 0.2)



Figure 5.33 Neural network training of the roll moment (horizontal circular arc r' = 0.2)



Figure 5.34 Neural network training of the pitch moment (horizontal circular arc r' = 0.2)



Figure 5.35 Neural network training of the heave force (horizontal circular arc r' = 0.2)



Figure 5.36 Plot of sway force vs. prediction (horizontal circular arc r' = 0.1)



Figure 5.37 Plot of yaw moment vs. prediction (horizontal circular arc r' = 0.1)



Figure 5.38 Plot of roll moment vs. prediction (horizontal circular arc r' = 0.1)



Figure 5.39 Plot of pitch moment vs. prediction (horizontal circular arc r' = 0.1)



Figure 5.40 Plot of heave force vs. prediction (horizontal circular arc r' = 0.1)



Figure 5.41 Neural network prediction of the sway force (horizontal circular arc r' = 0.1)



Figure 5.42 Neural network prediction of the yaw moment (horizontal circular arc r' = 0.1)



Figure 5.43 Neural network prediction of the roll moment (horizontal circular arc r' = 0.1)



Figure 5.44 Neural network prediction of the pitch moment (horizontal circular arc r' = 0.1)



Figure 5.45 Neural network prediction of the heave force (horizontal circular arc r' = 0.1)



Figure 5.46 Plot of sway force vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.47 Plot of yaw moment vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.48 Plot of roll moment vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.49 Plot of pitch moment vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.50 Plot of heave force vs. training (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.51 Neural network training of the sway force (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.52 Neural network training of the yaw moment (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.53 Neural network training of the roll moment (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.54 Neural network training of the pitch moment (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.55 Neural network training of the heave force (sway chirp F= 0.1 to 0.3 Hz, V= 500 mm/s)



Figure 5.56 Plot of sway force vs. prediction (sway chirp F= 0.1 to 0.3 Hz, V= 250 mm/s)



Figure 5.57 Plot of yaw moment vs. prediction (sway chirp F= 0.1 to 0.3 Hz, V= 250 mm/s)



Figure 5.58 Plot of roll moment vs. prediction (sway chirp F= 0.1 to 0.3 Hz, V= 250 mm/s)



Figure 5.59 Plot of pitch moment vs. prediction (sway chirp F= 0.1 to 0.3 Hz, V= 250 mm/s)



Figure 5.60 Plot of heave force vs. prediction (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s)



Figure 5.61 Neural network prediction of the sway force (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s)



Figure 5.62 Neural network prediction of the yaw moment (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s)



Figure 5.63 Neural network prediction of the roll moment (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s)



Figure 5.64 Neural network prediction of the pitch moment (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s)



Figure 5.65 Neural network prediction of the heave force (sway chirp F= 0.1 to 0.3 Hz V= 250 mm/s)



Figure 5. 66 Comparison between neural network training and least squares estimate of the sway force (horizontal circular arc r' = 0.2)



Figure 5. 67 Comparison between neural network prediction and least squares estimate of the sway force (horizontal circular arc r' = 0.1)



Figure 5. 68 Comparison between neural network training and least squares estimate of the yaw moment (horizontal circular arc r' = 0.2)



Figure 5. 69 Comparison between neural network prediction and least squares estimate of the yaw moment (horizontal circular arc r' = 0.1)



Figure 5. 70 Comparison between neural network training and least squares estimate of the roll moment (horizontal circular arc r' = 0.2)



Figure 5. 71 Comparison between neural network prediction and least squares estimate of the roll moment (horizontal circular arc r' = 0.1)



Figure 5. 72 Comparison between neural network training and least squares estimate of the pitch moment (horizontal circular arc r' = 0.2)



Figure 5. 73 Comparison between neural network prediction and least squares estimate of the pitch moment (horizontal circular arc r' = 0.1)

5.4. Discussion

Module	Heave	Sway	Yaw	Roll	Pitch
Training events	240768	403788	87780	135432	393756
Training epochs	95	160	34	53	156
Training time, min.	89	154	132	50	148

The horizontal arc network consisted of five modules. Table 5.1 shows the training criteria for the network.

Table 5. 1 Training criteria for horizontal circular arc network

From Figures 5.31 and 5.41 it can been seen that the neural network prediction for the sway force work fairly well. Moreover the network prediction from the steady state segment of the arc is shown to be of a constant value which agrees with the fact that the model is turning with a constant yaw rate. On the other hand the fluctuation on the actual (measured by MDTF) force is due to model vibration and rocking. The same discussion is valid for the rest of the hydrodynamics components. In the case of out of plane force and moment, Figures 5.43, 5.44 and 5.45, the network slightly over-predicts the steady state force.

The sway chirp maneuvers network has the same architecture as the horizontal arc network. The training criteria for the sway network are shown in Table 5.2. The prediction of the " in plane " components was good but once again the network slightly over-predicts the out-of-plane components. It is notable to say at this point that the-out-of plane components were very small in this case since it is a pure sway maneuver. The author feels that the presence of these forces, heave and pitch, in the sway chirp maneuver was mainly due to the flexibility of the sting and resulting model vibration. A
closer look at the strut displacements showed that there was a 0.2 to 0.5 degree yaw angle which might have been enlarged by the sting flexibility and resulted in the shown forces. Changing the architecture of the net reduced the training time significantly. Moreover the net can be disassembled and one of the modules can be retrained and assembled into the net. This gives a great advantage to this architecture.

Module	Heave	Sway	Yaw	Roll	Pitch
Training events	14385189	5622810	5802900	2187093	11515755
Training epochs	7188	2809	2899	1092	5754
Training time, min.	104	40	42	19	87

Table 5. 2 Training criteria for sway chirp network

Neuroshell[®] 2, a commercial software available from Ward Inc., was used in building the modules. The network was then exported to Visual Basic code and a Windows[®] version of the net was assembled together. A C $\stackrel{\leftrightarrow}{\rightarrow}$ code can also be exported to be included with some other code that can be run in any environment (i.e. Unix, VAX, Windows).

6. CONCLUSIONS

In this work a new tool for predicting the hydrodynamic model for a submarine was presented. A neural network technique was used to predict the hydrodynamic forces acting on the submarine. The approach was validated using digitally generated data for coupled heave and pitch motions as well as experimental, see Figures 5.12 to Figure 5.24, data for circular arc maneuvers and sway chirp maneuvers, Figures 5.31 to Figure 5.65.

The motion time series was numerically generated and both neural network predictions and least squares estimates were obtained and compared to the actual force. Results indicate that both the least squares method and the neural technique can provide accurate predictions for the hydrodynamic forces and moments as long as the data are not contaminated with noise. The neural network approach is shown to be superior to the least squares method when there is noise in the data. The network maximum error when applied to the noisy data was 2.67 % while the least squares produced 8.067 % error.

In section 5.3, the tool was used to predict the hydrodynamics of a submarine model undergoing certain maneuvers. The maneuvers considered were horizontal arc maneuvers and sway chirp maneuvers. A single run from each maneuver was used to train the network. The fully trained networks were then used to predict the hydrodynamic forces acting on the model at different conditions. For both maneuvers the force and moment prediction agree fairly well with the original measurement although there were some cases where the network over predicted the force. During the experimental tests visual observation showed that there were some vibrations in the model as it followed the desired trajectory and in some cases the vibration exceeded the MDTF limitation and the maneuvers were terminated by the control loop. We feel that this vibration affected the measured forces and since the motion history used for training the network were taken from the MDTF struts motion, the relation between the force and the motion changed to some extent. Filtering was used to eliminate the effect of noise on the data.

A comparison between the neural network and the least squares estimate is also shown in Section 5.3. The comparison showed that the neural network approach is more superior than the classical technique.

Vertical arc maneuvers and vertical chirp maneuvers were limited in number and they were not considered within this study.

The combination between the proposed tool and the MDTF represents a new and reliable way to investigate the hydrodynamics of a submarine. With the new technique only a limited number of maneuvers have to actually be performed to train the network. The network can then be used to generate the force and moment for the remaining needed maneuvers. By doing this we combined the capabilities of multi-degrees-of-freedom testing with the affordability and convenience of computational techniques.

