

VERTICAL AND INCLINED EDGE-INDENTATION
OF FRESHWATER ICE SHEETS

CENTRE FOR NEWFOUNDLAND STUDIES

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DAVID W. FINN, B.Eng.



**VERTICAL AND INCLINED
EDGE-INDENTATION OF
FRESHWATER ICE SHEETS**

BY

©David W. Finn, B. Eng.

**A thesis submitted to the School of Graduate
Studies in partial fulfillment of the
requirements for the degree of
Master of Engineering**

**Faculty of Engineering and Applied Science
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ABSTRACT

A series of freshwater ice indentation experiments were performed with stiff vertical and downward-breaking inclined indentors in the ice tank at the Institute for Marine Dynamics in the fall of 1989. Indentor width, indentor angle, indentor velocity and ice sheet thickness were varied for a total of 94 tests. Three forces, one moment, three accelerations, indentor displacement, and carriage speed were measured. High sampling rates were used to capture the dynamics of the indentor response. Crushed ice extruded in front of the indentor was collected and sieved whenever possible.

Failure modes of crushing, radial cracking, circumferential cracking, spalling and in-plane cleavage were all observed during vertical indentation. The maximum force on the structure was 29.1 *kN*. Analysis of peak pressures revealed good agreement with data collected by previous researchers. Peak pressures (averaged over the indentor area) ranged from 4 to 11 *MPa*. A slight decrease in peak pressures with increasing aspect ratio was observed. The small range of contact areas used in the test series produced no evidence of a pressure-area relationship. Peak pressure increased slightly with velocity, up to speeds of 50 *mm/s*. At velocities higher than 50 *mm/s* the indentor began to vibrate steadily and peak pressures dipped slightly. Significant vibrations were induced in the structure by crushing failure of the ice. Crushing frequency varied proportionately with velocity at low velocities. At velocities above 50 *mm/s* the response became locked at the natural frequency of the structure. An unusual "double-beat" force-time trace was sometimes observed during this locked-in response, and spectral analysis of the signal revealed the emergence of a higher second frequency in the vibration of the structure.

For the inclined indentation tests, mixed failure modes of crushing and flexural failure were observed. For low indenter angles, crushing dominated. For high indenter angles flexural failure dominated, with crushing still occurring during many tests. Flexural failure was characterized by the formation of a principal circumferential crack and one or two "subsidiary" circumferential cracks. The formation of these subsidiary cracks was due to high in-plane forces combined with vertical deflection of the ice sheet to produce shear and buckling failure. The failure mode underwent transition from bending to crushing as velocity increased, ice thickness increased, and indenter angle decreased. The maximum horizontal force on the structure was 32.7 kN, produced with a 10° indenter while crushing failure was occurring. The normalized peak horizontal force exerted on the inclined indentors increased as the indenter approached vertical. The broken ice pieces produced by flexural failure were between 5% and 40% of the characteristic length of the ice sheet. The dynamic effect of decreasing broken piece size with increasing velocity was not clearly demonstrated.

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List of Symbols

| | |
|------------|---|
| α | indenter angle from vertical |
| ϕ | indenter-ice friction angle |
| ρ | ice density |
| σ_f | flexural strength of ice |
| ζ | structural damping |
| A | apparent contact area |
| a_C | acceleration of the carriage |
| a_I | acceleration of the structure at the indenter |
| a_{TF} | acceleration of the structure at the test frame |
| D | indenter width |
| E | elastic modulus of ice |
| F_x | horizontal force on indenter face |
| F_y | horizontal force on indenter side |
| F_z | vertical force on indenter face |

| | |
|------------|--|
| f | characteristic failure frequency |
| f_n | structure natural frequency |
| H | normalized peak horizontal force |
| h | ice thickness |
| K | stiffness of the structure |
| K_I | stiffness of the ice sheet |
| L_c | characteristic length of ice sheet |
| l | damage length |
| M_y | moment due to F_x |
| P_{peak} | peak horizontal pressure |
| u | indenter displacement with respect to carriage |
| V | indenter velocity |

Chapter 1

INTRODUCTION

The design of many engineering structures intended for operation in Canada's offshore or inland waterways is complicated significantly by the presence of ice. Canada's East and North Coasts and thousands of rivers and lakes become ice-bound for a major part of the year, and ice-going vessels, fixed and floating offshore oil and gas platforms, lighthouses, bridges and other marine structures must be built to withstand the rigours of this environment. With increasing exploration and development of natural resources in the Canadian Arctic and off the eastern seaboard, the amount of research on ice-related engineering problems has grown proportionately. Recently, the problem of structural vibration caused by cyclic ice failure processes (particularly crushing) has come under particular scrutiny. These vibrations can lead to structural fatigue and failure; instigate the liquefaction and failure of a fixed structure's soil foundation; induce superstructure motions capable of impeding operation of drilling derricks and other equipment; and cause severe discomfort for crew-members and passengers of ice-going vessels. In March of 1986 an ice-structure interaction featuring periodic crushing around the caisson-

retained drilling structure *MOLIKPAQ* in the Beaufort Sea threatened the safety of the rig and forced evacuation. The magnitude of the forces exerted on the structure was not threatening, but the periodic nature of the crushing event caused partial liquefaction of the structure's sand core. This event revealed that the dynamic nature of ice crushing activity can pose a serious problem for offshore structures and must be taken into account when designing these structures.

The purpose of the present research is to study the dynamic behaviour of structures during freshwater ice indentation. Specifically, to enable more accurate prediction of the forces exerted on a structure and the response of a structure subjected to this type of loading. To accomplish this, a series of tests were performed in the ice tank of the Institute for Marine Dynamics in St. John's, Newfoundland. The test programme was divided into two areas: vertical indentation and inclined indentation. Three vertical indentors of different widths, and four downward-breaking inclined indentors of varying slope were used in the tests for the following purposes:

1. to examine the effects of velocity and aspect ratio (the ratio of structure width to ice thickness) on ice forces and failure mode during vertical indentation.
2. to examine the effects of velocity and aspect ratio on the crushing failure frequency of the ice sheet and the response of the structure during vertical indentation.
3. to examine the effects of velocity and indenter angle on ice forces and failure mode (particularly the transition from flexural to crushing failure) during inclined indentation.
4. to examine the effects of velocity and indenter angle on the size of the broken ice pieces created by flexural failure during inclined indentation.
5. to examine the effects of velocity, indenter angle and ice thickness on the failure frequency of the ice sheet during inclined indentation.

The thesis is divided into four main sections. A review of the literature relevant to small scale vertical and inclined indentation and associated dynamics will be followed by a detailed description of the experimental work performed. The presentation of results and subsequent analysis for vertical and inclined indentation will be done in two separate sections.

Chapter 2

LITERATURE REVIEW

2.1 Introduction

Ice behaves as a visco-elastic material when its interaction with a structure takes place at low relative velocities: the energy of interaction is dissipated by creep mechanisms such as grain-boundary sliding and the movement of dislocations within a single ice crystal. At higher relative velocities the ice behaves as a brittle material, breaking into discrete pieces during interaction with the structure. The size of these discrete pieces can vary from fractions of a millimeter to kilometers, depending on the interaction velocity, geometry and ice properties. The way the ice breaks is described by a particular failure mode such as crushing, buckling or bending. More importantly, the force required to break the ice can vary considerably, depending on the mode of ice failure. This review focusses on the interaction of ice with vertical and inclined structures in the brittle failure regime.

2.2 Vertical structures in ice

The failure mode of ice encountering an advancing vertical structure in a brittle indentation mode has been investigated by many researchers. The geometry of vertical indentation is shown in Figure 2.1. For static design purposes, the peak pressure exerted on a structure during indentation is of most importance. This pressure is directly related to the ice failure mode, which in turn is dependent on indentation velocity (V), aspect ratio (D/h), the ice-structure friction angle (ϕ), the degree of contact between structure and ice, and the size of the structure and ice. For a narrow vertical structure in contact with a confined ice mass, crushing is the dominant failure mode in brittle indentation. Crushing can occur by itself or with other failure mechanisms, and is the failure mode responsible for exciting a large structural response during dynamic interactions. The following description of the ice crushing process, illustrated in Figure 2.2, is based on the work of Jordaan and Timco (1988). When contact occurs and a force is developed at the ice-structure interface, the structure deflects elastically and the ice viscoelastically. Energy is stored in both the structure and ice. Microcracking begins in the grain boundaries and within grains of the ice. These cracks grow and finally coalesce, instantaneously forming a thin layer of small crushed ice particles immediately in front of the structure. Upon crushing, the structure and parent ice sheet rebound and squeeze out the mass of crushed ice in a rapid extrusion process. As the crushed ice is cleared from the ice-structure interface, a thin layer of particles may be sintered together by the frictional melting and high local pressures of extrusion, presenting a porous, fused ice mass to the advancing indenter. At some point the structure once again encounters a "solid", albeit damaged, ice mass and the cycle begins again. The "solid" ice sheet in this case is not a virgin

undamaged ice sheet, but a highly-damaged mass of ice which may behave as a viscous material.

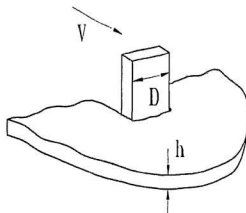


Figure 2.1: *Vertical indentation geometry*

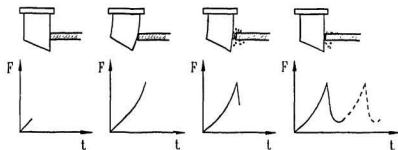


Figure 2.2: *Cyclic ice crushing process for a vertical indenter*

Timco (1936) conducted a series of freshwater indentation tests in the brittle mode with flat vertical indentors and identified five main failure modes, four of

which include crushing as one of the primary failure mechanisms:

1. Pure crushing - The ice directly in front of the indenter is broken into a mass of fine discrete particles. There is little or no radial cracking, but the intact ice beyond the crushed region is damaged by microcracking. This failure mode dominates when the ice is highly confined, i.e. at low aspect ratios.
2. Crushing with spalling - In addition to crushing, large chips are broken off the surface of the ice sheet immediately in front of the indenter.
3. Crushing with radial cracking - In addition to crushing, large radial cracks emanate from the indenter into the intact ice sheet.
4. Crushing with radial and circumferential cracking - In addition to crushing and radial cracking, circumferential cracks form at some distance from the indenter due to flexural stresses placed on the ice. Roughly triangular broken ice pieces are formed by the radial and circumferential cracks.
5. Radial and circumferential cracking with buckling - At lower velocities, negligible amounts of crushing occur and the ice fails in buckling, resulting in the formation of radial and circumferential cracks.

Any of these failure modes can dominate under specific indentation conditions. Nakazawa and Sodhi (1990) recently conducted a series of flat vertical freshwater indentation tests and observed similar failure modes. Another failure mode, observed by Michel and Blanchet (1983) and Nakazawa and Sodhi (1990) is that of cleavage. In this mode, a large semi-circular crack is formed immediately in front of the indenter in the plane of the ice sheet. This type of failure may occur occasionally, but cannot be considered a continuous failure mode. The five primary failure modes, and cleavage, are illustrated in Figure 2.3.

A useful representation of the variation in failure mode with indentation parameters is a deformation-mode map, which shows the type of ice failure as a function of indentation rate and aspect ratio. For any single indentation test, the interaction velocity and aspect ratio are usually held constant. For a series of



PURE CRUSHING



CRUSHING WITH SPALLING



CRUSHING WITH
RADIAL CRACKING



BUCKLING



CRUSHING WITH
RADIAL AND
CIRCUMFERENTIAL
CRACKING



CLEAVAGE

Figure 2.3: Ice failure modes during vertical edge-indentation (after Timco, 1986)

tests, velocity and aspect ratio can be varied over a considerable range of values to derive a deformation-mode map such as that seen in Figure 2.4 (after Timco, 1986).

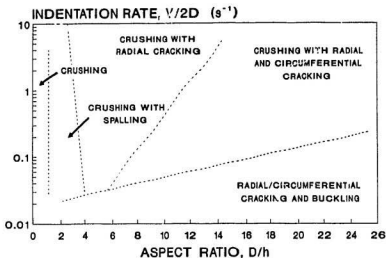


Figure 2.4: *Deformation-mode map of ice failure showing dominant failure modes at various aspect ratios and strain rates (after Timco, 1986)*

Timco compared his results with those of Zablnsky *et al.* (1975), Hirayama *et al.* (1974) and Michel and Blanchet (1983), who all conducted similar experiments. For all the tests, it was found peak pressure (averaged over indenter area) decreased with increasing aspect ratio from about 14 MPa at $D/h = 0.4$ to about 2 MPa at $D/h = 80$. Peak pressure decreased slightly with increasing contact area ($A = Dh$), from about 8 MPa at $A \approx 2 \text{ cm}^2$ to about 6 MPa at $A \approx 200 \text{ cm}^2$. This trend of decreasing pressure with increasing contact area was not found by Nakazawa and Sodhi (1990), probably due to the limited variation in contact area

for their experiments.

The peak pressure exerted on the structure can be dependent on interaction velocity. Peak pressure increases almost linearly with velocity in the ductile regime, reaches a peak during the transition from ductile to brittle failure and then drops slightly to a value which remains relatively constant as velocity increases throughout the brittle failure regime. Timco (1986) found a slight decrease in peak pressure with increasing velocity, while Nakazawa and Sodhi (1990) report an increase in maximum peak pressure with increasing velocity.