92

7. RECOMMENDATIONS

Future work should include maneuvers that were not considered within this study due to the lack of time and the limited number of tests conducted. Maneuvers such as vertical arcs, combined chirps, and five-degree-of freedom maneuvers such as cork-screw maneuvers should also be investigated.

As stated in the conclusions due to model vibration the use of the rig struts displacements introduces some uncertainty to the relation obtained by the network. Further work should use the estimate of the actual motion obtained from the onboard accelerometers.

REFERENCES

- Bhattacharyya, R., 1978, "Dynamics of Marine Vehicles", John Wiley & Sons. New York, NY.
- Bohlmann, H., 1990, "Calculation of hydrodynamic coefficients of submarines for the prediction of motion patterns" Ph.D. Thesis, Institute of Naval Architecture University of Hamburg, Hamburg, Germany.
- Feldman, J., 1995, "Method of performing captive model experiments to predict the stability and the control characteristics of submarines", CRDKNSWC-HD-0393-25.
- Haddara, M. R., 1995, "On the use of neural network techniques for the identification of ship stability parameters at sea", Proceedings of the 14th International Conference on Offshore Mechanics and Arctic Engineering, vol. II, pp.127-135.
- Haddara, M. R., and Hinchey, M., 1995, "On the use of neural network techniques in the analysis of free roll decay curves", International Shipbuilding Progress, vol. 42, no. 430, pp. 166-178.
- Haddara, M. R., and Wang, Y. 1996, "Parametric identification of coupled sway and yaw motions". Proceedings of the 15th International Conference on Offshore Mechanics and Arctic Engineering, vol. I, pp. 267-273
- Haddara, M. R, and Xu, J., 1999, "On the identification of ship coupled heave-pitch motions using neural networks", Ocean Engineering Journal, no. 26, pp. 381-400.

- Hinchey, M., 1994, "A neural network fit to icebreaker resistance data". Proceedings of the 12th International Conference on Offshore Mechanics and Arctic Engineering, vol. I, pp. 263-266.
- Kalske, S., 1992, "Motion simulation of underwater vehicles", Technical Research Center of Finland (VTT), VTT publication 97, ESPOO 1992.
- Lainiotis, D., and Plataniotis, K., 1994, "Neural network estimators: application to ship position estimation", Proceedings of IEEE conference, pp. 4710-4717.
- Math Works Inc., 1994, "MATLAB High performance numeric computation and visualization software", User's guide.
- Math Works Inc., 1997, "Wavelet toolbox for the use with MATLAB", User's guide.
- Mackay, M., 1988, "The prediction of submarine out of plane force and moment using panel method", RINA Warship 88 Symposium on Conventional Naval Submarines, London.
- Mackay, M., Conway, J., 1990, "Prediction of the effects of body separation vortices on submarine configurations using the CANERO panel method", Proceedings of AIAA 28th Aerospace Science Meeting, AIAA 90-0302.
- Mackay, M, Conway, J., 1991, "Modeling the cross flow body separation on a submarine using panel method", Warship 91 Symposium on Conventional Naval Submarines, London
- Mehrotra, K., Mohan, C., and Ranka, S., 1997, "Elements of Artificial Neural Networks", MIT Press, Cambridge, MA.
- Montgomery, D., 1997, " Design and Analysis of Experiments", John Wiley & Sons. New York, NY.

- Papoulias, A., and Mckinley, D., 1994, "Inverted pendulum stabilization of submarines in free positive buoyancy ascent", Journal of Ship Research, Vol. 38, No. 1, pp. 71-82.
- Papoulias, A., and Papadimitriou, H., 1995, "Nonlinear studies of dynamic stability of submarines in the dive plane", Journal of Ship Research, Vol. 39, No. 4, pp. 347-356.
- Rivera, C., and Hinchey, M., 1999, "Hydrodynamic loads on subsea robots", Ocean Engineering Journal, no. 26, pp. 805-812.
- Rumelhart, D., Hinton, G., Williams, R., 1986, "Learning internal representation by error propagation", Parallel distributed processing: Exploration in the microstructure of cognition. vol. 1: Foundation, MIT Press.
- Ward System Group, Inc. 1995," Neural Shell 2: User Manual".
- Watt, G., 1988, "Estimates for the added mass of a multi-component, deeply submerged vehicle", Defence Research Establishment Atlantic, Technical Memorandum 88/213, Dartmouth, NS.
- Watt, G., Nguyen, V., Cooper, K., and Tanguay, B., 1993, "Wind tunnel investigations of submarine hydrodynamics", Canadian Aerodynamics and Space Journal, vol. 39, no. 3, pp. 119-126.
- Widrow, B., and Lehr, M., 1990, "30 years of adaptive neural networks: Perceptron, Madaline, and Backpropagation", Proceeding, IEEE, vol. 78, no. 9, pp. 1415-1442.
- Williams, C., Mackay, M., Perron, C., and Muselet, C., 1999, "The NRC-IMD Marine Dynamic Test Facility: a six-degree-of-freedom forced motion apparatus for underwater vehicle testing", NRCC/IMD report IR-1999-28, St. John's, NF.

APPENDIX A NUMERICAL RESULTS

The following are the calculations for the multiple linear regression in the case of uncoupled heave, uncoupled pitch and coupled heave and pitch as well as the effect of random noise.

Uncoupled Heave.

The mathematical model for the heave force can be expressed as

$$F_i = \beta_0 + \beta_1 \dot{x}_i + \beta_2 \ddot{x}_i \tag{A.1}$$

Using the least squares method one can obtain the coefficients in the equation as follows:

$$\mathbf{X}^{T}\mathbf{X} = \begin{bmatrix} 229 & 6.4 & -1.5 \\ 6.4 & 2960.5 & 7 \\ -1.5 & 7 & 871.3 \end{bmatrix}$$
 A.2
$$\mathbf{X}^{T}\mathbf{F} = \begin{bmatrix} 0.0215 \\ 699.791 \\ 872.975 \end{bmatrix}$$
 A.3

$$(\mathbf{X}^{\mathsf{T}} \mathbf{X})^{-1} = \begin{bmatrix} 0.0044 & 0 & 0 \\ 0 & 0.0003 & 0 \\ 0 & 0 & 0.00011 \end{bmatrix}$$
 A.4

$$\hat{\boldsymbol{\beta}} = \begin{bmatrix} 0.0044 & 0 & 0 \\ 0 & 0.0003 & 0 \\ 0 & 0 & 0.00011 \end{bmatrix} \begin{bmatrix} 0.0215 \\ 699.791 \\ 872.975 \end{bmatrix} = \begin{bmatrix} 0.0 \\ 0.234 \\ 1.0 \end{bmatrix}$$
A.5

so the expected heave force would be

$$\hat{F}_i = 0.0 + 0.234\dot{x}_i + 1.0\ddot{x}_i$$
 A.6

the actual Heave force was

$$F_i = 0.0 + 0.234\dot{x}_i + 1.0\ddot{x}_i$$

Uncoupled Pitch

Using the least squares method the pitch moment is assumed to follow the mathematical

model shown in equation A.7

-

$$F_i = \beta_0 + \beta_1 x_i + \beta_2 \dot{x}_i + \beta_3 \ddot{x}_i \qquad A.7$$