Design for dynamic loading of structures in ice requires knowledge of not only the magnitude of the ice force, but the variation in force with time. Structures have generally been categorized as either rigid or flexible in the past, but a strict definition for a flexible structure does not exist. No structure is perfectly rigid, but some can be considered very stiff when compared to the stiffness of the ice sheet. The flexibility of the structure can have a significant effect on the structure's response and the determination of the response force of the structure. Frederking and Timco (1987) report significant magnification of forces between the point of application (indenter face) and the foundation for "flexible" structures, while "rigid" structures do not exhibit this magnification. There are two predominant explanations of ice-induced vibrations found in the literature: the tendency of ice to crush into particles of a certain size, and the "negative damping" (or self-excited) model for flexible structures proposed by Blenkarn (1970) and refined by Määttänen (1978) and others. Both will be reviewed here.

Peyton (1968) studied the oscillatory nature of ice forces on oil drilling platforms in Cook Inlet, Alaska. He observed a cyclic, ratcheting ice failure at a frequency of about 1 Hz, which was also the natural frequency of the test platform. After conducting further tests in a laboratory environment where the ice

failure frequency remained at 5 Hz despite variations in the structure's natural frequency, he concluded that the failure frequency was a basic property of the ice only, known as the "characteristic failure frequency". Peyton also found that the maximum ice forces and the ice compressive strength decreased with increasing velocity. Neill (1976) stated that the ice tends to break into pieces of a certain size, and this size distribution at a particular velocity produces a characteristic frequency spectrum. This may be true when large ice fragments are created, such as in spalling, but the size of the fine particles produced by crushing are unlikely to be directly reflected in the failure frequency.

The average length of ice crushed per cycle, called the "damage length" l , is often found as the ratio of the velocity to the dominant failure frequency:

$$l = \frac{V}{f} \quad (2.1)$$

This formulation assumes that the distance travelled by the indenter between failure peaks is equal to the length of ice crushed in every cycle, and that all the crushed material is ejected from the ice-structure interface. In reality, a portion of the length of crushed ice may be sintered together at the end of the extrusion cycle to form a highly viscous mass between the indenter and the original "intact" ice. Michel (1978) found from his experiments that the damage length was between 25% and 50% of the ice thickness ($0.25h$ to $0.5h$). Sodhi and Morris (1986) conducted indentation experiments in urea-doped ice and used spectral analysis of the force-time records to determine the characteristic crushing frequency. They found that this frequency increased linearly with respect to the ratio of velocity to ice thickness, and the typical damage length was between $0.2h$ and $0.5h$. The shape and the size of the crushed layer depends on the degree of confinement at the ice-structure interface (Singh, 1990). The flexibility of the structure also has an

important effect on the thickness of the crushed layer. A highly flexible structure will store more elastic energy (subsequently released when the ice fails) and create a thicker crushed layer than a geometrically similar and stiffer structure.

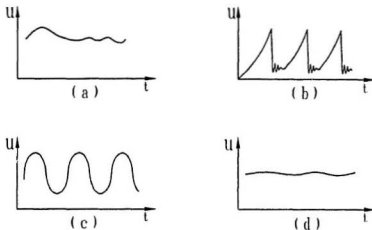


Figure 2.5: *Idealization of force-time histories for four modes of structural response: (a) creep mode; (b) intermittent crushing; (c) continuous crushing; (d) continuous crushing at high velocity (after Kärnä and Turunen (1990))*

Toyama *et al.* (1983) performed a series of indentation tests by forcing saline ice sheets against single- and double-pile configurations with variable natural frequencies. They found that the crushing frequency increased with velocity until it reached the natural frequency of the structure. At this point the crushing frequency (and structural vibrations) remained at the natural frequency despite further increases in velocity. This phenomenon became known as “lock-in”. Tsuchiya *et al.* (1985), Singh *et al.* (1990) and Kärnä and Turunen (1990) also observed the same lock-in behaviour. Kärnä and Turunen summarized the four observed modes of structural response to ice loading and discussed the lock-in phenomenon

in detail. At extremely low velocities where creep behaviour dominates, a constant structural deflection occurs, such as shown in Figure 2.5(a). When velocity increases such that ice fails in the brittle regime, the structure usually oscillates in a sawtooth-type manner due to intermittent crushing (Figure 2.5(b)). When the interaction velocity is high enough to induce locking-in of the ice crushing frequency at the natural frequency of the structure, the structural response is a steady harmonic vibration (Figure 2.5(c)). For extremely high ice velocities the structure can no longer respond at the exciting frequency at which the ice crushes, and breaks out of the lock-in phenomenon. The response amplitude decreases significantly to an almost constant deflection (Figure 2.5(d)) caused by the average ice load. This final response mode has been achieved rarely in experimental work, and Sodhi (1989) has published the only evidence of it to date. Kärnä and Turunen developed a model incorporating the crushing and clearing theory of Jordaan and Timco (1988) which correctly predicts these response modes for interactions dominated by the crushing mode of failure.

The negative damping or self-excited theory was first proposed by Blenkarn (1970) after studying extensive ice force data acquired on platforms in Cook Inlet, Alaska. He noted that the measured ice forces were random in nature, while the structure responded at its natural frequency in a periodic manner. This led him to believe that this dynamic response was due to structural characteristics as well as ice properties, i.e. structural vibrations were self-excited. Like Peyton, he noted that the ice compressive strength decreased with increased loading rate and used the concept of negative damping in a single-degree-of-freedom model of the structure's behaviour. Negative apparent damping dictates that the amplitude of structural oscillations becomes progressively higher in a particular velocity range. As velocity increases the damping becomes positive and the vibration amplitude

reaches a limit (Frederking, 1989). Määttänen (1978) extended the self-excited model to a multi degree of freedom system capable of predicting saw-tooth force-time histories and their frequencies at low velocities. Other researchers (Eranti *et al.*, 1981; Toyama *et al.*, 1983; Daoud and Lee, 1986) have also developed refinements and variations of the self-excited model. Sodhi (1988) summarized a number of objections to the self-excited model. The self-excited model assumes the excitation force induced by ice failure to be dependent only on the relative velocity between the structure and ice, ignoring the effects of relative displacement, time-dependence, changing contact area and damage beyond the crushed layer. The excitation force in the brittle failure mode is especially dependent on these other factors ignored by the self-excited model. Another objection, raised by Singh *et al.* (1990), is that the negative damping model ignores the large damping of structural oscillations by the presence of the crushed ice material at the ice-structure interface. The clearing of the crushed material, an important part of the overall indentation process, is not included in the model.

2.3 Inclined structures in ice

When an inclined structure comes into contact with a confined ice mass, a new failure mode (flexure) can occur which changes the ice-structure interaction. The loads on a structure encountering flexural failure are much lower than those experienced from crushing failure.

The following description of the interaction between a downward-breaking inclined indenter and a level ice sheet is based on Sørensen (1977) and Jebaraj *et al.* (1990). As the sloping surface of the indenter contacts the edge of the ice sheet local crushing and extrusion occur at the ice-structure interface in a cyclic

fashion as for a vertical indenter (see Figure 2.6). With each crushing and clearing cycle, however, the apparent contact area increases and the resulting force-time sawtooth pattern will exhibit larger successive peaks. At the same time as this local crushing occurs, the ice sheet is being forced downwards by the structure and flexural stresses are induced in the ice at some distance from the ice-structure interface. Radial cracks sometimes form in the ice sheet, usually emanating from the corners of the indenter. When the flexural stress in the ice sheet exceeds the strength of the ice, a circumferential crack forms at a finite distance from the structure and the force on the structure drops to that required to clear the broken ice pieces. When the structure again reaches the edge of the ice sheet, the cycle repeats. Flexural failure results in the formation of a small number of large broken ice pieces compared to crushing failure where an extremely large number of tiny particles are formed. The flexural failure process exerts smaller forces on the structure than crushing failure.

Most experimental work on inclined structures has been conducted on cones, either upward- or downward-breaking (eg. Hirayama and Obara, 1986). Experiments with flat indentors have included Zabilansky *et al.* (1975), Sørensen (1977), Haynes *et al.* (1983), Timco (1984), Frederking and Timco (1985), Michel and Picard (1987) and Valanto (1989). The primary focus in this review will be on the effects of indenter angle (α), ice thickness (h) and velocity (V) on the peak horizontal force and broken ice piece size.

The peak horizontal force is usually normalized with respect to the flexural strength of the ice (σ_f) and the square of the thickness (h) to obtain the normalized peak horizontal force, H :

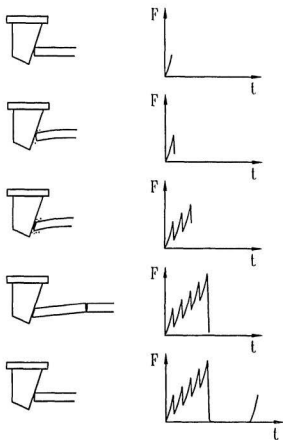


Figure 2.6: *Idealized interaction between an inclined structure and edge-loaded ice sheet*

$$H = \frac{F_{x_{proj}}}{\sigma_f h^2} \quad (2.2)$$

Haynes *et al.* (1983) used narrow indentors and varied velocity from 0 - 100 mm/s. They found that the normalized horizontal force H was dependent on indenter angle, increasing dramatically as indenter angle decreased below 20° from the vertical. Hirayama and Obara (1986), summarizing data from several experiments with cones, observed the same dramatic increase in H at slightly higher angles. The increase in H with decreasing indenter angle is expected as the failure mode changes from flexure to crushing as the structure approaches vertical. Vertical loading is responsible for flexural failure and horizontal loading is responsible for crushing failure. As α decreases the horizontal component of the total load will increase and the vertical component will decrease. If the inclination is sufficiently small, crushing may dominate. Both Zabilansky *et al.* (1975) and Bercha and Danys (1975) (conical indenter) observed the transition from flexure to crushing with decreasing indenter angle. Jebaraj *et al.* (1989) noted that the ice failure mode is also influenced by the thickness of the ice sheet. The thickness of the ice sheet will have a large effect on the flexural strength of the ice and consequently how great a load can be supported before flexural failure occurs. Simply, if the crushing or shear strength of the ice is less than the flexural strength, the failure mode will likely become dominated by crushing and shear, and H will increase dramatically.

Valanto (1989) examined the dynamic effects of velocity on the failure process using a planar indenter in Wärtsilä Arctic Research Centre (WARC) Fine Grain (FG) model ice. As the indenter strikes the ice edge, the sheet is deflected downwards and the water underneath resists this deflection. As the indenter velocity increases, the downward acceleration of the ice sheet increases and the hydrody-

dynamic inertia increases, and the load on the indenter increases. Valanto noted that the peak force on the indenter was caused by hydrodynamic inertia at the first impact of the indenter, and that this peak force increased almost linearly with increasing velocity. The failure mode for all Valanto's tests was flexure, and he noted no increase in average force with velocity.

The increase in hydrodynamic resistance with velocity also contributes to the transition from flexure to crushing and the corresponding increase in H . Flexural stresses which lead to bending failure in the ice are caused by out-of-plane deflections of the ice sheet. As the vertical load required to deflect the ice sheet increases with velocity, the horizontal component of the total load must correspondingly increase. If this horizontal component exceeds the crushing or shear strength of the ice before the ice can be deflected enough to fail in bending, the failure mode will change from flexure to crushing or shear, and H will correspondingly increase. Lipsett and Gerard (1980) and Haynes *et al.* (1983) observed transitions in failure mode from flexure to crushing with increases in velocity.

The size of the broken ice pieces created by flexural failure is dictated by the point of circumferential cracking. Frederking and Timco (1985), conducting tests with a 1 m wide inclined indenter in urea-doped ice, found that the circumferential crack forms at approximately 75% the characteristic length of the ice. Michel and Picard (1987), conducting tests with 100 to 200 mm wide inclined indentors in freshwater ice, found breaking lengths between 80% and 175% of the characteristic length. Sørensen (1978) and Valanto (1989) examined the dynamic effects of velocity on the length of broken ice piece. The increase in hydrodynamic resistance with velocity effectively increases the stiffness of the ice sheet. Consequently, the radius of circumferential cracking will decrease and smaller broken ice pieces will be produced. Sørensen and Valanto's tests both verified a reduction in broken

ice piece size with increasing indenter velocity. Sørensen's piece size was usually between 10% and 30% of the characteristic length of the ice sheet, but reached as high as 80%.

The most important frequency in the flexural failure process is the "single icebreaking frequency", defined by Ettema and Stern (1989) as the ratio of velocity to the distance travelled between two flexural failure events. Correspondingly, the "single icebreaking period" ($1/f$) multiplied by the indenter velocity can be used to estimate the size of the ice pieces broken during flexural failure events.

Chapter 3

EXPERIMENTAL WORK

3.1 Test Facility

The experiments were performed in the ice tank of the Institute for Marine Dynamics (IMD) at St. John's, Newfoundland from September 25 to October 6, 1989. The IMD ice tank is 96 *m* long, 12 *m* wide and 3 *m* deep. One end of the tank can be thermally isolated by a large sliding door, producing a bay which is used to house the carriage when no tests are in progress. It also allows test preparation such as indenter changing and transducer mounting to be performed in a comfortable environment. The usable ice sheet grown on the basin is 76 *m* long, and extends from the carriage bay to the melting pit at the far end of the tank.