The coefficients are estimated as follows

$$\mathbf{X}^{\mathsf{T}}\mathbf{X} = \begin{bmatrix} 586 & 0.0014 & -0.1 & -0.0007 \\ 0.0014 & 1.291 & 0.001 & -0.761 \\ -0.1 & 0.001 & 0.776 & 0.0001 \\ -0.0007 & -0.761 & 0.0001 & 0.569 \end{bmatrix}$$
A.8
$$\mathbf{X}^{\mathsf{T}}\mathbf{F} = \begin{bmatrix} 0.0109 \\ 38.9769 \\ 0.1756 \\ -22.8582 \end{bmatrix}$$
A.9

$$\begin{pmatrix} \mathbf{X}^{\mathsf{T}} \mathbf{X} \end{pmatrix}^{-1} = \begin{bmatrix} 0.0017 & 0 & 0.0002 & 0 \\ 0 & 3.6537 & -0.0011 & 4.8836 \\ 0.0002 & -0.0011 & 1.2887 & -0.0016 \\ 0 & 4.8836 & -0.0016 & 8.2836 \end{bmatrix}$$
 A.10

$$\hat{\boldsymbol{\beta}} = \begin{bmatrix} 0.0017 & 0 & 0.0002 & 0 \\ 0 & 3.6537 & -0.0011 & 4.8836 \\ 0.0002 & -0.0011 & 1.2887 & -0.0016 \\ 0 & 4.8836 & -0.0016 & 8.2836 \end{bmatrix} \begin{bmatrix} 0.0109 \\ 38.9769 \\ 0.1756 \\ -22.8582 \end{bmatrix} =$$
 A.11

$$\begin{bmatrix} 0 \\ 30.7804 \\ 0.2222 \\ 1.0005 \end{bmatrix}$$

So the expected pitch moment would be

$$\hat{F}_i = 0.00 + 30.7804 x_i + 0.2222 \dot{x}_i + 1.0005 \ddot{x}_i$$
 A.12

the actual pitch moment is

 $F_i = 0.00 + 30.78 x_i + 0.222 \dot{x}_i + 1.0 \ddot{x}_i$

Coupled Heave-Pitch

Applying the least squares method one can obtain the following

$$\mathbf{X}_{s}^{*}\mathbf{X}_{s} = 10^{3} * \begin{bmatrix} 0.465 & 0.0137 & -0.0033 & -0.0033 & -0.0001 \\ 0.0137 & 4.5464 & 0.0136 & -0.0633 & -0.0407 \\ -0.0033 & 0.0136 & 1.8516 & 0.0408 & -0.0261 \\ -0.0033 & -0.0633 & 0.0408 & 0.0018 & 0 \\ -0.0001 & -0.0407 & -0.0261 & 0 & 0.0008 \end{bmatrix}$$
 A.13

$$\mathbf{X}_{3}^{T} \mathbf{X}_{3} = 10^{3} * \begin{bmatrix} 0.466 & 0.0106 & -0.0002 & -0.0001 & 0.0001 \\ 0.0106 & 4.5558 & -0.0635 & -0.0409 & -0.0259 \\ -0.0002 & -0.0635 & 0.0018 & 0.0 & -0.0008 \\ -0.0001 & -0.0409 & 0.0 & 0.0008 & 0 \\ 0.0001 & 0.0259 & -0.0008 & 0 & 0.0004 \end{bmatrix}$$
A.14
$$\mathbf{X}_{3}^{T} \mathbf{F}_{3} = 10^{3} * \begin{bmatrix} -0.0002 \\ 1.0559 \\ 1.8604 \\ 0.0265 \\ -0.0355 \end{bmatrix}$$
A.15
$$\mathbf{X}_{3}^{T} \mathbf{F}_{3} = \begin{bmatrix} 0.0091 \\ 703.506 \\ 17.643 \\ -23.6649 \\ -8.8516 \end{bmatrix}$$
A.16

$$\hat{\boldsymbol{\beta}}_{3} = \begin{bmatrix} 0.0 \\ 0.2340 \\ 1.0001 \\ 0.2355 \\ 0.1581 \end{bmatrix} \qquad \text{and} \qquad \hat{\boldsymbol{\beta}}_{3} = \begin{bmatrix} 0.0 \\ 0.5801 \\ 30.7843 \\ 0.2247 \\ 1.0044 \end{bmatrix} \qquad 1.17$$

So the expected heave force and pitch moment would be

$$\hat{F}_{3i} = 0.0 + 0.234 \dot{x}_{3i} + 1.0001 \ddot{x}_{3i} + 0.2355 x_{5i} + 0.1581 \dot{x}_{5i}$$
 A.18

$$\hat{F}_{5i} = 0.0 + 0.5801 \dot{x}_{3i} + 30.7843 x_{5i} + 0.2247 \dot{x}_{5i} + 1.0044 \ddot{x}_{5i}$$
 A.19

the actual heave and pitch moment were

 $F_{3i} = 0.0 + 0.234 \dot{x}_{3i} + 1.0001 \ddot{x}_{3i} + 0.238 x_{5i} + 0.1581 \dot{x}_{5i}$

 $F_{5i} = 0.0 + 0.58\dot{x}_{3i} + 30.78x_{5i} + 0.222\dot{x}_{5i} + 1.0\ddot{x}_{5i}$

APPENDIX B VISUAL BASIC PROGRAM

"SIMULATION"

The following Visual Basic program was written to generate the sub motion time series

used in the validation of the method.

Dim delta As Double, omega As Double, k(4) As Double, t As Double Dim L(4) As Double, a3(4000), a5(4000), M(4) As Double, N(4) As Double, v3(4000) As Double, v5(4000) As Double Dim x3(4000) As Double, t5(4000) As Double, F1(4000) As Double, F2(4000) As Double Dim B33, c33, B35, c35, B53, c53, B55, c55 Dim i As Integer, j As Integer, f30 As Integer Dim G1 As Double, C2 As Double, ne As Integer, Nois As Double Dim workfile As String

Private Sub Command1_Click() 'reading data from input form Dim Counter As Integer Counter = 0 ProgressBar1.Max = 14001 ProgressBar1.Visible = True

'Set the Progress's Value to Min.

ProgressBarl.Value = ProgressBarl.Min ProgressBarl.Value = Counter B33 = b11(0).Text B35 = b21(1).Text B55 = b31(2).Text B53 = b41(3).Text c33 = Me_c33(4).Text c55 = Me_c35(5).Text c55 = Me_c55(6).Text

```
c53 = Me_c53(7).Text

[30 = Me_f30(8).Text

[50 = Me_f50(9).Text

omega = Me_omeg(10).Text

ne = Noise.Value

Nois = Noise_value(0).Text

ProgressBarl.Value = Counter
```

' creating a temp. working file

Open "c:\simulation\temp" For Output As #1 Print #1, B33, B35, B55, B53 Print #1, c33, c35, c55, c53 Print #1, f30, f50, omega, ne, Nois Close #1 delta = 0.1 x3(1) = 0 x3(1) = 0 x5(1) = 0 x5(1) = 0 t = 0

' the following generates the heave and pitch force

```
For i = 1 To 3000

Counter = Counter + 1

F1(i) = f30 * Sin(omega * t)

F2(i) = f50 * Sin(omega * t)

t = t + delta

ProgressBarl.Value = Counter

Next i
```

'Numerical integration of the ship's equations of motion

```
For i = 1 To 3000

Counter = Counter + 1

Call equation(B33, c33, B35, c35, B53, c53, B55, c55, x3(i), x5(i), v3(i), v5(i))

k(1) = delta * (v3(i))

L(1) = delta * (v5(i))

N(1) = delta * (v5(i))

N(1) = delta * (v5(i))

Call equation(B33, c33, B35, c35, B53, c53, B55, c55, x3(i) + 0.5 * k(1), x5(i) + 0.5 *

M(1), v3(i) + 0.5 * L(1), v5(i) + 0.5 * N(1))

k(2) = delta * (v5(i) + 0.5 * L(1))

L(2) = delta * (v5(i) + 0.5 * N(1))

k(2) = delta * (v5(i) + 0.5 * N(1))

k(2) = delta * (v5(i) + 0.5 * N(1))
```

```
N(2) = delta * (((F2(i) + F2(i + 1)) / 2) - G2)
Call equation(B33, c33, B35, c35, B53, c53, B55, c55, x3(i) + 0.5 * k(2), x5(i) + 0.5 *
M(2), v3(i) + 0.5 * L(2), v5(i) + 0.5 * N(2))
k(3) = delta * (v3(i) + 0.5 * L(2))
L(3) = delta * (((F1(i) + F1(i + 1))/2) - G1)
M(3) = delta * (v5(i) + 0.5 * N(2))
N(3) = delta * (((F2(i) + F2(i + 1))/2) - G2)
Call equation(B33, c33, B35, c35, B53, c53, B55, c55, x3(i) + k(3), x5(i) + M(3), v3(i) +
L(3), v5(i) + N(3))
k(4) = delta * (v3(i) + L(3))
L(4) = delta * (F1(i + 1) - G1)
M(4) = delta * (v5(i) + N(3))
N(4) = delta * (F2(i + 1) - G2)
x_3(i + 1) = x_3(i) + ((k(1) + 2 * k(2) + 2 * k(3) + k(4)) / 6)
x5(i + 1) = x5(i) + ((M(1) + 2 * M(2) + 2 * M(3) + M(4)) / 6)
v_{3}(i + 1) = v_{3}(i) + ((L(1) + 2 * L(2) + 2 * L(3) + L(4)) / 6)
v5(i + 1) = v5(i) + ((N(1) + 2 * N(2) + 2 * N(3) + N(4)) / 6)
ProgressBar1.Value = Counter
Next i
For i = 1 To 3000
Counter = Counter + 1
Call equation(B33, c33, B35, c35, B53, c53, B55, c55, x3(i), x5(i), v3(i), v5(i))
a3(i) = F1(i) - G1
a5(i) = F2(i) - G2
ProgressBar1.Value = Counter
Next i
 For i = 1 To 3000
 Counter = Counter + 1
 x_3(i) = x_3(i) + (x_3(i) * Rnd * Nois * ne)
x5(i) = x5(i) + (x5(i) * Rnd * Nois * ne)
v_3(i) = v_3(i) + (v_3(i) * Rnd * Nois * ne)
v5(i) = v5(i) + (v5(i) * Rnd * Nois * ne)
a3(i) = a3(i) + (a3(i) * Rnd * Nois * ne)
a5(i) = a5(i) + (a5(i) * Rnd * Nois * ne)
ProgressBar1.Value = Counter
Next i
t = 100
'Writing out the results
file = CStr(omega)
file = Trim(file)
Open "c:\simulation\hevpitch" + file + ".out" For Output As #4
Print #4, "t"; ","; "x3"; ","; "v3"; ","; "a3"; ","; "F30"; ","; "x5"; ","; "v5"; ","; "a5"; ",";
```

```
"f50"
```

```
For i = 1000 To 3000
Counter = Counter + 1
Print #4, t; ","; x3(j); ","; v3(j); ","; a3(j); ","; F1(j); ","; x5(j); ","; v5(j); ","; a5(j); ",";
F2(i)
t = t + delta
ProgressBar1.Value = Counter
Next i
Close #4
Timerl Interval = 2000
End Sub
Public Sub equation(B33, c33, B35, c35, B53, c53, B55, c55, x3 As Double, x5 As
Double, v3 As Double, v5 As Double)
G1 = (B33 * v3) + (c33 * x3) + (B35 * v5) + (c35 * x5)
G2 = (B53 * v3) + (c53 * x3) + (B55 * v5) + (c55 * x5)
End Sub
Private Sub Command2 Click()
'recalling the previous inputs
Open "c:\simulation\temp" For Input As #1
Input #1, B33, B35, B55, B53
Input #1, c33, c35, c55, c53
Input #1, f30, f50, omega, ne, Nois
Close #1
b11(0).Text = B33
b21(1).Text = B35
b31(2).Text = B55
b41(3).Text = B53
Me_c33(4).Text = c33
Me c35(5).Text = c35
Me c55(6).Text = c55
Me_c53(7).Text = c53
Me f30(8).Text = f30
Me_f50(9).Text = f50
Me omeg(10).Text = omega
Noise value(0).Text = Nois
If ne = 1 Then Noise.Value = 1
End Sub
```

Private Sub Command3_Click() Unload Me End Sub

Private Sub Timer1_Timer() ProgressBar1.Value = ProgressBar1.Min End Sub



APPENDIX C LIST OF RUNS

DREA_standard_sub_runs_13oct_to_17nov.xis I. Mohamed, C.D.Williams, 23 Dec 99 - revised 19 Jan 2000 Dynamic runs for DREA standard sub

	VMS	Date	Time	File	Maneuver	Orit					
Dir: TOW [TEST_PJ9868.OCT99]	blocks	acquired	acquired	type	Type	Angle	Status	Time segments	Cs	Amplitude	Remarks
SVA0500H_001.DAC;1	2086	08-Nov-99	9.52:08	Dynamic	Horizontal Arc 0.05	0	Successful	80-200 sec	0		
	902	08-Nov-99			Horizontal Arc 0.10	0	Premature termination	25-80 sec	0	11 11 11 11	High Following error- Aft vertical
SVA0500H_002.DAC;1	1124	08-Nov-99	11:47:03	Dynamic	Horizontal Arc 0.05	0	Successful	10-135 sec	0		
	754	08-Nov-99		Dynamic	Horizontal Arc 0.10	0	Premature termination	13-63 sec	0	100.000	High Following error- Aft vertical
	1420	08-Nov-99	11:56:34	Dynamic	Horizontal Arc 0.10	0	Successful	52-130sec	1.5		
	1346		12:00:46	Dynamic	Horizontal Arc 0.15	0		80-150 sec	1.5	and a present	High Following error- Aft vertical
SVA0500H_004.DAC;1	1346	08-Nov-99	12:22:45	Dynamic	Horizontal Arc 0.05	0	Successful	60-140 sec	1.5		
	902				Horizontal Arc 0 20	0,		65-95 sec	1.5	1.2-19.25	High Following error- Aft vertical
	1272					0		80-130 sec	1,5	1 - C - C - C - C - C - C - C - C - C -	High Following error- Aft vertical
SVA3000H_001.DAC;1	1346	08-Nov-99	15:03:56	Dynamic	Horizontal Arc 0.30	0	Premature termination	90-125 sec	1.5	10 - 10 mil	High Following error- Aft vertical
SVA0500V_001.DAC;1	2678	08-Nov-99		Dynamic	Vertical Arc 0.05						High Following error- Alt vertical
SVA0500V_002.DAC;1	2678		16:06:54		Vertical Arc 0.05						High Following error- Aft vertical
					Hull	+ Sail + 1	al				
HST_SVA0500H_001.DAC;1	1346	10-Nov-99	15:53:05	Dynamic	Horizontal Arc 0.05	0	Successful	75-150 sec	1.5		
HST_SVA1000H_001.DAC;1	1494	10-Nov-99	16:03:24	Dynamic	Horizontal Arc 0.10	0	Successful	85-160sec	1.5		
HST_SVA1500H_001.DAC;1	1346	10-Nov-99	16:12:57	Dynamic	Horizontal Arc 0.15	0	Successful	75-140 sec	1.5	100	
HST_SV2000H_001.DAC;1	1346	10-Nov-99	16:23:32	Dynamic	Horizontal Arc 0.20	0	Successful	65-140 sec	1.5		
HST_SV2500H_001.DAC;1	.1198	10-Nov-99		Dynamic	Horizontal Arc 0.25	0	Premature termination	60-130 sec	1.5		High Following error- Aft vertical
	1272			Dynamic	Horizontal Arc 0.30	0		70-140 sec	1.5	1217 1218	see foot note 1
HST_SV3000V_TEST_001.DAC;1	1642	10-Nov-99	16:54:12	Dynamic	Vertical Arc 0.30	0	Successful	50-175 sec	0		
					н	ull + Sail					
HS_SVA0500H_001.DAC;1	1346	12-Nov-99	13:07:09	Dynamic	Horizontal Arc 0.05	0	Successful	75-150 8400	1.5		
HS SVA1000H 001.DAC;1	1272		13:16:50	Dynamic	Horizontal Arc 0.10	0	Successful	60-130 \$60	1.5		
HS SVA1500H 001.DAC;1	1272	12-Nov-99	13:28:18	Dynamic	Horizontal Arc 0.15	0	Successful	60-130 \$60	1.5		
HS SVA2000H 001.DAC;1	1198	12-Nov-99	13:39:34	Dynamic	Horizontal Arc 0.20	0	Successful	60-130 sec	1.5		
HS_SVA2500H_001.DAC;1	1198	12-Nov-99	13:49:54	Dynamic	Horizontal Arc 0.25	0	Successful	60-125 840	1.5		
HS_SVA3000H_001.DAC;1	605	12-Nov-90	13:58:29	Dynamic	Horizontal Arc 0.30	0	Failed		1.5	1000	Following error-Fwd Lateral
HS_SVA3000H_002.DAC;1	1272	12-Nov-90	16:34:30	Dynamic	Horizontal Arc 0.30	0	Successful	70-140 800	1.5		
					Hull	+ Sail + 1	ail				
HST_SVA0505H_001.DAC;1	1346		12:21:02	Statio	Horizontal Arc 0.05	5	Successful	50-150 sec	1.5		
HST SVA0505H 002 DAC:1	1346	15-Nov-99	12:28:42	Dynamic	Horizontal Arc 0.05	5	Successful	80-150 \$40	1.5		
HST_SVA0510H_001.DAC;1	1272	15-Nov-99	12:38:24	Dynamic	Horizontal Arc 0.05	10	Successful	75-150 sec	1.5		
HST_SVA1005H_001.DAC;1	1642	15-Nov-99	14:41:56	Dynamic	Horizontal Arc 0.10	5	Successful	120-190 sec	1.5		
HST_SVA1010H_001.DAC;1	1568	15-Nov-99	14:54:02	Dynamic	Horizontal Arc 0.10	10	Successful	90-160 sec	1,5		
HST_SVA1505H_001.DAC;1	1198	15-Nov-99	15:04:38	Dynamic	Horizontal Arc 0.15	5	Successful	65-130 sec	1.5		
HST_SVA2005H_001.DAC;1	1198	15-Nov-99	15:15:05	Dynamic	Horizontal Arc 0.20	6	Successful	65-130 sec	1.5		
HST_SVA2505H_001.DAC;1	1198	15-Nov-99	15:24:44	Dynamic	Horizontal Arc 0.25		Successful	60-125 sec	1.5		
HST_SVA1510H_001.DAC;1	1124	15-Nov-99	15:35:17	Dynamic	Horizontal Arc 0.15	10	Successful	60-125 sec	1.5		
HST_SVA2010H_001.DAC;1	1124	15-Nov-99	15:46:11	Dynamic	Horizontal Arc 0.20	10	Successful	60-125 sec	1.5		
HST_SVA2510H_001.DAC;1	1346	15-Nov-99	15:55:59	Dynamic	Horizontal Arc 0.25	10	Successful	80-155 sec	1.5		
HST_SVA0500V_001.DAC;1	1050	15-Nov-99	16:20:41	Dynamic	Vertical Arc 0.05	0	Successful	45 - 120 sec	1.5		
HST_SVA1000V_001.DAC;1	532	15-Nov-99	17:02:58		Vertical Arc 0.05						see footnote 2