The carriage itself is 15 *m* long, 14.2 *m* wide, 3.9 *m* high and weighs 80 tonnes (Jones, 1987). The carriage is driven along steel rails by either a rack-and-pinion drive system or a friction-drive system. Both drives are powered by electric motors. There are two operating regimes. In the high-speed operating range (20

- 4000 mm/s), the carriage is driven by 4 motors and velocity can be maintained with an accuracy of 0.1%. In the low-speed operating range (0.2 - 40 mm/s), the carriage is driven by 2 motors and velocity can be maintained within 0.5%. Up to eight different speeds can be tested in a single run. Each individual speed, the distance moved at this speed, and the carriage acceleration are programmed into the computer before each run, and the computer subsequently controls carriage motion during the test. Mounted on the carriage is a test frame which can be raised and lowered to facilitate test preparation and allow precise draft setting for testing. This frame can also be moved laterally to allow testing at the quarter points of the tank width, as well as along the centerline. For this test series all runs were done along the centerline.

3.2 Instrumentation and Data Acquisition

Seven indentors were manufactured from 3/4" mild steel: 80 mm , 100 mm and 120 mm wide vertical indentors and 30°, 20°, 10° and 5° downward-breaking inclined indentors all of 120 mm width. The vertical indentors can be considered as having 0° inclination. No special treatment or coating was provided to indenter surfaces. The combinations of indenter width and ice thickness were chosen to generate forces that would approach the design limit of the towing carriage. Since the maximum design carriage load applied at centerline is 60 kN , a target force of 40 kN was used, providing a margin of safety.

For each test, the indenter was securely bolted to a 44.5 kN AMTI 6-component load cell which was in turn attached to the towing carriage via a test-frame extension (see Figure 3.1). Only four components were measured for this test series: the horizontal forces (F_x forward, F_y sideways), the vertical force (F_z), and

the moment about the y -axis (M_y). Three accelerometers were mounted on the arrangement: one at the indenter just above the waterline (acceleration at the indenter a_I), one at the test frame immediately above the load cell (acceleration of the test frame a_{TF}), and one on the main carriage body (acceleration of the carriage a_C). A linear-voltage-displacement-transducer (LVDT) mounted on a separate post on the carriage measured the displacement u of the indenter relative to the carriage. Displacement in the direction of positive F_x loading is considered positive. Initially, a string potentiometer ("yo-yo") was mounted on a platform on the ice several meters ahead of the indenter to measure the displacement of the indenter relative to the fixed ice sheet. Examination of the acquired data revealed that the "yo-yo"'s spring response was not capable of capturing the indenter's oscillations, and the only displacement recorded was that of the carriage. The use of the "yo-yo" was subsequently abandoned.

Tests were performed at eight speeds: 400, 200, 100, 50, 20, 10, 2 and 0.2 mm/s. "High-speed" tests (400 - 50 mm/s) were sampled at 2000 Hz and passed through a 1000 Hz anti-aliasing filter. "Low-speed" tests (20 - 0.2 mm/s) were sampled at 200 Hz and filtered at 100 Hz. This reduction in sampling rate was required because the longer test times associated with the slower speed tests would have produced exorbitantly large data files, filling the acquisition system's available memory before all speeds could be tested. A NEFF System 620 Series 300 signal conditioner provided excitation voltage to all the measuring instrumentation. The resulting analog signals were amplified and digitized by a NEFF System 620 Series 100 amplifier/multiplexer and stored on a VAX 11/750 computer, and a KYOWA RTP-600B 14-channel tape recorder for back-up purposes.

Three video cameras recorded the tests. One was positioned underwater and ahead of the indenter, another filmed the tests from the side of the carriage and

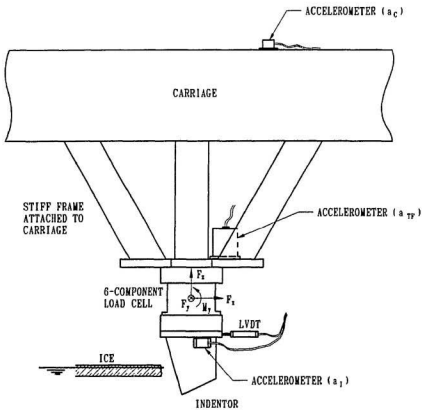


Figure 3.1: *Test arrangement*

the final camera filmed from the front of the carriage. For inclined indenter tests a fourth camera filmed the channel behind the indenter to record the size of the broken ice pieces. A still camera was mounted above and in front of the indenter to photograph cracking patterns in the ice sheet illuminated by underwater lighting.

3.3 Experimental procedure

An even edge was cut in the ice sheet using a pruning saw and the indenter advanced to the interface. The four "high-speed" (50-400 mm/s) tests were run consecutively in order of increasing speed, crushing 2 m of ice at each velocity. Crushed ice samples were collected for most tests and sieved immediately afterwards to determine the size distribution of the crushed particles.

A new interface was cut and the four "low-speed" (20 - 0.2 mm/s) tests were performed in order of decreasing speed, and when *dry* crushed ice was produced it was collected and sieved. For the 20 and 10 mm/s tests, a 2 m length of ice was crushed. The time required to crush 2 m of ice at both the 2 and 0.2 mm/s speeds would have resulted in the saturation of the data acquisition system's storage capacity before the lowest speed was reached. Consequently, time limits of 400 and 500 seconds (corresponding to ice lengths of 0.8 m and 0.1 m) were placed on the velocities of 2 and 0.2 mm/s respectively. A total of 94 successful tests were performed with variations in carriage speed (V), ice thickness (h), indenter width (D) and indenter angle (α). For several attempted tests the carriage was unable to maintain the programmed velocity, and on three occasions was unable to progress through the ice at all. Significant fluctuations in carriage speed occurred for almost all tests at 20 mm/s and 10 mm/s , and the data was not included in the analysis. The low-speed carriage operating system was used for these tests,

and the two drive motors could not maintain steady velocity due to the fluctuating nature of the ice load. Table 3.1 (vertical) and Table 3.2 (inclined) provide detailed test matrices.

To determine the natural frequency of the indenter and support structure step unloading, or “plucking”, tests were performed with the indenter in air and water. A rope was secured around the indenter, led through a pulley arrangement to the end of the tank and a 200 *kg* weight suspended from the end. The rope was suddenly cut, effectively “plucking” the indenter to set it oscillating at its natural frequency. These oscillations were sampled at 2000 *Hz*, passed through a 1000 *Hz* anti-aliasing filter, and recorded for future analysis. The indenter displacement, indenter acceleration and F_z signals were subjected to spectral analysis and the natural frequency of the structure, f_n , was found to be approximately 63 *Hz*. Structural damping ζ was 4.6% ($\zeta = 0.046$), and the stiffness of the structure K was $9.4 \times 10^6 \text{ N/m}$ (9.4 *kN/mm*).

3.4 Ice properties

Six freshwater ice sheets were grown with a wet-seeding process which produces a fine-grained S2, strictly columnar ice. The temperature inside the tank was lowered to -20°C , and a mist of warm water droplets sprayed into the air. These droplets freeze and drop to the water surface to produce a fine-grained skim of ice, and these grains act as nuclei for columnar growth. The tank was kept at -20°C until the target ice thickness was reached. Since freshwater ice was used, no warm-up or tempering was required, and the tests were conducted at -5°C . After testing, ice samples were immediately taken and stored in IMD’s cold room for thin-sectioning. The average grain size was determined from these thin sections

| TEST | Indenter width (mm) | Ice thickness (mm) | Aspect ratio (D/h) | Test speed (mm/s) | Mean force (kN) | Peak force (kN) |
|----------------|---------------------|--------------------|--------------------|-------------------|-----------------|-----------------|
| Fresh1-HI-Run2 | 80 | 27.5 | 2.78 | 50 | 0.09 | 12.89 |
| Fresh1-LO-Run2 | | | | 10 | 3.50 | |
| Fresh1-HI-Run3 | | | | 100 | 0.36 | |
| Fresh1-LO-Run3 | | | | 2 | 8.28 | |
| Fresh2-HI-Run1 | 80 | 35.9 | 2.23 | 0.2 | 4.96 | 12.21 |
| | | | | 400 | 0.61 | |
| | | | | 200 | 0.50 | |
| | | | | 100 | 0.48 | |
| Fresh2-LO-Run1 | 100 | 35.9 | 2.79 | 50 | 0.98 | 22.35 |
| | | | | 2 | 12.46 | |
| | | | | 0.2 | 9.71 | |
| | | | | 400 | 0.71 | |
| Fresh2-HI-Run2 | 120 | 26.7 | 4.49 | 200 | 0.53 | 26.97 |
| | | | | 100 | 0.43 | |
| | | | | 50 | 1.02 | |
| | | | | 2 | 13.42 | |
| Fresh2-LO-Run2 | 100 | 26.7 | 3.75 | 0.2 | 9.90 | 21.82 |
| | | | | 400 | 0.65 | |
| | | | | 200 | 0.50 | |
| | | | | 100 | 0.47 | |
| Fresh3-HI-Run1 | 80 | 46.3 | 1.73 | 50 | 0.85 | 18.92 |
| | | | | 2 | 9.47 | |
| | | | | 0.2 | 6.16 | |
| | | | | 400 | 0.48 | |
| Fresh3-LO-Run1 | 100 | 26.2 | 3.05 | 200 | 0.40 | 15.26 |
| | | | | 100 | 0.35 | |
| | | | | 50 | 0.84 | |
| | | | | 2 | 8.98 | |
| Fresh3-HI-Run2 | 80 | 35.6 | 2.81 | 0.2 | 5.17 | 16.67 |
| | | | | 400 | 17.09 | |
| | | | | 2 | 25.25 | |
| | | | | 0.2 | 21.70 | |
| Fresh4-LO-Run4 | 100 | 26.2 | 4.58 | 400 | 6.71 | 19.75 |
| | | | | 200 | 5.45 | |
| | | | | 100 | 5.00 | |
| | | | | 50 | 20.89 | |
| Fresh5-HI-Run5 | 80 | 26.2 | 3.82 | 400 | 3.26 | 10.53 |
| | | | | 200 | 3.56 | |
| | | | | 100 | 2.87 | |
| | | | | 50 | 3.18 | |
| Fresh6-HI-Run1 | 100 | 26.2 | 3.82 | 2 | 7.39 | 13.96 |
| | | | | 0.2 | 2.68 | |
| | | | | 400 | 5.68 | |
| | | | | 200 | 4.05 | |
| Fresh6-LO-Run2 | 120 | 26.2 | 4.58 | 100 | 3.98 | 12.31 |
| | | | | 50 | 6.44 | |
| | | | | 2 | 7.75 | |
| | | | | 0.2 | 7.14 | |
| Fresh6-HI-Run3 | 80 | 26.2 | 3.82 | 400 | 6.06 | 19.90 |
| | | | | 200 | 4.64 | |
| | | | | 100 | 4.32 | |
| | | | | 50 | 8.96 | |
| Fresh6-LO-Run3 | 100 | 26.2 | 3.82 | 2 | 8.69 | 16.32 |
| | | | | 0.2 | 6.77 | |
| | | | | | | |
| | | | | | | |

Table 3.1: Summary of tests conducted with vertical indentors

| TEST | Indenter width (mm) | Indenter angle (degrees) | Ice thickness (mm) | Test speed (mm/s) | Mean force (kN) | Peak force (kN) | Failure mode |
|-----------------|---------------------|--------------------------|--------------------|-------------------|-----------------|-----------------|--------------|
| Fresh3-III-Run3 | 120 | 30 | 26.7 | 400 | 1.09 | | C,F |
| | | | | 200 | 0.84 | | F |
| | | | | 100 | 0.65 | | F |
| | | | | 50 | 1.35 | | F |
| Fresh3-LO-Run3 | 120 | 30 | 46.3 | 10 | 0.60 | 1.88 | F |
| 400 | | | | 2.99 | 5.07 | C | |
| 200 | | | | 2.50 | 6.03 | C | |
| 100 | | | | 1.24 | 4.13 | F,C | |
| Fresh4-LO-Run1 | 120 | 20 | 46.3 | 50 | 2.39 | 4.77 | C |
| | | | | 20 | 0.55 | 4.29 | F |
| | | | | 10 | 1.19 | 4.17 | F |
| 400 | | | | 4.70 | 8.84 | C | |
| 200 | | | | 3.89 | 8.40 | C | |
| 100 | | | | 3.90 | 10.04 | C | |
| 50 | | | | 4.61 | 13.61 | C | |
| Fresh4-LO-Run2 | 120 | 10 | 46.3 | 10 | 1.31 | 9.93 | F |
| 400 | | | | 7.88 | 24.11 | C | |
| 200 | | | | 9.27 | 15.52 | C | |
| 100 | | | | 13.66 | 32.73 | C | |
| Fresh4-III-Run3 | 120 | 30 | 35.6 | 50 | 13.62 | 27.84 | C |
| | | | | 400 | 1.92 | 4.07 | C,F |
| | | | | 200 | 1.08 | 3.96 | F |
| 100 | | | | 1.07 | 3.06 | F,C | |
| Fresh5-LO-Run1 | 120 | 20 | 35.6 | 50 | 1.12 | 2.36 | C |
| | | | | 20 | 0.55 | 2.80 | F,C |
| | | | | 10 | 0.33 | 2.89 | F |
| 400 | | | | 1.56 | 5.58 | F | |
| 200 | | | | 0.67 | 5.19 | F | |
| 100 | | | | 0.15 | 4.56 | F | |
| 50 | | | | 0.31 | 8.06 | C | |
| Fresh5-LO-Run2 | 120 | 10 | 35.6 | 20 | 0.43 | 5.10 | F |
| 10 | | | | 0.45 | 4.84 | F | |
| 400 | | | | 7.67 | 19.70 | C | |
| 200 | | | | 6.47 | 10.10 | C | |
| Fresh5-III-Run3 | 120 | 5 | 35.6 | 100 | 8.10 | 23.70 | C |
| | | | | 50 | 7.53 | 20.92 | C |
| | | | | 400 | 6.79 | 21.91 | C |
| 200 | | | | 5.17 | 20.67 | C | |
| Fresh5-III-Run4 | 120 | | | 100 | 3.98 | 13.44 | C |
| | | | | 50 | 12.40 | 27.03 | C |
| | | | | 20 | 2.00 | 23.15 | F,C |
| | | | | 10 | 2.24 | 24.14 | F,C |

Table 3.2: Summary of tests conducted with inclined indentors

using the mean intercept length method (Dieter, 1974) which gives good results for strictly columnar ice (Cole, 1989). This grain size was between 1.35 mm and 1.64 mm for all ice sheets. Typical sections are shown in Figures 3.2 and 3.3.