HST HSPY F1T3V700 001 DAC:	605	16-Nov-99	18:11:35	Dynamic	4 DOF Chirp 0.1 to 0.3	Premature termination	45-65 \$00	2	Following error- All vertical
HST YP F1T3V700 001.DAC:1	605		18:21:55	Dynamic	Combined Yaw & Pitch Chirp		50-60 sec	2	Following error- Aft vertical
	-				Huli + Sail				
HS F1T3V250S 001.DAC:1	902	[16-Nov-99]	19:10:41	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Successful	45-110 sec	2	
HS_E1T3V500S_001.DAC:1	1198	16-Nov-99	19:24:08	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Successful	85-140 sec	2	
HS_E1T3V600S_001 DAC:1	754		19:52:49	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Premature termination	63-85 600	2	High following error- Fwd Lateral
HS E1T3V700S 001 DAC:1	902	16-Nov-99	19:43:01	Dynamic	Swary Chim 0.1 to 0.3 Hz	Successful	45-105 sec	2	
HS F1T3V800S 001 DAC:1	680		19:58:34	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Premature termination	50-65 840	2	High following error- Fwd Lateral
HS F1T3V600S 002 DAC:1	976	16-Nov-99	20:27:53	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Successful	50-105 sec	2	111
HS E1T3V800S 002 DAC:1	680	16-Nov-99	20.39-28	Dynamic	Swiry Chirp 0.1 to 0.3 Hz	Premature termination	45-75 sec	2	High following error- Fwd Lateral
HS F1T3V250H 001.DAC:1	976	16-Nov-99	20:48:58	Dynamic	Heave Chirp 0.1 to 0.3 Hz	Successful	50-105 sec	2	
HS F1T3V500Y 001 DAC:1	902	16-Nov-99	20:59:49	Dynamic	Yaw Chirp 0.1 to 0.3 Hz	Successful	40-105 sec	2	
HS_E1T5V250Y_001.DAC:1	976	16-Nov-99	21:10:52	Dynamic	Yaw Chirp 0.1 to 0.5 Hz	Successful	60-114 sec	2	
HS F1T3V700Y 001.DAC:1	902	16-Nov-99	21:21:14	Dynamic	Yaw Chirp 0.1 to 0.3 Hz	Successful	50-105 sec	2	
HS F1T3V250YS 001.DAC:1	1124	16-Nov-99	21:31:58	Dynamic	Combined Yaw & Sway Chirp	Successful	75-130 sec	2	
HS F1T3V500YS 001.DAC:1	976	16-Nov-99	21:41:32	Dynamic:	Combined Yaw & Sway Chirp	Successful	60-114 sec	2	
HS F1T5V400YS 001.DAC:1	976	16-Nov-99	21:50:56	Dynamic	Combined Yaw & Sway Chim	Successful	57-110 sec	2	
	754				Combined Yaw & Sway Chim		60-75 sec	2	Following error- Fwd Lateral
	606				4 DOF Chirp 0.1 to 0.5		40-62 800	2	Following error-Aft vertical
HS YP F1T3V700_001.DAC:1	502	16-Nov-99	22-24:33	Dynamic	Combined Yaw & Pitch Chiro	Falled		2	Following error
					Hull + Fins				
HT F1T3V250S 001.DAC:1	1420	17-Nov-99	10:46:50	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Successful	110-165 sec	2	
HT F1T3V500S 001 DAC:1	1346	17-Nov-99	10:58:23	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Successful	95-150 sec	2	
HT_F1T3V600S_001.DAC:1	1050	17-Nov-99	11:05:57	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Successful	60-110 sec	2	
HT F1T3V700S 001 DAC:1	1198	17-Nov-99	11:24:39	Dynamic	Sway Chirp 0.1 to 0.3 Hz	Successful	80-130 sec	2	
HT F1T3V800S 001 DAC:1	1198	17-Nov-99	11:36:30	Dynamic	Swary Chirp 0.1 to 0.3 Hz	Premature termination	110-130 sec	2	High following error- Fwd lateral
HT_F1T3V250H_001.DAC;1	1124	17-Nov-99	11:48:17	Dynamic	Heave Chirp 0.1 to 0.3 Hz	Successful	70-125 sec	2	
HT_F1T3V500Y_001.DAC:1	1494	17-Nov-99	12:11:12	Dynamic	Yaw Chirp 0.1 to 0.3 Hz	Successful	80-130 sec	2	
HT_F1T5V250Y_001.DAC:1	1124	17-Nov-99	12:20:33	Dynamic	Yaw Chirp 0.1 to 0.5 Hz	Successful	60-115 sec	2	
HT F1T3V700Y_001.DAC:1	1272	17-Nov-99	12:29:58	Dynamic	Yaw Chirp 0.1 to 0.3 Hz	Successful	80-140 sec	2	
HT_F1T3V250YS_001.DAC;1	1272	17-Nov-99	13:47:55	Dynamic	Combined Yaw & Sway Chirp	Successful	85-140 sec	2	
HT F1T3V500YS 001.DAC:1	1124	17-Nov-99	14:17:31	Dynamic	Combined Yaw & Sway Chirp	Successful	60-120 sec	2	
HT F1T5V400YS 001.DAC:1	1124	17-Nov-99	14:26:51	Dynamic	Combined Yaw & Sway Chirp	Successful	70-125 sec	2	
HT_F1T5V500YS_001.DAC;1	1124	17-Nov-99	14:36:42	Dynamic	Combined Yaw & Sway Chirp	Successful	70-125 sec	2	
HT_HSPY_F1T3V700_001.DAC;1	754	17-Nov-99		Dynamic	4 DOF Chirp 0.1 to 0.3		60-75 sec	2	Following error- Aft vertical
HT_YH_F1T3V700_001.DAC:1	828	17-Nov-99		Dynamic	Combined Yaw & Heave Chirp		80-92 sec	2	Following error- Alt vertical
HT_SCREWSDEG_001.DAC;1	1124	17-Nov-99		Dynamic	Screw Maneuver 5 Deg Rotation	Successful	70-125 sec	2	
HT_SCREW_NOROT_001.DAC;1	1272	17-Nov-99		Dynamic	Screw Maneuver no Relation	Premature termination	85-140 sec	2	Following error
WATER_WT_001.DAC;1	384	17-Nov-99	15:46:17	Weight					
AID WT 001 DAC-1	384	17-Nov-99	16:14:05	Weight					

125 dynamic runs for the DREA standard sub

AR Strut shows no activity MDTF had to be shutt down and restarted
 Zystem Crasted - MDTF had to be shutt down and restated
 Solowing error. Field Later-invalid start to nod
 Following error. Field Later-invessive reckling in the model

DREA_STD_SUB_DYNAMIC_RUNS_APR_99 I. Mohamed, C.D.Williams, 10 Sep 99, Revised 20 January 1999

	100.00	1 Photo:									
A REAL PROPERTY OF TAXABLE PROPERTY.	VMS	Uate	Time	File	Maneuver		Time				
DV TOW[TEST_PJ98883.APH99.HAW]	blocks	acquired	acquired	type	Type	Status	segments	Ca	Frequenc	Amplitude	Remarks
Hull Sail + Tail											
SCREW 5DEG 001 001.DAC:1	1796	11-May-99	15:27:42	Danamin I	Cadaran	00017100	1 00 010	-	-		
SCREW SDEG 001 DAC:1	1796	11.May.00	16-08-04	D	Consciew	Successful	30 - 240 SHC	0	-		
	1100			Synamic	Conscrew	Successful	30 - 240 sec	0			
SCHEW NO HOT OUT DAU;1	1004	11-May-99	15:31:05	Dynamic	Corksonew	Successful	20 - 120 sec	0			
SCREW_5DEG_002.DAC;1	1928	11-May-99	15:37:18	Dynamic	Corkscraw	Currenterhal	10,150,665	0			
HSF_V3_HA200_HF025_001.DAC;1	740	12-May-99	13:19:47	Dynamic	Harmonic Heave	Curcossful	60.75 800	3	0.25	0.2	
HSF. V3_HA333_HF015_001.DAC:1	806	12-May-92	13:32:14	Danamin	Magnetic Manage	Currenti	0013300		0.15	0.333	
MSE V3 HA333 HEA15 002 DAC-1	200	12.86		- Pragman	Fighting the Preserve	Successrul	60 - 90 Sec.	3	0.10	0.333	
1101_10_104000_111010_00&_DH0,1	000	15-0092-02	13/43.24	Unamic	Harmonic Heave	L Successful	40 - 75 sec	3	0,15	0.333	
HSF_V3_HA111_HF045_001.DAC;1	740	12-May-99	13:54:20	Dynamic	Harmonic Heave	Successful	63 - 88 sec	3	0.45	0.111	
HSF_V3_HA077_HF065_001.DAC;1	608	12-May-99		Denamic	Harmonic Heave	TOTAL OF THE OWNER		8	0.65	0.077	The second s
HSF_V3_SA333_SF015_001.DAC;1		14-May-99		Dinamic	Harmonic Heave	Enlard				0.333	
HSF_V3_SA333_SF015_002.DAC;1	806	14-May-99	8:29:15	Dynamic	Harmonic Search	Successful	60 - 95 sec	3	0.15	0.993	
HSF_V3_SA200_SF025_001.DAC:1	674	14-May-99	8:44:15	Dimamin	Harmonic Carne	Currentd	10,00		0.16	0.9	
WEE VO EARER PEOLE OOL DACH	740	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	A 7 4 44		Page 100 mg officer	Successiu	00-00		0.40	0.4	
1107_13_04000_07010_001.DRD,1	740	14-M3Y-99	8.56.06	Unamic	Harmonic Sway	Successful	60 - 88 sec	3	0.15	0.666	
HSF_V3_SA400_SF025_001.DAC;1	740	14-May-99	9:07:43	Dynamic	Harmonic Sway	Successful	55 - 88 sec	3	0.25	0.444	
					DESCRIPTION OF TAXABLE PARTY.	of strength of the local division of the	of the local division of the	and the local division of		COLUMN TWO IS NOT	

Total of 15 files

DREA_STD_SUB_DYNAMIC_RUNS_NOV_98 I. Mohamed, C.D.Williams, 10 Sep 99. Revised 20 January 1999

	VMS	Date	Time	Filo	Maneuver	Contraction of the local division of the loc					
Dir TOW: TEST_PJ98683.RAW	blocks	acquired	acquired	type	' Type	Status	Time segments	Ca	Frequency	Amplitude	Remarks
					10 10 10 10 10 10 10 10 10 10 10 10 10 1	Hull + Sail + Tai	1			-	
V0_SWAYTEST_001.DAC;1	482	05-Nov-98	14:53:43	Dynamic	Harmonic Sway	Successful	10 - 30 sec	0	0.05		
V0_HEAVETEST_001.DAC;1	638	05-Nov-98	15:01:15	Dynamic	Harmonic Heave	Successful	10-60 sec	0	0.12		1 C C C C C C C C C C C C C C C C C C C
V0_HEAVETEST_002.DAC;1	2588	05-Nov-98	17:10:32	Dynamic	Harmonic Heave	Successful	50 - 300 sec	0	0.015		
V0_HEAVETEST_003.DAC;1	1340	05-Nov-98	17:14:27	Dynamic	Harmonic Heave	Successful	0 - 140 sec	0	0.03		2
V0_HEAVETEST_004.DAC;1	404	05-Nov-98	17:15:37	Dynamic	Harmonic Heave	Successful	0 - 20 sec	0	0.145		
V0_HEAVETEST_005.DAC;1	404	05-Nov-98	17:16:56	Dynamic	Harmonic Heave	Successful	0 - 25 900	0	0.145		
V0_HR314_HF15_001.DAC;1	482	05-Nov-98	17:20:46	Dynamic	Harmonic Heave	Successful	0 - 25 sec	0	0.15		
V0_HR314_HF25_001.DAC;1	482	05-Nov-98	18:11:56	Dynamic	Harmonic Heave	Successful	0 - 30 sec	0	0.25		
V0_HR314_HF45_001.DAC;1		05-Nov-98		Dynamic	Harmonic Heave	Failed			0.45		
V0_HR628_HF15_001.DAC;1		05-Nov-98		Dynamic	Harmonic Heave	Failed					
V0_SR314_SF15_001.DAC;1	794	05-Nov-98		Dynamic	Harmonic Sway	Failed					
V0_SR314_SF15_002.DAC;1	1340	08-Nov-98	13:55:59	Dynamic	Harmonic Sway	Successful	80 - 140 sec	0	0.15		
V0_SR400_SF15_001.DAC;1	794	08-Nov-98	14:04:33	Dynamic	Harmonic Sway	Successful	13 - 62 sec	0	0.15		
V0_SR314_SF25_001.DAC;1	950	08-Nov-98	14:09:57	Dynamic	Harmonic Sway	Successful	40 - 75 sec	0	0.25		
V0_SR628_SF15_001.DAC;1	638	08-Nov-98	14:13:08	Dynamic	Harmonic Sway	Failed					
V0_SR628_SF15_002.DAC;1		08-Nov-98		Dynamic	Harmonic Sway	Falled					Actuator plot shows that amplitude is 0.325
V0_SR628_SF15_003.DAC;1	794	08-Nov-98	16:18:41	Dynamic	Harmonic Sway	Success/ul	12 - 75 500	0	0.15		
V1_SR628_SF15_001.DAC;1	1106	08-Nov-98	16:26:13	Dynamic	Harmonic Sway	Success/ul	45 - 110 sec	1	0.15		Server and the server
V35_SR628_SF15_001.DAC;1	872	08-Nov-98	16:34:33	Dynamic	Harmonic Sway	Success/ul	25 - 50 sec	3.5	0.15		
V35_SR314_SF25_001.DAC;1	638	08-Nov-98	16:42:59	Dynamic	Harmonic Sway	Successful	30 - 50 sec	3.5	0.25		
V0_SR314_YF15_001.DAC;1	1808	08-Nov-98	17:24:59	Dynamic	Combined Sway & Yaw	Success/ul	80 - 140 sec	0	0.15		
V0_SR400_YF15_001.DAC;1	794	08-Nov-98	17:31:28	Dynamic	Combined Sway & Yaw	Successful	12 - 62 sec	0	0.15		
V0_SR628_YF15_001.DAC;1	638	08-Nov-98	17:36:13	Dynamic	Combined Sway & Yaw	Successful	20 - 60 sec	0	0.15		
V35_SR628_YF15_001.DAC;1	716	08-Nov-95	17:40:15	Dynamic	Combined Sway & Yaw	Successful	30-60	3.5	0.15		
V0_SF15_YF15_001.DAC;1	716	08-Nov-98	17:58:10	Dynamic	Combined Sway & Yaw	Successful	10 - 50 sec	0	0.15		
V35_SF15_YF15_001.DAC;1	794	08-Nov-98	18:03:01	Dynamic	Combined Sway & Yaw	Successful	40 - 70 sec	3.5	0.15		
V0_SF15_YF15_002.DAC;1	716	08-Nov-98	18:28:03	Dynamic	Combined Sway & Yaw	Successful	20 - 75 sec	0	0.15		
V0_SF25_YF25_001.DAC;1	716	08-Nov-98	18:30:25	Dynamic	Combined Sway & Yaw	Successful	13-62 800	0	0.25		
V35_SF25_YF25_001.DAC;1	638	08-Nov-98	18:33:23	Dynamic	Combined Sway & Yaw	Successful	30 - 45 sec	3.5	0.25		
V0_SF25_YF25_002.DAC;1	3914	08-Nov-98	18:46:40	Dynamic	Combined Sway & Yaw	Successful	10 - 50 sec	0	0.25		