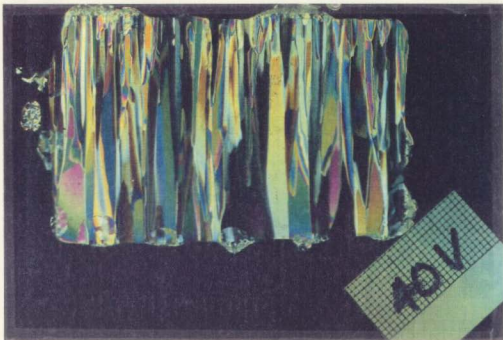


Figure 3.2: *Vertical section of 40 mm ice sheet (Fresh5)*

Ice properties were measured before and after testing. The flexural strength (σ_f), the elastic modulus (E) and the density (ρ) were tested before the first run of each day. The flexural strength of the ice depends on the direction of loading, and is generally higher when loaded downwards. The flexural strength of the ice was tested in both the downward-breaking and upward-breaking modes. The ice continues to grow slightly during a day of testing, and the ice thickness (h) was measured at different points along the broken channel after each run to record

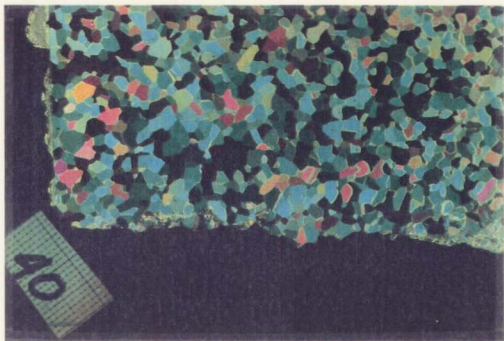


Figure 3.3: *Horizontal section of 40 mm ice sheet (Fresh5)*

variations with respect to tank position and time. A summary of average ice properties measured for each sheet is presented in Table 3.3.

| Ice Sheet | h_{NOM} (mm) | h_{AVG} (mm) | σ_f (kPa) | E (MPa) | E/σ_f | L_c (cm) | ρ (kg/m ³) |
|-----------|-------------------|-------------------|---------------------|--------------|--------------|---------------|--------------------------------|
| Fresh 1 | 30 | 27.5 | ↓ 1043.5 ↑ 996.5 | | | | |
| Fresh 2 | 40 | 35.9 | ↓ 902.0 ↑ 841.5 | 5867.3 | 6664 | 126 | 916 |
| Fresh 3 | 30 | 26.7 | ↓ 1048.5 ↑ 884.7 | 5892.8 | 5261 | 100 | 917 |
| Fresh 4 | 50 | 46.3 | ↓ 911.5 ↑ 682.0 | | | | 918 |
| Fresh 5 | 40 | 35.6 | ↓ 927.0 ↑ 809.5 | 5750.7 | 6270 | 119 | 918 |
| Fresh 6 | 30 | 26.2 | ↓ 1005.5 ↑ 951.0 | 4659.5 | 4561 | 90 | 919 |

Table 3.3: *Summary of ice properties*

Chapter 4

RESULTS AND ANALYSIS: VERTICAL INDENTORS

4.1 Failure modes

Visual records in the form of still photographs and video-tape were used in conjunction with first-hand observations to examine the failure mode of the ice during each test. Particular failure modes also have characteristic force-time records, and examination of these records can help verify the occurrence of a specific type of ice failure. Plots of all data for tests Fresh6_HI.Run2 and Fresh6_LO.Run2 ($D = 100mm$, $h = 30mm$, $V = 0.2, 2, 10, 20, 50, 100, 200$ and $400mm/s$) are presented in Appendix A.

4.1.1 Brittle failure

Tests performed at velocities from 10 mm/s to 400 mm/s induced brittle ice failure. This range corresponds to "strain rates" from $4 \times 10^{-2} \text{ s}^{-1}$ to 2.5 s^{-1} . The "strain rate" for vertical edge-indentation has been used by Timco (1986) and others as $(V/2D)$ for low aspect ratios (0.5). Other expressions for strain rate include V/D and $V/4D$. All these expressions imply that the stress in the ice caused by indenter penetration is distributed through the ice up to a distance of the order of magnitude of the indenter width. Jordaan and Timco (1988), however, have subsequently shown that almost the entire ice strain is absorbed in the crushed layer, and a much smaller length of the ice sheet than $2D$ should be used to determine the true strain rate. For the purposes of comparison with previously published results, $V/2D$ will be retained as a normalized velocity term but will be referred to as "indentation rate".

Examples of force-time traces recorded at different velocities are shown in Figure 4.1. A sawtooth type force trace indicative of intermittent crushing failure was observed at intermediate velocities. A harmonic force-time trace indicative of continuous crushing, and often an unusual "double-beat" force-time trace were observed at high velocities.

The dominant failure mode for all these tests was crushing with radial cracking and spalling. Radial cracks were generally 1 to 2 m in length, but sometimes extended for meters through the ice. These cracks originated near the corners and the center of the face of the indenter. As the test speed increased, the length of the radial cracks decreased. When more than one radial crack formed, circumferential cracking sometimes occurred at distances up to 2 m from the indenter. At intermediate speeds (10, 20, 50 and 100 mm/s) the crushed ice

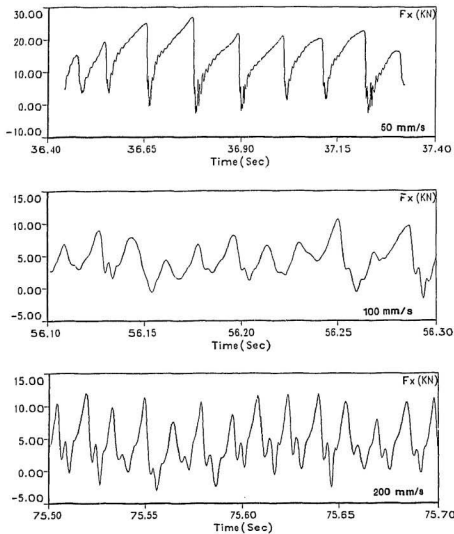


Figure 4.1: Typical force-time histories for tests with brittle failure: a) sawtooth; b) harmonic; c) "double-beat" (Test Fresh6.HI_Run2)

was ejected in spurts. For some tests a pronounced banging sound accompanied crushing events. These tests tended to be those in which the highest indenter loads and greatest indenter displacements were observed.

At high speeds (200 and 400 *mm/s*) crushing usually occurred in a more continuous manner. A steady spray of crushed ice was ejected from the indenter-ice interface up to 1.5 *m* ahead of the indenter. Long radial cracks did not always form. More common was the formation of short (20 to 30 *cm*) 45° radial cracks at both corners of the indenter at regular intervals. Circumferential cracks formed infrequently, and at smaller distances from the indenter face (< 1 *m*) than for intermediate speed tests.

Extensive microcracking took place in the region immediately in front of the indenter, indicated by the "clouding" of the ice. This region was roughly of semi-circular shape and extended about one indenter width into the parent ice sheet. At slower velocities (2 to 50 *mm/s*), shorter networks of cracks would sometimes emanate from points along the primary radial cracks (see Figure 4.2). Microcracking would occur at the ends of the "branches", although to a much smaller extent than immediately in front of the indenter. There was always a noticeable time gap (of the order of seconds) between the formation of the original large radial crack and the formation of the offshooting networks. The networks did not form at higher velocities (100 to 400 *mm/s*).

Thin sections of two ice samples taken from in front of the indenter immediately after two different 400 *mm/s* tests are shown in Figure 4.3. The horizontal thin section shows damage to the parent ice sheet caused by stress concentrations at the indenter edge. The resulting structure consists of grains many times smaller than those of the parent ice. The vertical thin section reveals a cleavage crack in the plane of the ice sheet at the end of a test.

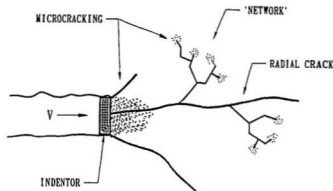


Figure 4.2: Microcracking activity during indentation, including networks and associated microcracking at low velocities

4.1.2 Ductile failure

"Ductile" behaviour was predominant for indentation rates below $1.25 \times 10^{-2} \text{ s}^{-1}$ (2 and 0.2 mm/s tests). Although the overall response of the ice at these test speeds can be characterized as "ductile", it must be emphasized that microcracking and larger local fracture damage the ice immediately in front of the indenter, leading to crack-enhanced viscous flow. A brief burst of cracking activity was followed by a long period where the indenter extruded the damaged material from the ice-structure interface in a viscous manner. Typical force-time traces from slower speed tests are shown in Figure 4.4. The rounded peaks of the force-time traces are indicative of ductile failure.

As the indenter progressed into the ice, a large radial crack usually formed at the center of the indenter face and extended up to 2 m into the parent ice sheet. Occasionally, a second large radial crack formed from the edge of the indenter face.

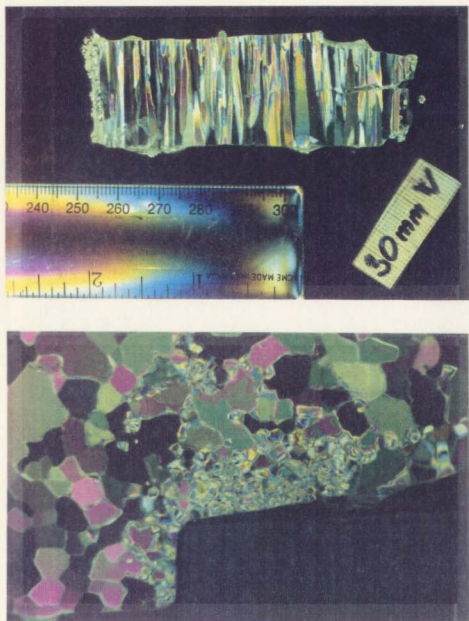


Figure 4.3: *Top: Vertical thin section with in-plane cleavage crack; Bottom: Horizontal thin section with damage to parent ice sheet*

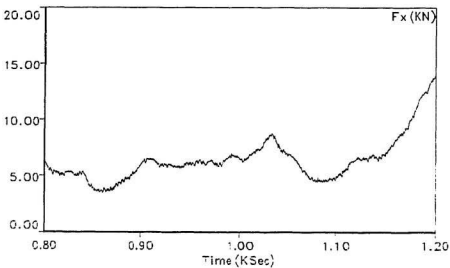
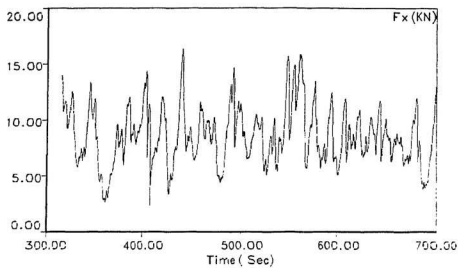


Figure 4.4: Typical force-time traces from slow speed tests (Top: 2 mm/s; Bottom: 0.2 mm/s)

The ice sheet was often deflected downwards during these slower tests, flooding up to 0.6 m in front of the indenter for 2 mm/s tests, and up to 2 m in front of the indenter for 0.2 mm/s tests. Buckling was responsible for this flooding. For some tests 1 or 2 circumferential cracks formed, at distances up to 2 m from the indenter face. At the indenter-ice interface, highly-damaged ice “flowed” from the contact region in a generally continuous fashion, accompanied by a high squeaking sound. The ice extruded from the interface was usually a partially fused “curl” of rod-shaped ice pieces (see Figure 4.5) with a “diameter” of 3 to 7 mm, and a length roughly the same as the indenter width.