Total of 30 files

APPENDIX D VISUAL BASIC PROGRAM

"PREPSHOP"

This appendix contains the code for the MDTF Prepshop transformation of axis. It reads the MDTF exported file and perform the steps described in chapter 4

Private Sub Form_Load() Timemin.Caption = HScroll1(0).Value Timemax.Caption = HScroll2(1).Value End Sub

Private Sub HScroll1_Change(Index As Integer) Timemin.Caption = HScroll1(0).Value End Sub

Private Sub HScroll2_Change(Index As Integer) Timemax.Caption = HScroll2(1).Value End Sub

Private Sub OK_Click() t3 = HScroll1(0).Value t4 = HScroll2(1).Value Timefrm.Hide End Sub

Private Sub Command1_Click() Sting_length = HScroll1.Value / 1000 stnig.Hide End Sub

Private Sub Form_Load() Stinglen.Caption = HScroll1.Value / 1000 End Sub

Private Sub HScroll1_Change() Stinglen.Caption = HScroll1.Value / 1000 End Sub

Dim () As Double, c() As Double, Fx() As Double, Fv() As Double, Fz() As Double, Mx() As Double, Mv() As Double, Mz() As Double, FV() As Double, Av() As Double, FI() As Double, Al() As Double Dim fax, fay, faz, aax, aay, aaz As Variant Dim Swav() As Double, Heave() As Double, Yaw() As Double, Pitch() As Double Dim Sway_vel() As Double, Heave_vel() As Double, Yaw_vel() As Double, Pitch_vel() As Double Dim i As Integer, v As Double, Sting length As Double, t3 As Integer, t4 As Integer Dim X As Single, pi As Double, Lower value As Single, Upper_value As Single Dim File_name As String, SaveFile As String, File_out As String Private Sub Picture1 Click() CommonDialog1.CancelError = True On Error GoTo ErrHandler CommonDialog1.Filter = "Ascii(*.asc)|*.asc|Prepshop (*.pmd)|*.pmd|All Files (*.*)|*.*|" CommonDialog1.ShowOpen File name = CommonDialog1.filename FileCharNo = InStr(File_name, ".") If FileCharNo = Len(File_name) Then SaveFile = (File name) Else SaveFile = Left(File_name, FileCharNo - 1) End If FrrHandler Exit Sub End Sub Private Sub Picture2 Click() stnig.Show End Sub Private Sub Picture3_Click() Timefrm Show End Sub Private Sub Picture5 Click() Static garb As Double Open File name For Input As #1 pi = 3.141592654 v = 1StatusBarl.SimpleText = "Loading File " + File name Sting_length = stnig.HScroll1.Value / 1000 t3 = Timefrm. HScroll1(0). Value

t4 = Timefrm, HScroll2(1), Value Do While Not EOF(1) Input #1. garb y = y + 1Loop Close #1 i = v / 18i=i ProgressBar1.Min = 0 ProgressBar1.Max = j ProgressBar1. Visible = True ProgressBar1.Value = Min ReDim t(i), c(i), Fx(i), Fy(i), Fz(i), Mx(i), My(i), Mz(i), FV(i), Av(i), Fl(i), Al(i) ReDim Swav(i) As Double, Heave(i) As Double, Yaw(i) As Double, Pitch(i) As Double ReDim Sway vel(i) As Double, Heave vel(i) As Double, Yaw vel(i) As Double, Pitch vel(i) As Double Open File name For Input As #1 Fori = 1 Toi-1 ProgressBar1.Value = i Input #1, t(i), c(i), Fx(i), Fy(i), Fz(i), Mx(i), My(i), Mz(i), FV(i), Av(i), Fl(i), Al(i), fax, fay, faz, aax, aay, aaz Nexti Close #1 ProgressBar1. Visible = False StatusBarl.SimpleText = "computing motion at BRC" For i = 1 To i Sway(i) = Al(i) + ((Sting_length / Sting_length - 2) * (Fl(i) - Al(i))) X = (Fl(i) - Al(i)) / 2Yaw(i) = Atn(X / Sqr(-X * X + 1))Yaw(i) = Yaw(i) * 180 / pi Heave(i) = Av(i) - ((Sting_length / Sting_length - 2) * (Av(i) - FV(i))) X = (Av(i) - FV(i)) / 2Pitch(i) = Atn(X / Sqr(-X * X + 1))Pitch(i) = Pitch(i) * 180 / pi Next i Prep.Refresh StatusBar1.SimpleText = "Differentiating motions to obtain velocities at BRC" h = t(3) - t(2)For i = 3 To i - 3 $Sway_vel(i) = (1 / (12 * h)) * (Sway(i - 2) - 8 * Sway(i - 1) + 8 * Sway(i + 1) - Sway(i + 1))$ 2)) Heave_vel(i) = (1 / (12 * h)) * (Heave(i - 2) - 8 * Heave(i - 1) + 8 * Heave(i + 1) - 1)Heave(i + 1)) $Yaw_vel(i) = (1/(12 * h)) * (Yaw(i - 2) - 8 * Yaw(i - 1) + 8 * Yaw(i + 1) - Yaw(i + 2))$ Pitch_vel(i) = (1 / (12 * h)) * (Pitch(i - 2) - 8 * Pitch(i - 1) + 8 * Pitch(i + 1) - Pitch(i + 2))

Next i StatusBarl.SimpleText = "Organizing time history for selected time segment" Lower_value = 13 / h Upper_value = 14 / h If Upper_value > i Then Upper_value = i StatusBarl.SimpleText = "Done" End Sub

```
Private Sub Picture4_Click()

CommonDialog1.CancelError = True

On Error GoTo ErrHandler2

CommonDialog1.filename = SaveFile + ".pmd"

CommonDialog1.ShowSave

CommonDialog1.ShowSave

CommonDialog1.Filter = "PrepShop(*.pmd)|*.pmd|"

CommonDialog1.DefaultExt = txt

File_out = CommonDialog1.filename

StatusBar1.SimpleText = "Writing Output file " + File_out

ProgressBar1.Max = Upper_value

ProgressBar1.Max = Up

ProgressBar1.Value = 0

ProgressBar1.Visible = True
```

```
Open File_out For Output As #2

Prep.Refresh

"Write #2, "Time", "Carriage Speed", "Heave", "Pich", "Sway", "Yaw", "Heave vel.",

"Pitch vel.", "Sway vel.", "Yaw vel.", "Fx", "Fy", "Fz", "Mx", "My", "Mz"

For is = Lower_value To Upper_value

ProgressBarl. Value = i

Print #2, t(i), c(i), Heave(i), Pitch(i), Sway(i), Yaw(i), Heave_vel(i), Pitch_vel(i),

Sway_vel(i), Yaw_vel(i), Fx(i), Fy(i), Fz(i), Mx(i); My(i), Mz(i)

Next i

Close #2

StatusBarl.SimpleText = "Finished"

ProgressBarl.Visible = False

ErrHandler2:
```

```
End Sub
```