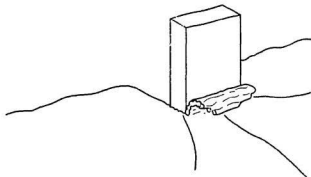


Figure 4.5: *Illustration of ice extruded from indenter-ice interface during slow speed tests (2 and 0.2 mm/s)*

4.2 Peak pressures

The peak force on the indenter face ($F_{x_{peak}}$) for each test was found using the DAS.CALC software at the IMD. The highest force measured was 29.14 kN for test Fresh6_HI.Run3 at 50 mm/s. This was a 120 mm wide vertical indenter in 30 mm thick ice. Peak pressures were calculated assuming a contact area of Dh ,

the indenter width times the thickness of the ice sheet, such that:

$$P_{peak} = \frac{F_{x_{peak}}}{Dh} \quad (4.1)$$

The actual contact area is certain to have varied between this maximum value (Dh) and lower values, due to the effect of spalling at the top and bottom of the ice sheet. Since the collection of spall samples was not continuous, and the actual shape of the contact area at the time the peak force was induced is not known, the apparent contact area (Dh) was used to determine peak pressures. The duration of indentation will also have an effect on the peak pressure. Keeping all other test parameters constant, a longer test time is likely to produce a higher peak load than a shorter test. This should be kept in mind when considering the comparisons of the peak pressures reported in the previous literature and the current tests presented in the following sections.

During test series Fresh1_HI, Fresh2_HI and Fresh3_HI, F_x was sampled at 2000 Hz and passed through a 1 Hz (not 1 kHz as intended) anti-aliasing filter. The peak forces determined from the resulting signal could not be included in the following analyses with confidence, and the data from the affected tests was not used.

4.2.1 Aspect ratio effect

A plot of peak pressure vs. aspect ratio including data from previous similar experiments (vertical indentation, freshwater ice, planar indenter, and aspect ratios between 1 and 5) is shown in Figure 4.6 (Nakazawa and Sodhi, 1990; Timco, 1986; Michel and Blanchet, 1983; Zabilansky *et al.*, 1975). Aspect ratio varied between 1.7 and 4.6 and the structure can be considered narrow. Peak pressures ranged

from 4 to 11.3 MPa, although most were below 8 MPa. Peak pressure exhibited a slight decline with increasing aspect ratio. The present results agree with the previous work and a slight decrease in peak pressure with increasing aspect ratio is exhibited. As the aspect ratio increases the relative amount of pure crushing making up the failure mode as a whole decreases, and radial and circumferential cracking and spalling activity increases. These failure mechanisms exert lower loads on the indenter face than crushing, and the overall effect is a reduction in total force on the indenter.

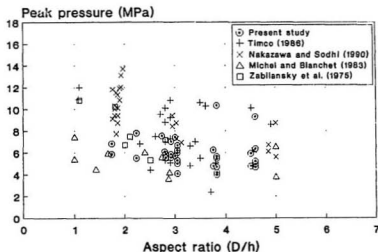


Figure 4.6: Peak pressure vs. aspect ratio (D/h), including previous work (Nakazawa and Sodhi, 1990; Timco, 1986; Michel and Blanchet, 1983; Zabilansky et al., 1975).

4.2.2 Velocity effect

Velocity is usually normalized with respect to the length of ice loaded during indentation to derive a test “strain rate”. As described in Section 4.1.1, the traditional normalized velocity term of $V/2D$ is not a true strain rate, and should not be referred to as such. For the purposes of comparison with previously published results, $V/2D$ will be retained as a normalized velocity term but will be referred to as “indentation rate”.

A plot of peak pressure vs. indentation rate including previously published results (Nakazawa and Sodhi, 1990; Timco, 1986; Michel and Blanchet, 1983; Zabilansky *et al.*, 1975) is shown in Figure 4.7. The data agrees well with the previous results. For the present tests, indentation rate varied between $8 \times 10^{-4} \text{ s}^{-1}$ and 2.3 s^{-1} , and appeared to have some effect on peak pressure. Peak pressure appears to increase consistently, however slightly, with indentation rate up to $V/2D = 0.2 \text{ s}^{-1}$, after which a dip occurs. This dip coincides with the transition from intermittent crushing to continuous crushing, and is associated with a change in the behaviour of the structure from static to dynamic. This drop will be discussed in detail when indenter dynamics are addressed in Section 4.3.

4.2.3 Contact area effect

A “scale effect” of decreasing pressure with increasing contact area has been reported by Sanderson (1986). A plot of peak pressure vs. contact area including previously published work (Nakazawa and Sodhi, 1990; Timco, 1986; Michel and Blanchet, 1983; Zabilansky *et al.*, 1975) is shown in Figure 4.8. The present data agrees with previous work. Contact area varied only from 21 cm^2 to 37 cm^2 , and no distinguishable decrease in peak pressure with increasing contact area is

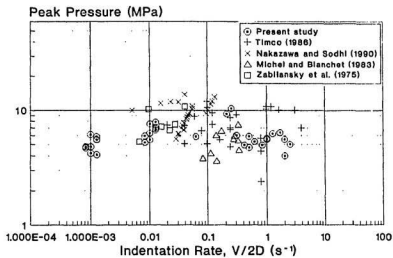


Figure 4.7: *Peak pressure vs. indentation rate ($V/2D$), including previous work (Nakazawa and Sodhi, 1990; Timco, 1986; Michel and Blanchet, 1983; Zabilansky et al., 1975)*

evident. This result is not entirely unexpected, due to the small range of contact areas used in the test series. The small range of contact area compared with previous work has produced a tight cluster of data points from the present study in Figure 4.8. For the sake of clarity, a plot of the present data alone is shown in Figure 4.9.

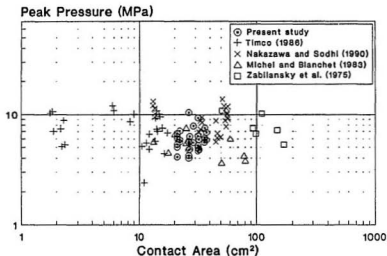


Figure 4.8: *Peak pressure vs. contact area, including previous work (Nakazawa and Sodhi, 1990; Timco, 1986; Michel and Blanchet, 1983; Zabilansky et al., 1975)*

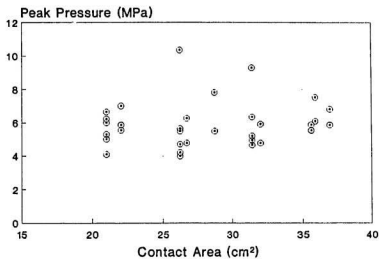


Figure 4.9: *Peak pressure vs. contact area, present study alone*

4.3 Dynamics

4.3.1 Characteristic failure frequency

The characteristic crushing frequency was obtained through spectral analysis of F_z and in some cases, M_y . This generally yielded a power spectrum with a dominant peak at the characteristic failure frequency (see Figure 4.10). When the resultant power spectrum yielded more than one peak with significant power, a visual check of the force-time record was used to verify the dominant failure frequency.

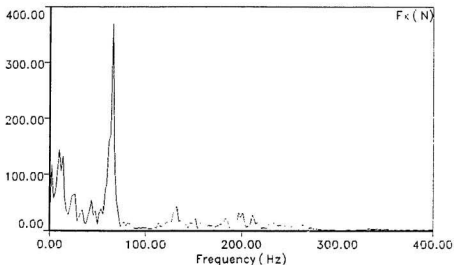


Figure 4.10: *Typical power spectrum of F_z time series*

During test series Fresh1.HI, Fresh2.HI and Fresh3.HI, F_z was sampled at 2000 Hz and passed through a 1 Hz (instead of 1 kHz as in other tests) anti-aliasing filter. This unfortunate error rendered dynamic analysis of this signal useless for the noted tests. Comparison of F_z with M_y for other series where F_z

was properly filtered at 1 kHz (Fresh4.HI, Fresh5.HI, Fresh6.HI, and Fresh1.LO through Fresh6.LO) showed a nearly perfect match of the two signals under all conditions. A plot of F_x and M_y from a properly recorded test (Fresh6.HI.Run2) illustrates this agreement (see Figure 4.11). Although the amplitude of peaks in the M_y spectrum cannot be compared with the amplitude of peaks in the matching F_x spectrum, the frequencies obtained from the M_y spectrum are the same as those which would have been found from a properly filtered F_x signal, as shown in Figure 4.12. Consequently, the M_y time trace from test series Fresh1.HI, Fresh2.HI and Fresh3.HI was used for spectral analysis to determine the characteristic crushing frequency for particular velocities.

Plots of the characteristic failure frequency normalized with respect to the natural frequency of the structure (f/f_n) vs. aspect ratio (D/h), and f/f_n vs. velocity (V) are shown in Figure 4.13 and Figure 4.14, respectively. The natural frequency of the structure was found from plucking tests to be 63 Hz. Variations in characteristic failure frequency occurred predominantly (and in a systematic fashion) only with changes in velocity. Aspect ratio has no apparent effect on the crushing frequency, although the narrow range of aspect ratios used in this test series may not have been sufficient to allow any relationship to emerge.

The frequency of failure reaches a plateau at the natural frequency of the structure as velocity approaches 100 mm/s, and is "locked-in" at the natural frequency of the structure for higher test velocities. The increase in failure frequency up to this plateau is proportional to the normalized velocity, and once the plateau is reached it becomes independent of velocity. This is in agreement with the findings of Neill (1976), Sodhi and Morris (1986) and Singh *et al.* (1990). Singh *et al.* also noted the "locking-in" of the dominant frequency at the natural frequency of the structure over a wide range of velocities. Similarly, velocity did

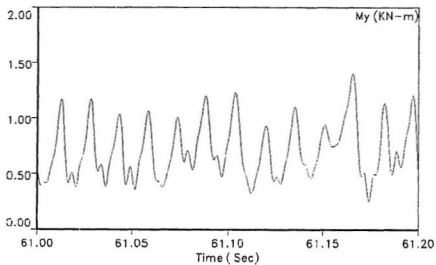
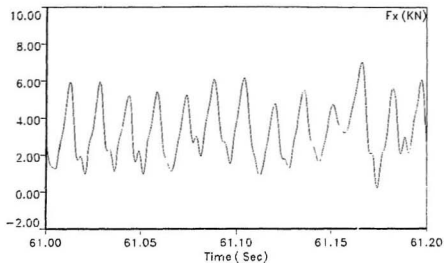


Figure 4.11: Portions of F_x and M_y from test Fresh6_HI_Run2 (50 mm/s)

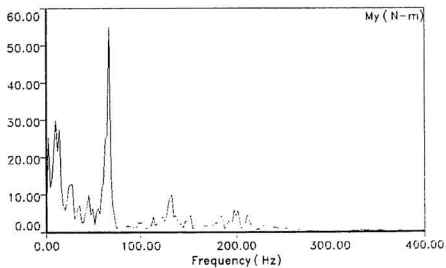
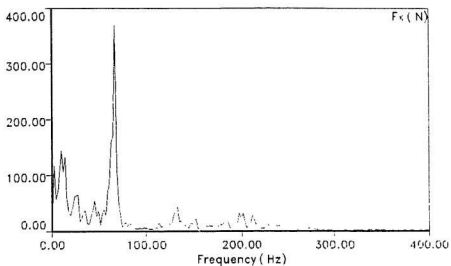


Figure 4.12: Power spectra of F_x and M_y from test Fresh6.HI.Run2 (50 mm/s)

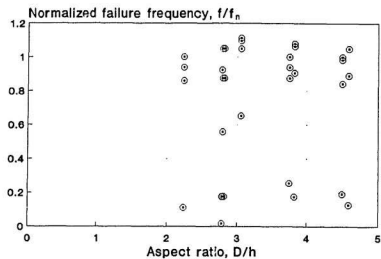


Figure 4.13: Normalized failure frequency vs. aspect ratio

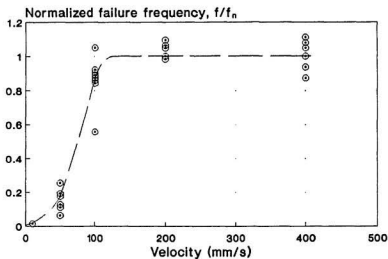


Figure 4.14: Normalized failure frequency vs. velocity

not increase enough to push the dominant frequency above the natural frequency of the structure, but at 200 and 400 mm/s higher frequencies did begin to appear in the spectrum.

Prior to lock-in, the indenter movements are characterized as transient or unsteady, and a sawtooth-shaped force-time trace was recorded. The indenter response decays significantly before the exciting force is again applied by the ice. At velocities above 100 mm/s indenter oscillations become steady at the natural frequency of the structure. Figure 4.15 is a plot of indenter displacement at speeds of 50, 100, 200 and 400 mm/s for test Fresh6-HI.Run2 ($h = 30\text{mm}$, $D = 100\text{mm}$). When the exciting force (crushing) is applied at the same frequency as the natural frequency of the structure a resonant condition should emerge where the structural response is large and the load on the structure required to induce this response is small (Rao, 1986). It can be seen from Figure 4.15 that changes in the response amplitude with increasing velocity are small, although the mean deflection of the indenter increases. At high indentation velocity ($\geq 100\text{ mm/s}$) the intrusion of the crushed layer and the "intact" ice sheet prevents the full rebound of the indenter to the "equilibrium" position (displacement $u = 0$). The mean position of the indenter is shifted in the positive- x direction. This condition is similar to that described by Kärnä and Turenne (1990) as continuous crushing at high velocity. If velocity had increased above 400 mm/s, it is possible that oscillations of the indenter would decrease and a positive constant displacement induced by the mean ice force established, such that $u = F_{\text{mean}}/K$.

Jordaan *et al.* (1991) indicate that the structural stiffness K has a significant effect on the crushing frequency and the amount of ice crushed per cycle. The static indenter stiffness was measured from the plucking tests as $K = 9.4\text{ MN/m}$. The stiffness of the ice, K_I , can be calculated as

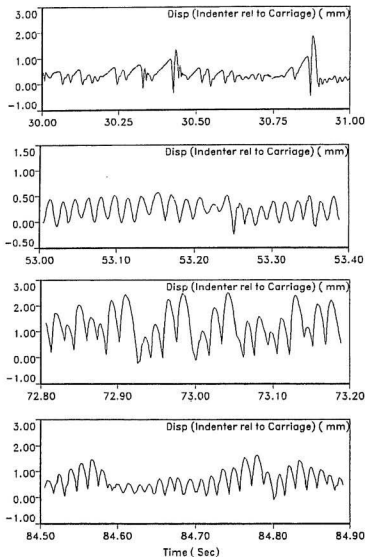


Figure 4.15: Indenter response at velocities of 50 mm/s, 100mm/s, 200 mm/s and 400 mm/s

$$K_I = 0.085\pi Eh \quad (4.2)$$

where the ice is assumed to be a semi-infinite elastic plate and the total load is distributed uniformly over the indenter width (Jordaan and Timco, 1988). For a narrow indenter, a uniform load distribution is a reasonable assumption. Using the values of h from Table 3.3 and $E = 10000 \text{ MPa}$ for rapid loading (Jordaan and Timco, 1988), the stiffness of the ice sheet can be calculated as varying from 70 MN/m to 124 MN/m , and the ratio of ice stiffness to indenter stiffness (K_I/K) ranges from 7.5 to 13. These ratios are considerably higher than the ice to structure stiffness ratio of 4 obtained by Timco (1986), as reported by Jordaan and Timco (1988). Although the absolute stiffness of the present structure is greater than that of Timco's structure, the present structure is at least twice as compliant as that of relative to the ice tested (Timco, 1986).

The amount of ice crushed per cycle and the high-velocity frequency dependence, however, lead to the conclusion that the indenter behaved as a relatively stiff structure when dynamic behaviour was excited. The higher the compliance of a structure, the lower the resulting crushing frequency will be for a given velocity and ice thickness. A more flexible structure will deflect more under a given load and crushing events will occur less frequently. The flexible structure will also release more strain energy and subsequently crush more ice per cycle. The region of velocity dependence in Figure 4.14 between 50 mm/s and 100 mm/s can be approximated by a line of slope $f/f_n V = 0.013$. Multiplying this value by the natural frequency of the structure, f_n , and the thickness of the ice, h , gives a dimensionless number $F = fh/V = 19$. Typically in laboratory scale tests F ranges from 3-5, while for medium scale tests conducted at Pond Inlet, F was as high as 500, and for the large-scale *MOLIKPAQ* events ranged from 20-100

(Jordaan *et al.*, 1991). As the stiffness of the structure increases, F should increase. The structure for the present test series is relatively stiff by this standard, compared to typical laboratory scale tests. This apparent contradiction is due to the different structure stiffnesses under static and dynamic loading. The region between 0mm/s and 50mm/s in Figure 4.14, when indenter behaviour was essentially static, can be approximated by a line having a slope $f/f_n V$ somewhere between 0.0013 and 0.0024. Again multiplying by f_n and h , F is found to range between 2.5 and 4.5. For purposes of comparison, Timco (1986) obtained a value of $F = 3$ (Jordaan and Timco, 1988). When the present structure is statically loaded (at low velocities) it behaves as a relatively flexible structure similar to other laboratory indenter structures. As a constant dynamic response is excited, however, the higher dynamic stiffness produces higher crushing frequencies and shorter damage lengths.

4.3.2 Damage length

When a rigid indenter crushes ice at a frequency f , then each crushing cycle takes $1/f$ seconds and the indenter moves a distance of V/f mm each cycle. This distance V/f is called the damage zone or damage length, l , as discussed in Section 2.2. A portion of the actual length of ice crushed in a single cycle may be sintered together at the end of the extrusion cycle to form a reconstituted mass between the indenter and the original "intact" ice. The presence of the sintered ice mass prevents travel of the indenter through the full damage length, effectively reducing the damage length as determined from the frequency response of the structure. It follows that the crushing length predicted by V/f is an underestimate of the actual crushing length. Unfortunately, it is extremely difficult to experimentally

determine the actual crushing length per cycle.

The ratio of damage length to ice thickness, V/fh , is typically between 0.2 and 0.5 (see Section 2.2). Plots of V/fh vs. aspect ratio (D/h), and V/fh vs. velocity (V) are shown in Figure 4.16 and Figure 4.17 respectively. The damage length ranged between $0.06h$ and $0.48h$, i.e. between 6% and 48% of the ice thickness was crushed in each cycle. Most values, however, were below about $0.25h$. Aspect ratio has no discernible effect on V/fh , while velocity has a definite effect.

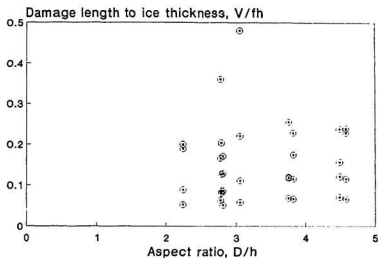


Figure 4.16: *Damage length to ice thickness ratio vs. aspect ratio*

For velocities below 50 mm/s , the damage length was usually between $0.1h$ and $0.2h$. Damage lengths up to about 50% of the ice thickness were calculated. These values are in agreement with the lower range of values suggested by previously published results. As discussed in Section 4.3.1, the compliance of the structure has a significant effect on its dynamic response. Typical values of fh/V for laboratory scale indentation tests range from 3-5, while values of fh/V for the

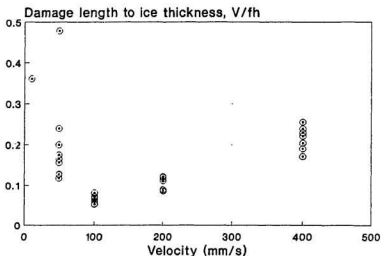


Figure 4.17: *Damage length to ice thickness ratio vs. velocity*

present tests are near 20, indicating high stiffness. Consequently, lower damage lengths are produced. At the point where locking-in of the characteristic failure frequency occurs ($V \approx 100 \text{ mm/s}$), the value of V/fh drops to 0.06 and then begins increasing linearly with velocity. As f is locked near the natural frequency of the structure, the value of V/fh becomes directly dependent on V , increasing accordingly.

4.3.3 Higher frequency observations

Figure 4.18 is a plot of the F_x trace and the indenter displacement-time trace from a 200 mm/s test (Fresh6.HI.Run2). The force trace exhibits a steady-state double beat pattern with two distinct peaks in every full cycle. The largest peak generally occurs at the maximum indenter displacement and coincides with a crushing event, while the smaller peak occurs as the indenter rebounds and may

be associated with a second crushing event or some extrusion process. This implies that there are two out-of-phase failure processes occurring at a frequency near the natural frequency of the structure. Occasionally, however, a smaller peak can be observed on the “up-swing” of the larger force peak. A more likely explanation of the double beat force-time trace is the superposition of two frequency components in the force: one at the natural frequency of the structure and another at its higher frequency of vibration. The power spectrum of this time series is shown in Figure 4.19 and confirms the presence of two distinct frequencies at approximately 65 *Hz* and 200 *Hz*. A frequency component near 200 *Hz* was observed in several other tests. If this component was evidence of ice failure at some frequency above the natural frequency of the structure, it would have some variability. The constancy of the higher frequency at ≈ 200 *Hz* indicates that it is the result of excitation of some different mode of structural vibration. A complete dynamic analysis of the indenter-carriage system must be performed to confirm the existence of this higher frequency in the structure, to ensure that it is not related to some ice failure phenomenon such as the extrusion process.

4.4 Sieve analysis

A portion of the crushed ice mass extruded from the indenter-ice interface was collected and passed through a series of 4 sieves to determine the size distribution of the crushed particles. The ranges of particle sizes, as determined by sieve sizes, were > 4.76 *mm*, 4.76-2.38 *mm*, 2.38-1.19 *mm*, 1.19-0.85 *mm*, and < 0.85 *mm*. The top sieve usually contained a number of larger ice pieces spalled from the parent sheet during indentation. The typical spall was roughly oval-shaped, with a thickness of less than 5 *mm* and dimensions of approximately 20 \times 30 *mm*.

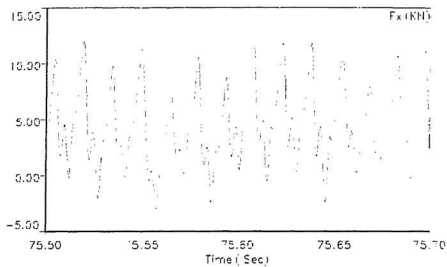


Figure 1.18: Portion of F_x time series with double beat pattern

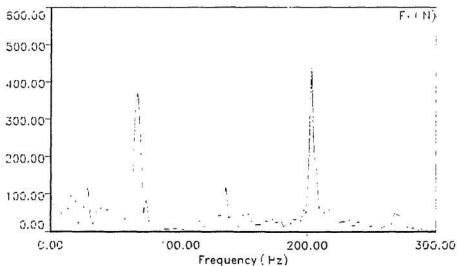


Figure 4.19: Power spectrum of double beat time series, showing two distinct frequencies

A plot of the percentage of crushed ice passed through each sieve for different velocities is shown in Figure 4.20.

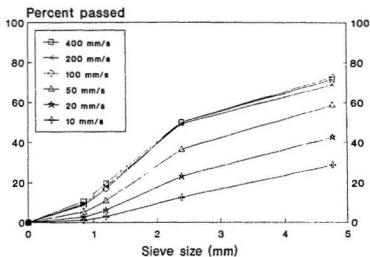


Figure 4.20: Sieve analysis results: percentage passed vs. sieve size

The increase in percent passed with increasing velocity indicates that the fineness of the crushed ice particles increases with velocity. After the ice is initially crushed, further grinding and crushing take place within the crushed layer as the particles are extruded from the ice-structure interface. The increase in particle fineness with velocity may be attributed to an increase in the amount of further crushing within the layer at higher velocities.

It is worth noting that some of the particles ejected from the ice-structure interface are actually several particles joined together by either re-freezing or some sintering process, and the particle sizes determined by the sieve analysis are almost certainly larger than the actual initial sizes of the crushed grains. The sliding of

particles within the crushed layer will induce friction melting on the surface of the particles. High local pressures can exist within the crushed layer as well, inducing pressure-melting and possibly sintering of particles. If inter-granular motion stops while several wetted particles are in contact, they can re-freeze to form a larger single particle. Examination of individual crushed particles was not performed for the present tests. Examination of particles from the 1990 Hobson's Choice Ice Island tests definitely revealed that some of the ejected crushed particles are re-frozen or sintered groups of smaller particles (Kenny *et al.*, 1991).

Chapter 5

RESULTS AND ANALYSIS: INCLINED INDENTORS

5.1 Failure modes

Visual records in the form of still photographs and videotapes were used in conjunction with first-hand observations to examine the failure mode of the ice during each test. Of particular interest was the transition from crushing failure to flexural failure as ice thickness h , indenter angle α and test speed V varied. Tests were performed at velocities from 10 mm/s to 400 mm/s and indenter angles of 5° , 10° , 20° and 30° from a vertical plane. Nominal ice thicknesses were 30 mm , 40 mm and 50 mm . Plots of all data from tests Fresh5.III.Run2 and Fresh5.I.O.Run2 ($D = 120\text{ mm}$, $h = 40\text{ mm}$, $\alpha = 20^\circ$, $V = 10, 20, 50, 100, 200$ and 400 mm/s) are presented in Appendix B.

Three primary failure modes were observed: continuous crushing; mixed crush-

ing and flexure; and pure flexural failure. Continuous crushing occurs when no flexural failure events are observed during a test. This failure mode may also contain shear failure adjacent to the indenter face. If the crushing is interrupted by sporadic flexural events, the failure was described as "mixed mode". If flexural failure is regular the failure mode is said to be pure flexure, even though short periods of crushing may occur before each event. Examples of the force-time series for each of these failure modes are shown in Figure 5.1.

For the 5° and 10° indentors continuous crushing dominated. Radial and circumferential cracking patterns similar to those for the vertical indentors were observed. Usually, two radial cracks formed from the corners of the indenter at the onset of indentation, and occasionally a third radial crack formed from the center of the indenter face. At speeds between 10 and 50 mm/s , these cracks could extend up to 5 m into the intact ice sheet. As the velocity increased, the length of the radial cracks shortened and tended to form only at the indenter corners. For 400 mm/s tests, a cracking pattern often observed was regular, short radial cracks shooting into the ice at 45° from the indenter corners. These cracks were about 0.5 m long and were separated by approximately 10 cm spacings along the broken track. Circumferential cracks sometimes formed at a radius of about 1 m from the indenter face. Despite the formation of circumferential cracks, the indenter usually continued crushing the ice without rotating and clearing the broken ice piece as expected for an inclined indenter. The likelihood of circumferential cracking, and the radius of any cracks, decreased as velocity increased.