Option Explicit

```
Private Sub Form_KeyPress(KeyAscii As Integer)
Prep.Show
Unload Me
End Sub
```

```
Private Sub Form_Load()

IblVersion.Caption = "Version " & App.Major & "." & App.Minor & "." &

App.Revision

IblProductName.Caption = App.Title

Timer1.Interval = 3000

End Sub

Private Sub Frame1_Click()

Prep.Show

Unload Me

End Sub

Private Sub Timer1_Timer()

Prep.Show

Unload Me

End Sub
```

APPENDIX E MATLAB FILTERING SCRIPT

The following is the MatLab script used for filtering followed by a number of plots for filtered data vs. noisy data for a selected number of runs.

```
pl=input('enter file name without extension pmd >' ,'s');
file load= [p1.'.pmd']:
eval(['load ',file_load]);
eval(['[s,co]=size(',p1,');']);
ti=eval([p1, '(:,1)']);
%figure(1)
ch=eval([p1, '(:,7)']);
[c.1]=wavedec(ch.10.'svm8');
[thr.sorh.keepapp]=ddencmp('den','wv',ch);
ch c7=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
subplot(4,1,1);plot(ti,ch);title('Heave Velocity');ylabel(' m/s')
subplot(4,1,2);plot(ti,ch_c7);title('Filtered Heave Velocity
'),ylabel('m/s')
Sfigure(2)
ch1=eval([p1,'(:,8)']);
[c, 1] =wavedec (ch, 10, 'sym8');
[thr, sorh, keepapp] =ddencmp('den', 'wv', chl);
ch_c8=wdencmp('gbl',c,l,'svm8',10,thr,sorh,keepapp);
subplot(4,1,3);plot(ti,ch1);title('Pitch Velocity');ylabel(' deg/s')
subplot(4,1,4);plot(ti,ch_c8);title('Filtered Pich Velocity
'),;ylabel('deg/s');xlabel('Time sec')
text(-2,-2,p1)
orient landscape
eval(['print ',p1,'1 -dps'])
spause
Sfigure(3)
ch=eval((p1,'(:,9)']);
[c,1]=wavedec(ch,10,'sym8');
[thr.sorh.keepapp]=ddencmp('den', 'wv',ch);
ch_c9=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
subplot(4.1.1);plot(ti,ch);title('Sway Velocity');ylabel(' m/s')
subplot(4,1,2):plot(ti,ch_c9);title('Filtered Sway Velocity '):ylabel('
m/s')
```

```
%figure(4)
chl=eval([p1,'(:,10)']);
```

```
[c, 1] = wavedec(ch1, 10, 'sym8');
[thr, sorh, keepapp] =ddencmp('den', 'wv', chl);
ch_cl0=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
subplot(4,1,3);plot(ti,ch1);title('Yaw Velocity');ylabel('deg/s')
subplot(4.1.4):plot(ti.ch c10):title('Filtered Yaw Velocity ');ylabel('
deg/s'):xlabel('Time sec')
text(0.0.pl)
orient landscape
eval(['print ',p1,'2 -dps'])
*pause
ch=eval([p1.'(:.11)']):
[c.l]=wavedec(ch.10.'svm8');
[thr, sorh, keepapp] =ddencmp('den', 'wv', ch);
ch cll=wdencmp('gbl',c,l,'svm8',10,thr,sorh,keepapp);
subplot(4,1,1);plot(ti,ch);title('Fx');ylabel(' N')
subplot(4,1,2);plot(ti,ch_cll);title('Filtered Fx ');ylabel(' N')
ch1=eval([p1,'(:,14)']);
[c.1]=wavedec(ch1,10,'svm8');
[thr.sorh, keepapp] =ddencmp('den', 'wv', ch1);
ch_c14=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
subplot(4,1,3);plot(ti,ch1);title('Mx');ylabel(' N-m')
subplot(4,1,4);plot(ti,ch_cl4);title('Filtered Mx ');ylabel(' N-
m'):xlabel('Time sec')
text(0,0,p1)
orient landscape
eval(['print ',pl,'3 -dps'])
Spause
ch=eval([p1,'(:,12)']);
[c, 1] =wavedec (ch, 10, 'sym8');
[thr, sorh, keepapp] =ddencmp('den', 'wv', ch);
ch_cl2=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
subplot(4,1,1);plot(ti,ch);title('Fy');ylabel('N')
subplot(4,1,2);plot(ti,ch_cl2);title('Filtered Fy ');ylabel(' N')
ch1=eval([p1,'(:,16)']);
[c, 1] =wavedec(ch1, 10, 'sym8');
[thr, sorh, keepapp] =ddencmp('den', 'wv', ch1);
ch_cl6=wdencmp('gbl',c,1,'sym8',10,thr,sorh,keepapp);
subplot(4,1,3);plot(ti,ch1);title('Mz');ylabel(' N-m')
subplot(4,1,4);plot(ti,ch_c16);title('Filtered Mz');ylabel(' N-
m');xlabel('Time sec')
text(1,1,p1)
orient landscape
eval(['print ',pl,'4 -dps'])
ch=eval([p1,'(:,13)']);
[c, 1] =wavedec (ch, 10, 'sym8');
```

```
[thr.sorh.keepapp]=ddencmp('den'.'wv'.ch);
ch c13=wdencmp('gbl'.c.l.'svm8'.10.thr.sorh.keepapp);
subplot(4.1.1);plot(ti.ch);title('Fz');ylabel('N')
subplot(4,1,2);plot(ti,ch cl3);title('Filtered Fz');ylabel(' N')
ch1=eval([p1,'(:.15)']):
[c,1]=wavedec(ch1,10,'svm8');
[thr.sorh.keepapp]=ddencmp('den', 'wv', ch1):
ch_cl5=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
subplot(4,1,3);plot(ti,ch1);title('My');ylabel(' N-m')
subplot(4.1.4):plot(ti.ch c15):title('Filtered My'):vlabel(' N-
m'):xlabel('Time sec')
text(1.1.pl)
orient landscape
eval(('print '.pl.'5 -dps'))
**pause
ch=eval([p1,'(:,2)']);
[c, 1] =wavedec (ch. 10, 'svm8');
[thr, sorh, keepapp]=ddencmp('den', 'wv', ch);
ch_c2=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
**pause
ch_cl=eval([p1.'(:.1)']);
ch3=eval([p1,'(:,3)']);
[c,1]=wavedec(ch3,10,'sym8');
[thr.sorh.keepapp]=ddencmp('den', 'wv', ch3);
ch_c3=wdencmp('gbl',c,l,'svm8',10,thr,sorh,keepapp);
ch3=eval([p1.'(:.4)']):
[c.1]=wavedec(ch3.10.'svm8');
[thr.sorh,keepapp]=ddencmp('den','wv',ch3);
ch_c4=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
ch3=eval([p1,'(:.5)']):
[c,1]=wavedec(ch3,10,'svm8');
[thr, sorh, keepapp] =ddencmp('den', 'wv', ch3);
ch_c5=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
ch3=eval([p1,'(:,6)']);
[c.1]=wavedec(ch3,10,'sym8');
[thr, sorh, keepapp] =ddencmp('den', 'wv', ch3);
ch_c6=wdencmp('gbl',c,l,'sym8',10,thr,sorh,keepapp);
subplot(2,2,1);plot(ti,ch_c3);title('Heave Disp.');ylabel('Heave m')
subplot(2.2.3):plot(ti,ch_c4):title('Pitch Displ.'):ylabel('Pitch deg')
subplot(2,2,2);plot(ti,ch_c5):title('Sway Disp.');ylabel('Sway m')
subplot(2,2,4);plot(ti,ch_c6);title('Yaw Displ.');ylabel('Yaw
deg'):xlabel('Time sec')
text(1..5.p1)
orient landscape
eval(['print ',p1,'6 -dps'])
Filesave=[p1.'.flt']:
matrix=[p1.'a']
eval([matrix,'=[ch_c1 ch_c2 ch_c3 ch_c4 ch_c5 ch_c6 ch_c7 ch_c8 ch_c9
ch_c10 ch_c11 ch_c12 ch_c13 ch_c14 ch_c15 ch_c16];']);
eval(['save ',Filesave,' ',matrix,' -ascii -double -tabs ;']);
```
