For the 20° and 30° indentors, indenter velocity and ice thickness had the greatest effect on failure mode. At test speeds of 20 and 10 mm/s , the ice failed predominantly in flexure, with short periods of crushing sometimes occurring prior to a flexural event. At higher speeds (50 to 400 mm/s) the failure mode was

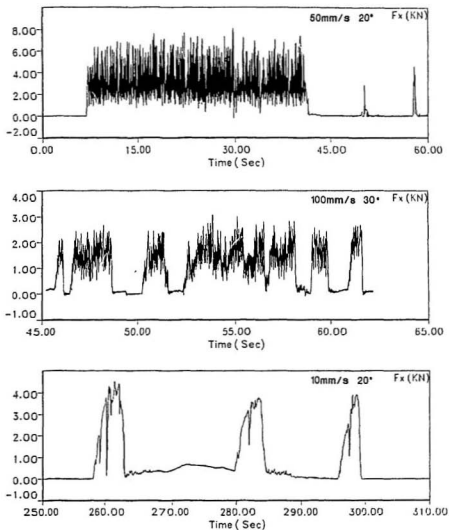


Figure 5.1: Typical force-time histories from inclined indentation tests: a) continuous crushing; b) mixed crushing and flexure; c) pure flexure

influenced by ice thickness, with flexural failure events occurring less often in thicker ice. The flexural failure events were characterized by the formation of multiple circumferential cracks, usually two at a time, and sometimes even three at a time. When flexural failure dominated, radial cracks sometimes formed after circumferential cracking. The first circumferential crack usually formed at a radius between 0.75 m and 1.5 m from the indenter face. A fraction of a second later, a second "subsidiary" circumferential crack almost always formed about 0.1 to 0.3 m from the indenter face. The subsidiary circumferential crack (closer to the indenter) would form a discrete ice slab which would rotate and clear. The length of the broken ice piece was the distance of the second crack from the indenter, while the width was sometimes over 1 m. If the piece was large, it was often rotated and "sandwiched" between the advancing indenter and the level ice edge and broken into smaller pieces. When the indenter next contacted the ice edge, flexural failure would occur at the next (previously-induced) circumferential crack, and the load required to induce this failure was correspondingly lower. Typically, a large peak force where two or three circumferential cracks were formed would be followed by one or two peaks between 25% to 75% of the first peak, as described above. Each peak is separated by a stretch of low or zero load as the indenter traverses open water or clears broken pieces. Figure 5.2 is a portion of the F_z time series for $V = 20 \text{ mm/s}$ from Fresh5.LO.Run2 featuring the formation of a principal circumferential crack and two subsidiary cracks. A series of sketches illustrating the failure sequence for this portion of the time series is presented in Figure 5.3.

The formation of the subsidiary cracks is due to three possible mechanisms: the formation of a truncated wedge after initial circumferential cracking, buckling failure or shear cracking. These explanations are discussed below. Unfortunately,

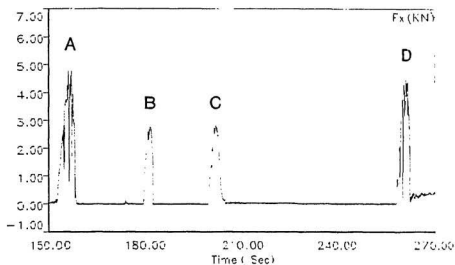


Figure 5.2: Portion of F_x series from test Fresh5.LO-Run2 featuring formation of principal and "subsidiary" circumferential cracks

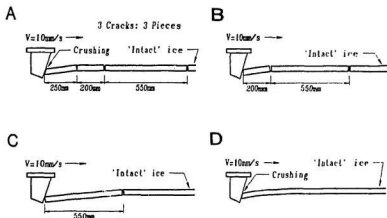


Figure 5.3: Illustration of failure sequence for time series of Figure 5.2

much previous work with inclined structures has concentrated on conical structures, and it will have to be assumed that the failure mechanisms described can be extended to planar surfaces.

The first circumferential crack was not always observed to propagate to the free ice edge. Assuming that just after the first circumferential crack is created two radial cracks emanate from the indenter corners, a truncated wedge is formed. According to Nevel (1972):

$$\frac{6P_w}{b_o\sigma_f h^2} = 1.10 + 2.40(a/L_c) - 0.10(a/L_c)^3 \quad (5.1)$$

and

$$x/L_c = 1.83 + 0.916\nu + 0.292(a/L_c)^2 \quad (5.2)$$

where

$$L_c = \left[\frac{Eh^3}{12\rho_w g} \right]^{1/4}$$

P_w = ultimate vertical load

b_o = a constant, such that $b = b_o x$

b = width of the wedge at a distance x from the wedge tip

x = position of maximum stress, i.e. distance at which failure occurs

a = loading length at wedge tip

ν = Poisson's ratio

ρ_w = density of water

g = gravitational acceleration

E = elastic modulus of ice

For the first peak shown in Figure 5.2, $\sigma_f = 927 \text{ kPa}$, $b_o = 2 \text{ m}$, $h = 35.6 \text{ mm}$, $L_c = 119 \text{ cm}$ and $a = 0.10$. An ultimate vertical load of $P_w = 530 \text{ N}$ is predicted using equation (5.1). From the vertical force-time record for this peak, P_w was measured at 680 N . Nevel's equation (5.2) enables prediction of the distance of cracking. For this case ($a/L_c = 0.10$) and the crack distance is predicted to be about 0.5 m . This agrees well with the distance of 0.45 m associated with the first subsidiary crack in Figure 5.2. The creation of the second subsidiary crack is not explained, however, and the radial cracks (essential for this failure mechanism) were not always observed in cases where the subsidiary cracks formed.

If the indenter angle α is small, and the friction between the ice and indenter surface high, it is conceivable that a high horizontal load could result in buckling failure. The formation of two or three cracks virtually simultaneously is also consistent with buckling failure. After the initial circumferential crack is formed, hinged boundary conditions are created at both the ice-indenter interface (due to the roughness of the indenter surface) and the first crack. A subsidiary crack may form at the halfway distance, a prediction in agreement with observations of the present tests. Buckling is associated with low indentation rates, wide structures and thin ice, however, none of which characterize the present tests. Timco (1986) predicts that buckling will occur at indentation rates below 0.03 s^{-1} ($V \approx 7 \text{ mm/s}$ for the present test geometry) for low aspect ratios. In a recent survey of all buckling failures observed in laboratory scale indentation tests, Blanchet *et al.* (1989) also note that at aspect ratios below 5 and indentation velocities above 10 mm/s , no buckling occurred. The formation of one or two subsidiary cracks occurred at velocities up to 400 mm/s in the present tests.

Wessels and Kato (1988) describe an interesting dependence of the size of the broken ice pieces on the ice-structure friction angle and the thickness of the

ice. For the case of pure bending failure, elastic plate theory predicts the length of broken ice piece to be of the order of magnitude of the characteristic length. It follows that as the characteristic length of the ice increases with increasing thickness, the size of the broken ice piece will increase as well. This correlation has been observed to hold true in experiments with *smooth* structures, where the indentation forces result in pure flexural failure. For rough structures, however, the size of the broken ice pieces is observed to *decrease* with increasing thickness. This is due to a transition from pure flexural failure to combined flexure and shear failure. The higher coefficient of friction of the rougher surface means a greater normal load must be applied to produce the same deflection of the ice sheet. Larger horizontal forces are developed at the interface, and the presence of an out-of-plane deflection leads to shear failure at some distance from the indenter rather than only pure crushing at the interface. Wessels and Kato further note that more than one circumferential crack forms at high velocities for combined flexure and shear. In the case of the present tests the rough surface of the indenter, small indenter inclination, and relatively thick ice make the presence of shear forces highly likely. The subsidiary cracks are probably formed by a combination of both the shear mechanism and dynamic buckling.

At higher speeds (50 to 400 mm/s) the failure mode was influenced by ice thickness, with flexural failure events occurring less often as ice thickness increased. Figure 5.4 shows the dominant mode of failure of each test plotted against indenter angle and velocity normalized with respect to ice thickness. This "map" is divided into three areas: flexural failure, crushing failure, and a mixed region where both modes occurred, sometimes in the same test. Although gaps in the data exist, the map gives a rough indication of the conditions under which a particular mode of failure is likely to occur.

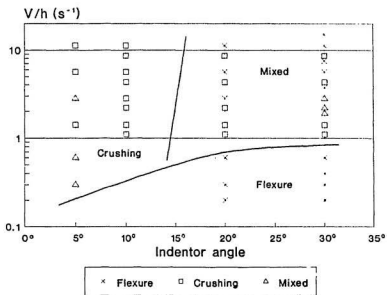


Figure 5.4: Failure mode map for tests with inclined indentors

As velocity increases, it is expected that the inertial resistance of the water to the downward acceleration of the ice sheet will increase, and the failure mode may change from flexure to crushing (Sodhi, 1987). Overall, this was found to be true for this test series, as the total number of flexural failure events decreased with increasing velocity. It was often observed, however, that crushing occurred primarily at the start of a run, i.e. at the first velocity (50 or 20 mm/s) to be tested, and changed to flexure some time into the run. Once one flexural failure was induced, the rest of the run was likely to be dominated by flexural failure. The change to flexure sometimes occurred while the indenter was still moving at the first velocity. The relatively undamaged state of the ice sheet at the start of a test run may allow crushing to continue for a short period of time, until the number of radial and circumferential cracks in the ice reaches a level where flexural failure inevitably occurs. The probability of encountering some flaw in the ice sheet leading to flexural failure also increases with the distance moved through the ice.

5.2 Peak horizontal forces

The peak horizontal force ($F_{x_{peak}}$) on the indenter face was found using the DAS.CALC software at the IMD. This peak force was normalized with respect to the square of the ice thickness h , and the flexural strength of the ice σ_f , to give the “normalized peak horizontal force”, H , such that:

$$H = \frac{F_{x_{peak}}}{\sigma_f h^2} \quad (5.3)$$

All inclined indentors had a width of 120 mm, and the 120 mm vertical indenter

is included in this analysis for purposes of comparison as a 0° “inclined” indenter.

5.2.1 Indentor angle effect

A plot of H as a function of indentor angle is shown in Figure 5.5. The peak forces on the indenter increase as α approaches 0°.

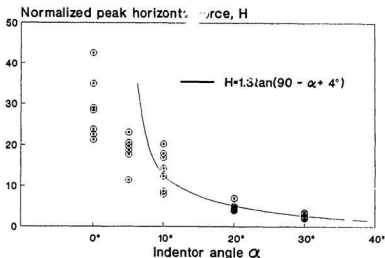


Figure 5.5: Normalized peak horizontal force vs. indentor angle

Previously published studies for inclined indentors have excluded crushing-dominated peak forces (Michel and Picard, 1989; Haynes *et al.*, 1983)) from analysis, and obtained a function of the form $H = a \tan(\alpha + \phi)$, where α is the indentor angle, ϕ the friction angle and a some constant. The solid line in Figure 5.5 represents a best-fit curve of H for indentor angles of 10° and greater (i.e. the curve was not fit to data points at 5° or 0°):

$$H = 1.3 \tan(90 - \alpha + 4^\circ) \quad (5.4)$$

This function greatly overpredicts H for indenter angles close to vertical, where crushing becomes predominant. Equation (5.4) assumes that the ice will fail in flexure, and the resulting peak stress predicted for indenter angles below 10° is much higher than the crushing strength of the ice. The application of equation (5.4) is not valid for conditions where crushing behaviour predominates.

5.2.2 Velocity effect

A plot of the normalized peak horizontal force, H , vs. indenter velocity is shown in Figure 5.6, with each indenter angle plotted as a separate series. The force initially increases to some peak value, then drops at $V/h \approx 2$ and begins increasing once again, although at a slower rate, as velocity increases. This effect becomes less dramatic as the indenter angle increases, and H is almost velocity-independent for the 30° indenter.

The explanation for this behaviour is related to the dynamic response of the structure. For the 0° , 5° and 10° indentors, crushing was the dominant failure mode and the structural response was similar to that for vertical indentors. Once the structural response becomes locked-in at the natural frequency (63 Hz) at V/h near 2, the load decreases to a minimum and again begins increasing with increasing velocity, as detailed in Section 4.3. At indenter angles of 20° and 30° the failure mode is predominantly bending, and the natural frequency of the structure is not excited. Consequently, the initial rise and fall of H noted for lower angle indentors is less dramatic or non-existent.

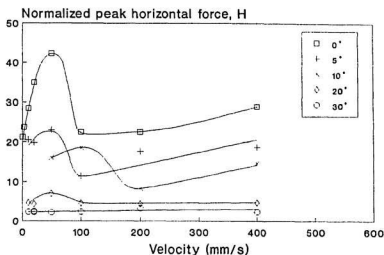


Figure 5.6: *Normalized peak horizontal force vs. indenter velocity*

5.3 Dynamics

From observations of the tests, the first circumferential crack was seen to usually occur at a distance close to the characteristic length of the ice sheet, between 1 and 1.5 m from the indenter face. This agrees well with breaking lengths observed by Frederking and Timco (1985) and Michel and Picard (1989). As discussed in Section 5.1, a second, subsidiary crack usually formed at some point roughly between the initial circumferential crack and the indenter, and sometimes a third subsidiary crack formed even closer to the indenter face. These pieces would rotate and clear, and the indenter would traverse the resulting open water before again contacting the ice edge. The piece sizes used in the following analysis are determined by the shortest cracking distance when more than one circumferential crack was formed. This distance also corresponded to the distance travelled

between flexural failure peaks.

The "single icebreaking frequency" was determined for tests where bending was the dominant mode of failure by performing spectral analysis of the resulting force-time series. These frequencies were double-checked by visually examining the individual time series. For test series Fresh3_HI.Run3, the F_x signal was inadvertently filtered at 1 Hz (instead of at 1 kHz as for other tests) and rendered useless for spectral analysis. As detailed in Section 4.3, the properly recorded M_y signal was used for this test to determine the frequency content of the horizontal force on the indenter. A total of 18 data points were obtained where bending failure dominated (four from test Fresh3_HI.Run3). Figure 5.7 is a plot of the single icebreaking frequency vs. velocity. A trend of increasing frequency with velocity is evident.

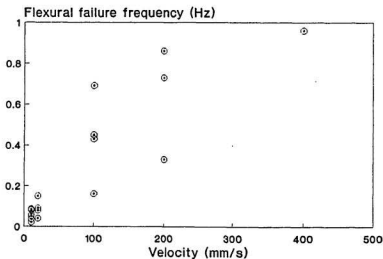


Figure 5.7: Single icebreaking frequency vs. velocity

From the single icebreaking frequency the average broken ice piece length

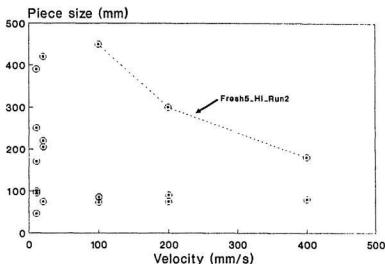


Figure 5.8: *Broken ice piece size vs. velocity*

can be determined. The period ($1/f$) times the test velocity gives the distance travelled between flexural events, which is presumed close to the broken ice piece size. Even when flexure was the dominant failure mode, however, a portion of the intact sheet was usually crushed before bending failure occurred for many tests. A better method of determining broken ice piece size, then, is to measure the time between flexural failure and new contact between the indenter and ice sheet (i.e. the time where the force on the indenter is at zero or some very low value) and multiply this value by the test velocity. This method of calculating broken piece size gave values ranging from 100 mm to almost 500 mm, which agree well with observed broken ice piece sizes. A plot of broken ice piece size vs. velocity is presented in Figure 5.8. The dynamic effect of decreasing broken piece size with increasing velocity as observed by Valanto (1989) is not clearly demonstrated here, probably due to the limited number of data points. For test Fresh5_HII_Run2,

however, a definite decrease in piece size is observed with increasing velocity, as indicated by the dashed line in Figure 5.8. The maximum piece size decreases from 450 mm at 100 mm/s to about 200 mm at 400 mm/s. The smallest piece sizes, however, were also observed at the lowest test velocities.

The characteristic length of the ice sheets ranged from 0.90 m to 1.26 m (see Table 3.3). A plot of the ratio of piece size to characteristic length vs. velocity is shown in Figure 5.9. Most failure occurred at between 10% and 40% of the characteristic length. These values are lower than those reported by Frederking and Timco (1985) and Michel and Picard (1989), due to the formation of one or more subsidiary circumferential cracks during failure.

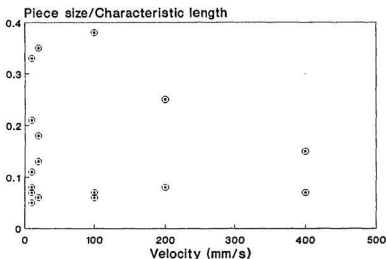


Figure 5.9: Ratio of broken ice piece size to characteristic length vs. velocity

Chapter 6

CONCLUSIONS

The vertical indentation experiments produced several results similar to those observed by several previous researchers. The indentors used were relatively narrow (aspect ratio ranged from 1.7 to 4.6), and brittle crushing was the dominant failure mode. Radial cracking, spalling and occasional circumferential cracking were also observed. These failure modes occurred at combinations of velocity and aspect ratio which closely followed the "failure mode map" developed by Timco (1986) for flat vertical indentors. The maximum force on the structure was 29.1 *kN* and peak pressures (averaged over the indenter area) ranged from 4 to 11 *MPa*, in good agreement with previous work. Comparisons of peak pressure between different experiments must consider the duration of individual test runs, however, as a longer test run will usually produce a higher peak pressure. The variation of peak pressures as velocity, ice thickness and indenter width changed confirmed behaviour observed by previous researchers. As aspect ratio increased the peak pressure on the structure slightly decreased. The failure mode at higher aspect ratios consisted of a lower proportion of pure crushing failure and increas-

ing proportions of spalling and radial and circumferential cracking. Indentation rate had an effect on peak pressure as well. Peak pressure increased slightly with velocity until a steady vibration was induced in the structure somewhere between test velocities of 50 mm/s and 100 mm/s. Once this dynamic response emerged, the load exerted on the structure dropped.

This transition from a static loading condition to a dynamic loading condition occurred, as stated above, between the velocities of 50 mm/s and 100 mm/s. At velocities below 50 mm/s, ice was crushed intermittently, producing a sawtooth-shaped force-time trace. The ice crushing frequency in this range linearly followed test velocity, and the dimensionless number $F = fh/V$ had a value between 2.5 and 4.5 (see Figure 4.14, Section 4.3). Typically, for relatively compliant laboratory-scale structures F ranges from 3-5, while for stiffer structures F can reach as high as 500. The measured stiffness, K , of the structure was high, but the high in-plane stiffness of the thick freshwater ice produced a relatively compliant ice-structure system. The effort to produce a very stiff structure was somewhat undermined by the high strength and stiffness of the tested ice sheets.

At velocities above 50 mm/s a dynamic loading condition emerged: a harmonic force-time trace was observed and the response frequency of the structure became locked at approximately 63 Hz, the natural frequency of the structure. The response frequency remained locked at 63 Hz even as velocity was increased to 400 mm/s. This behaviour has been reported by several researchers in the literature, including Singh *et al.* (1990). For the region between 50 mm/s and 100 mm/s in Figure 4.14, the value of $F = fh/V$ was found to be approximately 20. The peak pressures exerted on the structure dropped when this dynamic condition emerged, and indenter deflection also decreased. Essentially, the indenter behaved as a stiffer structure than in the static loading condition. The

damage length l , or length of ice crushed with each cycle, ranged from $0.06h$ to $0.5h$. These values are again low compared to typical laboratory results. Due to the relative stiffness of the structure in the dynamic condition, less deflection of the indenter occurs before the crushing strength of the ice is exceeded, and less elastic strain energy is returned to the ice. At very high velocities, 200 mm/s and 400 mm/s , a second frequency near 200 Hz began to appear in the power spectrum of the structure's response. This higher frequency was probably due to the excitation of some different mode of structural vibration rather than ice crushing at a higher frequency or some extrusion phenomenon. A complete dynamic analysis of the indenter-carriage system must be performed to confirm the existence of this higher frequency in the structure. The transition from "static" behaviour to "dynamic" behaviour could have been better studied if more test velocities between 50 mm/s and 100 mm/s had been included in the test series. At 50 mm/s the indenter behaved as a relatively compliant, static structure while at 100 mm/s the "locked-in" condition had been reached.

The inclined indentation tests produced mixed ice failure modes of crushing and flexure. The failure mode was influenced by indenter angle, ice thickness and indenter velocity. Indenter angle affects the proportion of total load applied in the in-plane and transverse directions. If the in-plane load exceeds the compressive strength of the ice before the transverse load produces sufficient deflection and bending stresses to induce a bending failure, the failure mode will be dominated by crushing. Flexural strength is directly related to ice thickness: as thickness increases, flexural strength increases and a higher transverse load is required to fail the ice in bending. Compressive strength is not geometry-related, and if the in-plane load becomes high enough before flexural failure can occur, the failure mode will again be dominated by crushing. Indenter velocity affects the downward

acceleration of the ice sheet and the resulting hydrodynamic inertia, as described by Sorensen (1978). At very high velocities this inertia can impede the transverse deflection of the ice sheet required for flexural failure, and crushing failure can result. These phenomenon were all observed in the present test series: the failure mode became dominated by crushing as indenter angle decreased, as ice thickness increased and indenter velocity increased. A "failure mode map" illustrating this transition (inspired by similar "maps" developed by Timco (1986) and others for vertical structures) was developed and is presented in Figure 5.4.

The largest peak horizontal force on the indenter was 32.7 kN, due to crushing failure. The normalized peak horizontal force H increased as the indenter approached vertical and crushing emerged as the dominant failure mode. For tests where flexural failure dominated (indenter angle $\alpha > 10^\circ$), the function $H = 1.3 \tan(90 - \alpha + 4^\circ)$ provided a good fit to experimental results. An exponentially increasing horizontal force with decreasing indenter angle has been observed and reported by several other researchers, as reported by Sodhi (1986).

A subsidiary cracking phenomenon was observed for many flexural failure events. A principal circumferential crack formed at a distance close to the characteristic length of the ice sheet, followed by one or two subsidiary circumferential cracks closer to the indenter face. High in-plane forces combined with vertical deflection of the ice sheet produced a shear and buckling failure responsible for this subsidiary cracking. The broken ice pieces generated by flexural failure events were subsequently smaller than those predicted by many previous authors, who do not document the formation of any subsidiary cracks. The distance of the initial flexural crack, however, is in agreement with the broken piece lengths reported by Frederking and Timco (1985) and Michel and Picard (1987).

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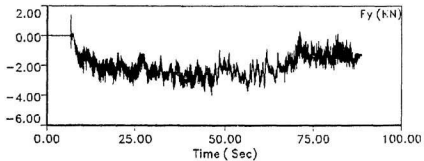
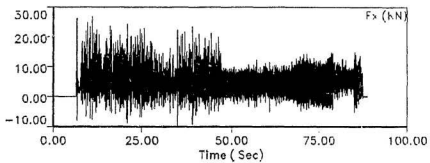
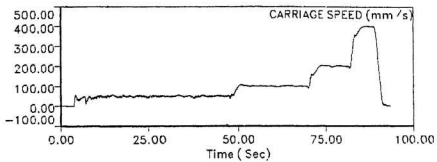
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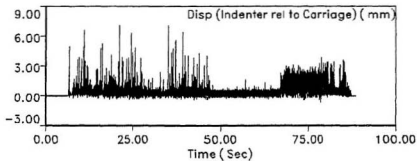
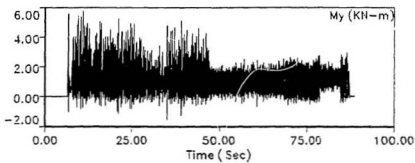
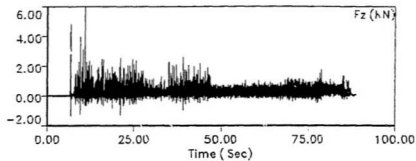
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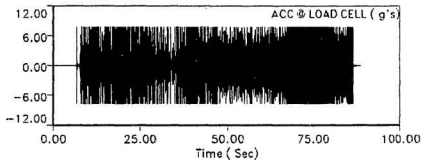
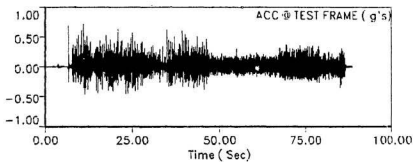
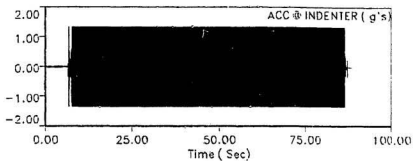
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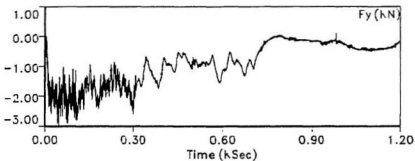
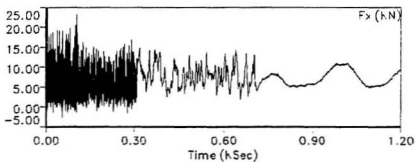
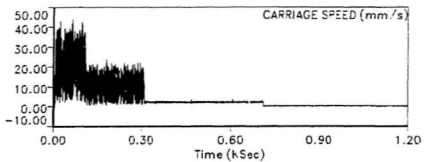
Appendix A

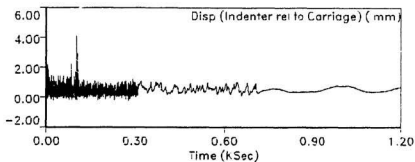
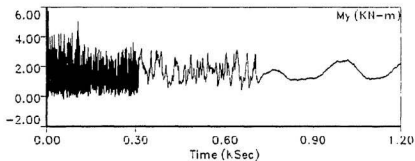
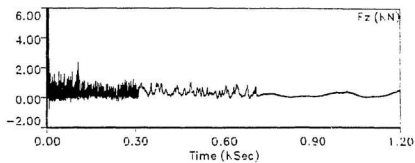
VERTICAL INDENTATION DATA

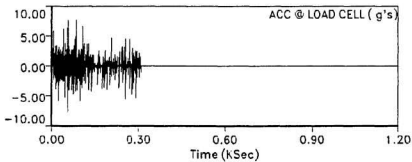
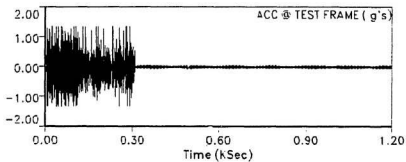
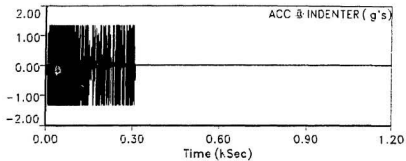












Appendix B

INCLINED INDENTATION DATA

